

EX BIBLIOTHECA



CAR. I. TABORIS.



22101921845

Med

K50269

57-

THE

INTERNATIONAL SCIENTIFIC SERIES.


- I. **FORMS of WATER: a Familiar Exposition of the Origin and Phenomena of GLACIERS.** By J. TYNDALL, LL.D., F.R.S. With 25 Illustrations. Seventh Edition. Crown 8vo. cloth, price 5s.
- II. **PHYSICS and POLITICS; or, Thoughts on the Application of the Principles of 'Natural Selection' and 'Inheritance' to Political Society.** By WALTER BAGEHOT. Fourth Edition. Crown 8vo. cloth, price 4s.
- III. **FOODS.** By EDWARD SMITH, M.D., LL.B., F.R.S. With numerous Illustrations. Fifth Edition. Crown 8vo. cloth, price 5s.
- IV. **MIND and BODY: the Theories of their Relation.** By ALEXANDER BAIN, LL.D. With Four Illustrations. Sixth Edition. Crown 8vo. cloth, price 4s.
- V. **The STUDY of SOCIOLOGY.** By HERBERT SPENCER. Seventh Edition. Crown 8vo. cloth, price 5s.
- VI. **On the CONSERVATION of ENERGY.** By BALFOUR STEWART, M.A., LL.D., F.R.S. With 14 Illustrations. Fifth Edition. Crown 8vo. cloth, price 5s.
- VII. **ANIMAL LOCOMOTION; or, Walking, Swimming, and Flying.** By J. B. PETTIGREW, M.D., F.R.S., &c. With 130 Illustrations. Second Edition. Crown 8vo. cloth, price 5s.
- VIII. **RESPONSIBILITY in MENTAL DISEASE.** By HENRY MAUDSLEY, M.D. Third Edition. Crown 8vo. cloth, price 5s.
- IX. **The NEW CHEMISTRY.** By Professor J. P. COOKE, of the Harvard University. With 31 Illustrations. Fourth Edition. Crown 8vo. cloth, price 5s.
- X. **The SCIENCE of LAW.** By Professor SHELDON AMOS. Third Edition. Crown 8vo. cloth, price 5s.
- XI. **ANIMAL MECHANISM: a Treatise on Terrestrial and Aërial Locomotion.** By Professor E. J. MAREY. With 117 Illustrations. Second Edition. Crown 8vo. cloth, price 5s.
- XII. **The DOCTRINE of DESCENT and DARWINISM.** By Professor OSCAR SCHMIDT (Strasburg University). With 26 Illustrations. Third Edition. Crown 8vo. cloth, price 5s.
- XIII. **The HISTORY of the CONFLICT between RELIGION and SCIENCE.** By J. W. DRAPER, M.D., LL.D. Eleventh Edition. Crown 8vo. cloth, price 5s.

London: C. KEGAN PAUL & CO., 1 Paternoster Square.

- XIV. **FUNGI**: their Nature, Influences, Uses, &c. By M. C. COOKE, M.A., LL.D. Edited by the Rev. M. J. BERKELEY, M.A., F.L.S. With numerous Illustrations. Second Edition. Crown 8vo. cloth, price 5s.
- XV. **The CHEMICAL EFFECTS of LIGHT and PHOTOGRAPHY.** By Dr. HERMANN VOGEL (Polytechnic Academy of Berlin). Translation thoroughly revised. With 100 Illustrations. Third Edition. Crown 8vo. cloth, price 5s.
- XVI. **The LIFE and GROWTH of LANGUAGE.** By WILLIAM DWIGHT WHITNEY, Professor of Sanskrit and Comparative Philology in Yale College, New Haven. Second Edition. Crown 8vo. cloth, price 5s.
- XVII. **MONEY and the MECHANISM of EXCHANGE.** By W. STANLEY JEVONS, M.A., F.R.S. Fourth Edition. Crown 8vo. cloth, price 5s.
- XVIII. **The NATURE of LIGHT, with a General Account of PHYSICAL OPTICS.** By Dr. EUGENE LOMMEL, Professor of Physics in the University of Erlangen. With 188 Illustrations and a Table of Spectra in Chromo-lithography. Second Edition. Crown 8vo. cloth, price 5s.
- XIX. **ANIMAL PARASITES and MESSMATES.** By Monsieur VAN BENEDEN, Professor of the University of Louvain, Correspondent of the Institute of France. With 83 Illustrations. Second Edition. Crown 8vo. cloth, price 5s.
- XX. **FERMENTATION.** By Professor SCHÜTZENBERGER, Director of the Chemical Laboratory at the Sorbonne. With 28 Illustrations. Second Edition. Crown 8vo. cloth, price 5s.
- XXI. **The FIVE SENSES of MAN.** By Professor BERNSTEIN, of the University of Halle. With 91 Illustrations. Second Edition. Crown 8vo. cloth, price 5s.
- XXII. **The THEORY of SOUND in its RELATION to MUSIC.** By Professor PIETRO BLASERNA, of the Royal University of Rome. With numerous Illustrations. Second Edition. Crown 8vo. cloth, price 5s.
- XXIII. **STUDIES in SPECTRUM ANALYSIS.** By J. NORMAN LOCKYER, F.R.S. With Six Photographic Illustrations of Spectra, and numerous Engravings on Wood. Second Edition. Crown 8vo. cloth, price 6s. 6d.
- XXIV. **A HISTORY of the GROWTH of the STEAM ENGINE.** By Professor R. H. THURSTON. With numerous Illustrations. Second Edition. Crown 8vo. cloth, price 6s. 6d.
- XXV. **EDUCATION as a SCIENCE.** By ALEXANDER BAIN, LL.D. Second Edition. Crown 8vo. cloth price 5s.
- XXVI. **The HUMAN RACE.** By Professor A. DE QUATREFAGES, Membre de l'Institut. Crown 8vo. cloth, price 5s.

INTERNATIONAL SCIENTIFIC SERIES.

VOL. XXVII.



Digitized by the Internet Archive
in 2016

<https://archive.org/details/b2806656x>

MODERN
CHROMATICS

WITH APPLICATIONS TO
ART AND INDUSTRY.

BY
OGDEN N. ROOD,

PROFESSOR OF PHYSICS IN COLUMBIA COLLEGE.

WITH 130 ORIGINAL ILLUSTRATIONS.

SECOND EDITION.

LONDON:
C. KEGAN PAUL & CO., 1 PATERNOSTER SQUARE.
1879.

17539

6163 714

Title	
Call	W. H. Omer
Call	
No	WH

TO
DR. WOLCOTT GIBBS

THIS VOLUME IS INSCRIBED,
AS A SMALL MARK OF THE ATTACHMENT
AND ADMIRATION OF
THE AUTHOR.

P R E F A C E .

IT was not my intention to write a preface to this book, as I have usually found such compositions neither instructive nor amusing. On presenting the manuscript to my publishers, however, it was suggested that, although prefaces are of no particular use to readers, yet from a certain point of view they are not without value.

I accordingly beg leave to state that my object in this work has been to present, in a clear, logical, and if possible attractive form, the fundamental facts connected with our perception of colour, so far as they are at present known, or concern the general or artistic reader. For the explanation of these facts, the theory of Thomas Young, as modified and set forth by Helmholtz and Maxwell, has been consistently adhered to. The whole class of musical theories, as well as that of Field, have been discarded, for reasons that are set forth in the text.

Turning now from the more purely scientific to the æsthetic side of the subject, I will add that it has been my endeavour also, to present in a simple and comprehensible manner the underlying facts upon which the artistic use of colour necessarily depends. The possession of these

facts will not enable people to become artists ; but it may to some extent prevent ordinary persons, critics, and even painters, from talking and writing about colour in a loose, inaccurate, and not always rational manner. More than this is true : a real knowledge of elementary facts often serves to warn students of the presence of difficulties that are almost insurmountable, or, when they are already in trouble, points out to them its probable nature ; in short, a certain amount of rudimentary information tends to save useless labour. Those persons, therefore, who are really interested in this subject are urged to repeat for themselves the various experiments indicated in the text.

In the execution of this work it was soon found that many important gaps remained to be filled, and much time has been consumed in original researches and experiments. The results have been briefly indicated in the text ; the exact means employed in obtaining them will be given hereafter in one of the scientific journals.

To the above I may perhaps be allowed to add, that during the last twenty years I have enjoyed the great privilege of familiar intercourse with artists, and during that period have devoted a good deal of leisure time to the practical study of drawing and painting.

O. N. R.

CONTENTS.

CHAPTER I.

	PAGE
TRANSMISSION AND REFLECTION OF LIGHT	9

CHAPTER II.

PRODUCTION OF COLOUR BY DISPERSION	17
--	----

CHAPTER III.

CONSTANTS OF COLOUR	30
-------------------------------	----

CHAPTER IV.

PRODUCTION OF COLOUR BY INTERFERENCE AND POLARIZATION	43
---	----

CHAPTER V.

COLOURS OF OPALESCENT MEDIA	53
---------------------------------------	----

CHAPTER VI.

PRODUCTION OF COLOUR BY FLUORESCENCE AND PHOSPHORESCENCE	62
--	----

CHAPTER VII.

PRODUCTION OF COLOUR BY ABSORPTION	65
--	----

CHAPTER VIII.

ABNORMAL PERCEPTION OF COLOUR AND COLOUR-BLINDNESS	92
--	----

CHAPTER IX.

YOUNG'S THEORY OF COLOUR	108
------------------------------------	-----

CHAPTER X.	
	PAGE
MIXTURE OF COLOURS	124
CHAPTER XI.	
COMPLEMENTARY COLOURS	161
CHAPTER XII.	
EFFECTS PRODUCED ON COLOUR BY A CHANGE IN LUMINOSITY AND BY MIXING IT WITH WHITE LIGHT	181
CHAPTER XIII.	
DURATION OF THE IMPRESSION ON THE RETINA	202
CHAPTER XIV.	
MODES OF ARRANGING COLOURS IN SYSTEMS	209
CHAPTER XV.	
CONTRAST	235
CHAPTER XVI.	
THE SMALL INTERVAL AND GRADATION	273
CHAPTER XVII.	
COMBINATIONS OF COLOURS IN PAIRS AND TRIADS	286
CHAPTER XVIII.	
PAINTING AND DECORATION	305
NOTE ON TWO RECENT THEORIES OF COLOUR	324
INDEX	327

MODERN CHROMATICS.

CHAPTER I.

THE REFLECTION AND TRANSMISSION OF LIGHT.

As long ago as 1795 it occurred to a German physicist to subject the optic nerve of the living eye to the influence of the newly discovered voltaic current. The result obtained was curious : the operation did not cause pain, as might have been expected, but a bright flash of light seemed to pass before the eye. This remarkable experiment has since that time been repeated in a great variety of ways, and with the help of the more efficient electric batteries of modern times; and not only has the original result of Pfaff been obtained, but bright red, green, or violet, and other hues have been noticed by a number of distinguished physicists. If, instead of using the electrical current, mechanical force be employed, that is, if pressure be exerted on the living eye, the optic nerve is again stimulated, and a series of brilliant, changing, fantastic figures seem to pass before the experimenter. All these appearances are distinctly visible in a perfectly dark room, and prove that the sense of vision can be excited without the presence of light, the essential point being merely the stimulation of the optic nerve. In the great majority of instances, however, the stimulation of the optic nerve is brought about, directly or indirectly, by the

aid of light ; and in the present work it is principally with vision produced in this normal manner that we have to deal.

Back in the rear portion of the eye there is spread out a delicate, highly complicated tissue, consisting of a wonderfully fine network woven of minute blood-vessels and nerves, and interspersed with vast numbers of tiny atoms, which under the microscope look like little rods and cones. This is the retina ; its marvellous tissue is in some mysterious manner capable of being acted on by light, and it is from its substance that those nerve-signals are transmitted to the brain which awake in us the sensation of vision. For the sake of brevity, the interior globular surface of the retina is ordinarily called the seat of vision. An eye provided *only* with a retina would still have the capacity for a certain kind of vision ; if plunged in a beam of red or green light, for example, these colour-sensations would be excited, and some idea might be formed of the intensity or purity of the original hues. Some of the lower animals seem to be endowed only with this rudimentary form of vision ; thus it has lately been ascertained by Bert that minute crustaceans are sensitive to the same colours of the spectrum which affect the eye of man, and, as is the case with him, the maximum effect is produced by the yellow rays. With an eye constructed in this simple manner it would, however, be impossible to distinguish the forms of external objects, and usually not even their colours. We have, therefore, a set of lenses placed in front of the retina, and so contrived as to cast upon it very delicate and perfect pictures of objects toward which the eye is directed ; these pictures are coloured and shaded, so as exactly to match the objects from which they came, and it is by their action on the retina that we see. These retinal pictures are, as it were, mosaics, made up of an infinite number of points of light ; they vanish with the objects producing them—though, as we shall see, their effect lasts a little while after they themselves have disappeared.

This leads us in the next place to ask, "What is light, that agent which is able to produce effects which to a thoughtful mind must always remain wonderful?" A perfectly true answer to this question is, that light is something which comes from the luminous body to us; in the act of vision we are essentially passive, and not engaged in shooting out toward the object long, delicate feelers, as was supposed by the ancients. This something was considered by Sir Isaac Newton to consist of fine atoms, too fine almost to think of, but moving at the rate of 186,000 miles in a second. According to the undulatory theory, however, light consists not of matter shot toward us, but of undulations or waves, which reach our eyes somewhat in the same way as the waves of water beat on a rocky coast.

The atoms, then, which compose a candle flame are themselves in vibration, and, communicating this vibratory movement to other particles with which they are in contact, generate waves, which travel out in all directions, like the circular waves from a stone dropped into quiet water; these waves break finally upon the surface of the retina, and cause in some unexplained way the sensation of sight—we see the candle flame. Substances which are not self-luminous cannot be seen directly or without help; to obtain vision of them it is necessary that a self-luminous body also should be present. The candle flame pours out its flood of tiny waves on the objects in the room; in the act of striking on them some of the waves are destroyed, but others rebound and reach the eye, having suffered certain changes of which we shall speak hereafter.

This rebound of the wave we call reflection; all bodies in the room reflect some of the candle light. Surfaces which are polished alter the direction of the waves of light falling on them, but they do not to any great extent scatter them irregularly, or in all directions. It hence follows that polished surfaces, when they reflect light, present appearances

totally unlike those furnished by surfaces which, though smooth, are yet destitute of polish ; the former are apt to reflect very much or very little light, according to their positions, but this is not true to the same extent with unpolished surfaces. The power which different substances have under various circumstances to reflect light is not without interest for us ; we shall see hereafter that this is a means often employed by nature in modifying colour.

As a general thing polished metallic surfaces are the best reflectors of light, and may for the most part be considered by the artist as reflecting all the light falling on them. Polished silver actually does reflect ninety-two per cent. of the light falling perpendicularly on it ; and though the percentages reflected by steel and other metals are smaller, yet the difference is not ordinarily and easily distinguished by an untrained eye.

The case is somewhat different with smooth water : if light falls on it making a small angle with its surface, the amount reflected is as large as that from a metallic surface ; while, if the light falls perpendicularly on it, less than four per cent. is reflected. Thus with a clear blue sky and smooth water we find that distant portions of its surface appear very bright, while those at the feet of the observer are of an almost unbelievable dark-blue tint. In this particular instance, the difference between the brightness of near and distant portions of the water is still further exaggerated by the circumstance that the sky overhead is less luminous than that near the horizon ; and the distant portions of the sheet of water reflect light which comes from the horizon, the nearer portions that which has its origin overhead. The reflecting power of water is constantly used by artists as a most admirable means of duplicating in a picture a chromatic composition, and easily affords an opportunity, by slight disturbances of its surface, for the introduction of variations on the original chromatic design.

It may here be remarked that in actual landscapes con-

taining surfaces of still water, it ordinarily happens that the reflected pictures are not exactly identical with those which are seen directly, and the difference may often be considerable. For example, it may easily be the case that an object beyond the water, and situated at some distance from it, is not seen in the reflected picture at all, light from it either not reaching the water, or reaching the water and not being reflected to the eye of the observer.

Polished surfaces, as we have seen, reflect light not only in large quantity, but they as it were press the light well together in rather sharply defined masses ; with unpolished surfaces the case is entirely different, the light which falls on them being scattered in all directions. Hence, wherever the eye is placed, it receives some of this light, and a change of position produces far less effect on the quantity received than is the case with light reflected from polished surfaces. Owing to their power of scattering light in all directions, rough surfaces, however situated, never send very intense light to the eye.

If a surface of white linen drapery be illuminated by a dozen different sources, it will reflect to the eye a sample of each kind of light, and what we call its hue will be made up of as many constituents. When we remember that all the different objects in a room reflect some, and usually coloured light, we see that the final tint of our piece of linen drapery depends not only on the circumstance that its natural colour is white, but also on the presence and proximity of curtains, books, chairs, and a great variety of objects ; the final colour will hence not be exactly white, but some delicate, indescribable hue, difficult of imitation except by practiced artists. With objects which are naturally coloured, or which show colour when placed in white light, the case becomes still more complicated. Let us suppose that our drapery when placed in pure white light appears red ; its hue will

still be modified by the light it receives from objects in the room : for example, if it receives some green light from objects of this colour placed in its neighbourhood, the red hue will incline toward orange ; if the added portion of light be yellow, the tendency to orange will be still more marked ; on the other hand, light received from blue or violet surfaces will cause the red to pass into crimson or even purple. The grandest illustrations of these changes we find in those cases where objects are illuminated simultaneously by the yellow rays of the sun and the blue light of the clear sky : here, by this cause alone, the natural colours of objects are modified to a wonderful extent, and effects of magical beauty produced, which by their intricacy almost defy analysis. The nature of these changes will be considered in a subsequent chapter, after the principles upon which they depend have been examined.

Finally, it may not be altogether out of place to add that the majority of paintings and chromatic designs are seen by the aid of light which they *reflect* in a diffused way to the eye of the observer ; transparencies, designs in stained or painted glass, etc., are, on the other hand, seen by light which passes entirely through their substance before reaching the eye. Corresponding to this we find that by far the larger proportion of natural objects act upon our visual organs by means of reflected light, while a few only are seen by a mixture of reflected and transmitted light. It hence follows that Nature and the painter actually employ, in the end, exactly the same means in acting on the eye of the beholder. This point, seemingly so trite, is touched upon, as an idea seems to prevail in the minds of many persons that Nature paints always with light, while the artist is limited to pigments : in point of fact, *both* paint with light, though, as we shall hereafter see, the total amount at the disposal of the painter is quite limited.

In concluding this matter of reflection, we may perhaps be allowed to add that the term reflection is quite frequently confused with shadow—the reflected image of trees on the edge of quiet water being often spoken of as the shadows of trees on the water. The two cases are of course essentially different, a genuine, well-defined shadow on water scarcely occurring except in cases of turbidity.

We have seen that all bodies reflect some of the light falling on them ; it is equally true that they transmit a certain portion. A plate of very pure glass, or a thin layer of pure water, will transmit all the light falling on it, except that which is reflected ; they transmit it unaltered in tint, and we say they are perfectly transparent and colourless substances. Here we have one of the extremes ; the other may be found in some of the metals, such as gold or silver : it is only when they are reduced to very thin leaves that they transmit any light at all. Gold leaf allows a little light to pass through its substance, and tinges it bluish-green. Almost all other bodies may be ranged between these two examples ; none can be considered absolutely transparent, none perfectly opaque. And this is true not only in a strictly philosophical sense, but also in one that has an especial bearing on our subject. The great mass of objects with which we come in daily contact allow light to penetrate a little way into their substance, and then, turning it back, reflect it outward in all directions. In this sense all bodies have a certain amount of transparency. The light which thus, as it were, just dips into their substance, has by this operation a change impressed on it ; it usually comes out more or less coloured. It hence follows that, in most cases, two masses of light reach the eye : one, which has been superficially reflected with unchanged colour ; and another, which, being reflected only after penetration, is modified in tint. Many beautiful effects of translucency are due to these and strictly analogous causes ; the play

of colour on the surfaces of waves is made up largely of these two elements ; and in a more subdued way we find them also producing the less marked translucency of foliage or of flesh.

One of the resources just mentioned the painter never employs : the light which is more or less *regularly* reflected from the outermost surface, he endeavours to prevent from reaching the eye of the beholder, except in minute quantity, his reliance being always on the light which is reflected in an irregular and diffused way, and which has for the most part penetrated, first, some little distance into his pigments.

The glass-stainer and glass-painter make use of the principle of the direct transmission of light for the display of their designs. Now, as painted or stained glass transmits enormously more light than pigments reflect in a properly lighted room, it follows that the worker on glass has at his disposal a much more extensive scale of light and shade than the painter in oils or water-colours. Owing to this fact it is possible to produce on glass, paintings which, in range of illumination, almost rival Nature. The intensity and purity of the tints which can thus be produced by direct transmission are far in advance of what can be obtained by the method of reflection, and enable the designer on glass successfully to employ combinations of colour which, robbed of their brightness and intensity by being executed in oils or fresco, would no longer be tolerable.

CHAPTER II.

PRODUCTION OF COLOUR BY DISPERSION.

IN the previous chapter we have seen that the sensation of sight is produced by the action of very minute waves on the nervous substance of the retina ; that is to say, by the aid of purely mechanical movements of a definite character. When these waves have a length of about $\frac{1}{39000}$ of an inch, they produce the sensation which we call red—we see red light ; if they are shortened to $\frac{1}{41000}$ of an inch, their action on us changes, they call up in us a different sensation—we say the light is coloured orange ; and as the lengths of the waves are continually shortened, the sensation passes into yellow, green, blue, and violet. From this it is evident that colour is something which has no existence outside and apart from ourselves ; outside of ourselves there are merely mechanical movements, and we can easily imagine beings so constructed that the waves of light would never produce in them the sensation of colour at all, but that of heat.

The colour-sensations just mentioned are not the only ones capable of being produced by the gradual diminution of the wave-length : between the red and orange we find every variety of orange-red and red-orange hue ; the orange, again, changes by a vast number of insensible steps into yellow, and so of all the other tints. Types of all colours possible, except the purples, could be produced by this method. The colours generated in this way would not only pass by the gentlest gradations into each other, forming a long series of blending hues, but they would also be

perfectly pure, and, if the light was bright, very intense. The advantage of providing, in the beginning of our colour studies, a set of tints possessing these precious qualities, is evident without much argument.

Now, white light consists of a mixture of waves possessing every desirable degree of length, and it is only necessary to select some instrument which is able to sort out for us the different kinds of light, and neatly arrange them side by side in an orderly series. Fortunately for us, we find in the glass prism a simple and inexpensive apparatus which is able to effect the desired analysis. We may, if we are willing to take a little trouble, arrange matters so as to

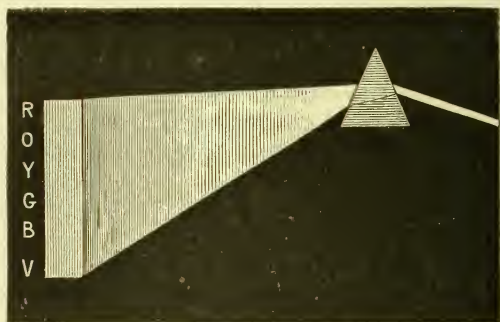


FIG. 1.—Prismatic Spectrum.

repeat the famous experiment made by Newton many years ago: viz., admit a small beam of sunlight into a darkened room, and allow it to fall on the prism, as indicated in Fig. 1. We shall notice, by observing the illuminated path of the sunbeam, that the prism bends it considerably out of its course; and, on tracing up this deflected portion, we shall find it no longer white, but changed into a long streak of pure and beautiful colours, which blend into each other by gentle gradations. If this streak of coloured light be received on a white wall, or, better, on a large sheet of white cardboard, the following changes in the colours can

be noticed: It commences at one end with a dark-crimson hue, which gradually brightens as we advance along its length, changing at the same time into scarlet; this runs into orange, the orange becomes more yellowish, and contrives to convert itself into a yellowish-green without passing noticeably into yellow, so that at first sight yellow does not seem to be present. The orange-yellow and greenish-yellow spaces are brighter than any of the others, but the rise in luminosity is so gradual that the difference is not striking, unless we compare these two colours with those at a considerable distance from them. As we pass on, the tendency to green becomes more decided, until finally a full green hue is reached. This colour is still pretty bright,

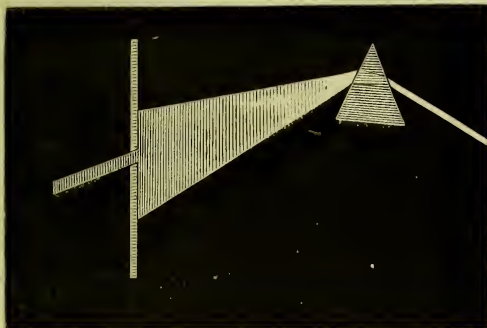


FIG. 2.—Mode of isolating a Single Colour of the Prismatic Spectrum.

and not inferior to the red in intensity; by degrees it changes into a greenish-blue, which will not at first attract the attention; next follows a full blue, not nearly so bright as the green, nor so striking; this blue changes slowly into a violet of but little brightness, which completes the series. If we wish to isolate and examine these tints separately, we can again follow the example of Newton, by making a small, narrow aperture in our cardboard, and use it then as a screen to intercept all except the desired tint, as is indicated in Fig. 2. In this manner we can examine separate

portions of our spectrum more independently, and escape from the overpowering influence of some of the more intense tints. Under these circumstances the greenish-blue becomes quite marked, and the blue is able to assert itself to a greater degree; but the yellow will not be greatly helped, for in fact it is confined to a very narrow region, and it is only by greatly magnifying the spectrum that we can obtain a satisfactory demonstration of its existence.

These experiments, though very beautiful, are quite rough; every two minutes the beam of sunlight strays away from the prism and needs again to be directed toward it; and besides that, the colours blend into each other in such a subtle, puzzling way, that, without a scale or landmark of some kind to separate them, it seems hopeless to undertake any exact experiments. In this difficulty it is to the spectroscope that we must turn for aid; it was certainly not originally contrived for such purposes as these, but nevertheless is just what we need. It is not necessary to stop to describe the instrument, as this has been done by Professor Lommel in another volume of this series; it is enough for us that it is a convenient instrument for sorting out the different kinds of light which fall on it, according to their wave-length, and that it performs this work far more accurately than a prism used according to Newton's plan. Just at this point we can take advantage of a singular discovery made by Fraunhofer, and independently to some extent by Dr. Wollaston, early in the present century. These physicists found that when the coloured band of light just described is produced by a spectroscope, or by apparatus equivalent to one, the band is really not continuous, but is cut up crosswise into a great many small spaces. The dividing lines are called the fixed lines of the solar spectrum. Almost their sole interest for us is in the fact that they serve as admirable landmarks to guide us through the vague tracts of ill-defined colour. Fig. 3 shows the positions of some of the more important fixed lines of

the spectrum. The figure is based on measurements made by the author on a flint-glass prism, with aid of a large spectroscope, or rather spectrometer, admirably constructed by Wm. Grunow, of New York. At the same time a series of observations was made on the extent of the coloured spaces in the spectrum; these are indicated in the figure, and accurately given in one of the tables that follow.* Let us suppose that the spectrum from A to H includes 1,000 parts; then the following table indicates the positions of the fixed lines:

* It will be noticed that the term *indigo*, originally introduced by Newton, has been entirely rejected in this work, and ultramarine substituted for it. Bezold suggested this change some time ago, basing his objection to indigo on its dinginess; the author, however, finds a much more fatal objection in the fact that indigo in solution, and as a pigment, is a somewhat greenish-blue, being really identical with Prussian-blue in colour, only far blacker. In the dry state this tendency to greenness is neutralized by the reddish tinge which the substance sometimes assumes: it was probably used by Newton in the dry state. A mixture of six parts of artificial ultramarine-blue, two parts white, and ninety-two parts black, when mingled according to the method of Maxwell's disks, furnishes a colour quite like that of commercial indigo in the dry state.

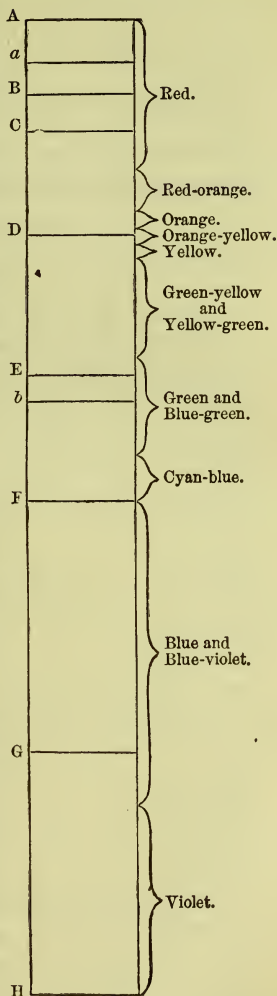


FIG. 3.—Fixed Lines and Coloured Spaces of Prismatic Spectrum.

FIXED LINES OF THE PRISMATIC SPECTRUM.

A.....	0	E.....	368·11
<i>a</i>	40·05	<i>b</i>	389·85
B.....	74·02	F.....	493·22
C.....	112·71	G.....	753·58
D.....	220·31	H.....	1000·00

The next table gives the positions of the coloured spaces in this spectrum, according to the observations of the author :

COLOURED SPACES IN THE PRISMATIC SPECTRUM.

Red begins at.....	0
Red ends, orange-red begins at.....	149
Orange-red ends, orange begins at.....	194
Orange ends, orange-yellow begins at.....	210
Orange-yellow ends, yellow begins at.....	230
Yellow ends, greenish-yellow begins at.....	240
Yellow-green ends, green begins at.....	344
Blue-green ends, cyan-blue begins at.....	447
Cyan-blue ends, blue begins at.....	495
Violet-blue ends, violet begins at.....	806
Violet ends at.....	1,000

The space out beyond 0 is occupied by a very dark red, which has a brown or chocolate colour, and outside of the violet beyond 1,000 is a faint greyish colour, which has been called lavender.

The third table shows the spaces occupied in the prismatic spectrum by the several colours :

Red.....	149
Orange-red.....	45
Orange.....	16
Orange-yellow.....	20
Yellow.....	10
Greenish-yellow and yellowish-green.....	104
Green and blue-green.....	103
Cyan-blue.....	48
Blue and blue-violet.....	311
Violet.....	194

1,000

In making these observations, matters were arranged so that only a narrow slice of the spectrum presented itself to the observer ; thus its hues could be studied in an isolated condition, and the misleading effects of contrast avoided. The figures given in the two latter tables are the mean of from fifteen to twenty observations. The hues of the spectral colours change very considerably with their luminosity ; hence for these experiments an illumination was selected such that it was only comfortably bright in the most luminous portions of the spectrum, and this arrangement retained as well as possible afterward.

The colours as seen in the spectroscope really succeed each other in the order of their wave-lengths, the red having the greatest wave-length, the violet the least. But the glass prism does this work in a way which is open to criticism ; it crowds together some portions of the series of tints more than is demanded by their difference in wave-lengths ; other portions it expands, assigning to them more room than they have a right to claim. Thus the red, orange, and yellow spaces are cramped together, while the blue and violet tracts stretch out interminably. Taking all this into consideration, it may be worth while to go one step further, and, without abandoning the use of the spectroscope, replace its prism by a diffraction grating, or plate of glass ruled with very fine, parallel, equidistant lines, such as have been made by the celebrated Nobert, and lately of still superior perfection by Rutherfurd. In Lommel's work, previously referred to, the mode in which a plate of this kind produces colour is explained ; at present it is enough to know that the general appearance of the spectacle will be unchanged ; the same series of colours, the same fixed lines, will again be recognized ; but in this new spectrum all the tints will be arranged in an equable manner with reference to wave-length. According to this new allotment of spaces, the yellow will occupy about the centre of the spectrum,

the red and different kinds of orange taking up more room than formerly ; the dimensions of the blue and violet will be greatly reduced.

Let us suppose, as before, that the spectrum from A to H includes 1,000 parts ; then the following table, which is calculated from the observations of Ångström, will indicate the positions of the principal fixed lines :

FIXED LINES IN THE NORMAL SPECTRUM.

A.	0	E.	638·92
a	113·74	b	664·79
B.	201·61	F.	749·24
C.	285·05	G	902·07
D.	468·38	H.	1000·00

The next table gives the positions of the coloured spaces in the normal spectrum, according to the observations of the author :

COLOURED SPACES IN THE NORMAL SPECTRUM.

Red begins at.....	0
Pure red ends, orange-red begins at.....	330
Orange-red ends, orange begins at.....	434
Orange ends, orange-yellow begins at.....	459
Orange-yellow ends, yellow begins at....	485
Yellow ends, greenish-yellow begins at.....	498
Yellow-green ends, full green begins at...	595
Full green ends, blue-green begins at.....	682
Blue-green ends, cyan-blue begins at.....	698
Cyan-blue ends, blue begins at.....	749
Blue ends, violet-blue begins at.....	823
Blue-violet ends, pure violet begins at.....	940

The following table exhibits the spaces occupied by the several colours in the normal spectrum :

Pure red	330
Orange-red.....	104
Orange.....	25
Orange-yellow	26

Yellow.....	13
Greenish-yellow and yellow-green.....	97
Full green.....	87
Blue-green.....	16
Cyan-blue.....	51
Blue.....	74
Violet-blue and blue-violet.....	117
Pure violet.....	60
	<hr/>
	1,000

Fig. 4 shows the normal spectrum with fixed lines and coloured spaces, corresponding to the tables just given.

If these tables are compared with those obtained by the aid of a prism of glass, it will be seen that the fixed lines and coloured spaces are arranged somewhat differently; the main cause of this difference has already been pointed out. When, however, we compare the spacing of the colours in the two spectra, it is also to be remembered that it is affected by another circumstance, viz., the distribution of the luminosity in the two spectra does not agree, and this influences, as will be shown in Chapter XII., the appearance of the colours themselves; very luminous red, for example, assuming an orange hue, very dark blue tending to appear violet, etc. The normal spectrum employed by the author

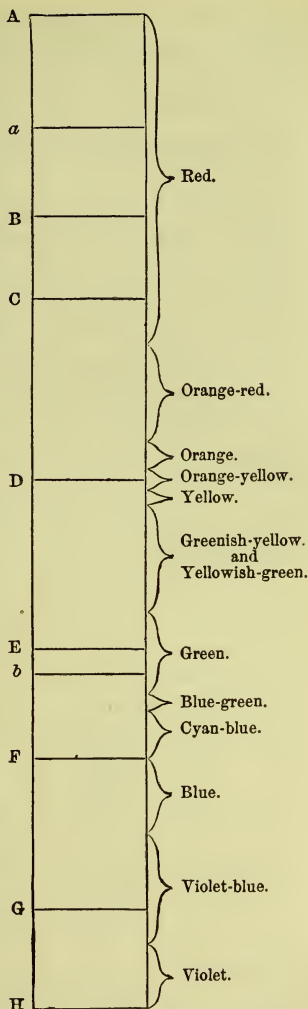


FIG. 4.—Fixed Lines and Coloured Spaces of Normal Spectrum.

was obtained by using a superb plate for which he was indebted to Mr. Rutherford. The plate contained nearly 19,000 lines to the English inch, and was silvered on the back, so that the colours were as bright as those from a glass prism. The spectrum selected for use was nearly six times as long as that furnished by the glass prism—a circumstance, of course, that favoured accurate observation.

The tables that have just been given enable us very easily to calculate the lengths of the waves of light, corresponding to the centres of the coloured spaces in the normal spectrum. It is only necessary to ascertain the number corresponding, for example, to the centre of the red space, then to multiply it by 3.653, and to subtract the product from 7,603: the result will be the wave-length corresponding to that part of the normal spectrum, expressed in ten-millionths of a millimetre. The following table contains the wave-lengths corresponding to the centres of the coloured spaces:

WAVE-LENGTH IN $\frac{1}{10,000,000}$ MM.

Centre of red	7,000
“ orange-red.....	6,208
“ orange.....	5,972
“ orange-yellow.....	5,879
“ yellow.....	5,808
“ full green.....	5,271
“ blue-green.....	5,082
“ cyan-blue.....	4,960
“ blue.....	4,732
“ violet-blue.....	4,383
“ pure violet.....	4,059

The results here given differ somewhat from those obtained by Listing in 1867; the differences are partly due to the terms employed; the author, for example, dividing up into orange-red, orange, and orange-yellow, a space which is called by Listing simply orange. According to the author

cyan-blue falls on the red side of the line F ; it is placed by Listing, however, on the violet side of this line. Other less important differences might be mentioned ; but, as a discussion of them would be out of place in a work like the present, the curious reader is referred for further information to Listing's paper.*

A little study of the normal spectrum, Fig. 4, will enable us to answer some interesting questions. We have already seen that change in colour is always accompanied by change in the length of the waves of light producing it ; hence if we begin at one end of our normal spectrum where the colour is red, and the length of the waves equal to 7,603 ten-millionths of a millimetre, as we diminish this length, we expect to see a corresponding change in the colour of the light : small changes we anticipate will produce small effects on the colour, large changes greater effects.

Now, the question arises whether equal changes of wave-length actually are accompanied by equal alterations of hue in all parts of the spectrum. To take an example : in passing from the orange-yellow, through the pure yellow and greenish-yellow well into the yellow-green region, we find it necessary to shorten our wave-length about 400 of our units ; now will an equal curtailment in other regions of the spectrum carry us through as many changes of hue ? The answer to this is not exactly what we might expect. In a great part of the red region a change of this kind produces only slight effects, the red inclining a little more or less to orange, and the same is true of the blue and violet spaces, the hue leaning only a little toward the blue or violet side, as the case may be. Hence it seems that the eye is far more sensitive to changes of wave-length in the middle regions of the spectrum than at either extremity. This circumstance, to say the least, is curious ; but, what is more to our purpose, it is a powerful argument against any theory

* Poggendorff's " Annalen," cxxxi., p. 564.

of colour which is founded on supposed analogies with music. But more of this hereafter.

In the prismatic spectrum and in our normal spectrum we found no representative of purple, or purplish tints. This sensation can not be produced by one set of waves alone, whatever their length may be ; it needs the joint action of the red and violet waves, or the red and blue. All other possible tints and hues find their type in some portion of the spectrum, and, as will be shown in the next chapter, this applies just as well to the whole range of browns and greys, as to colours like vermilion and ultramarine.

We have seen that the mixture of long and short waves which compose white light can be analyzed by a prism into its original constituents : the long waves produce on us the

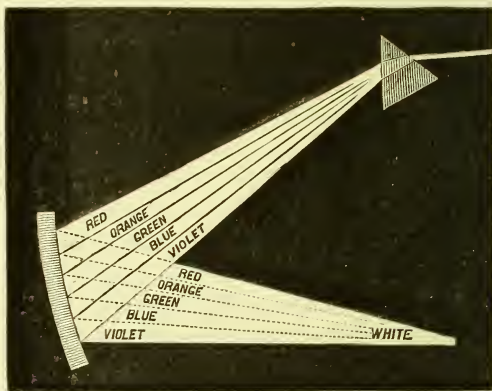


FIG. 5.—Recomposition of White Light.

sensation that we call red, and, as we allow shorter and shorter waves to act on the eye, we experience the sensations known as orange, yellow, green, blue, and violet. When, on the other hand, we combine or mix together these different kinds of light, we reproduce white light. There are a great many different ways of effecting this recom-

position ; one of the most beautiful was contrived several years ago by Professor Eli Blake. The spectrum is received on a strip of ordinary looking-glass, which is gently bent by the hands of the experimenter till it becomes somewhat curved ; it then acts like a concave mirror, and can be made to concentrate all the coloured rays on a distant sheet of paper, as shown in Fig. 5. The spot where all the coloured rays are united or mixed appears pure white.

CHAPTER III.

THE CONSTANTS OF COLOUR.

THE tints produced by Nature and art are so manifold, often so vague and indefinite, so affected by their environment, or by the illumination under which they are seen, that at first it might well appear as though nothing about them were constant; as though they had no fixed properties which could be used in reducing them to order, and in arranging in a simple but vast series the immense multitude of which they consist.

Let us examine the matter more closely. We have seen that when a single set of waves acts on the eye a colour-sensation is produced, which is perfectly well defined, and which can be indicated with precision by referring it to some portion of the spectrum. We have also found that when waves of light, having all possible lengths, act on the eye simultaneously, the sensation of white is produced. Let us suppose that by the first method a definite colour-sensation is generated, and afterward, by the second method, the sensation of white is added to it: white light is added to or mixed with coloured light. This mixture may be accomplished by throwing the solar spectrum on a large sheet of white paper, and then casting on the same sheet of paper the white light which is reflected from a silvered mirror, or from an unsilvered plate of glass. Fig. 6 shows the arrangement. By moving the mirror M, Fig. 6, the white band of light may be made to travel slowly over the whole spectrum, and thus furnish a series of mixtures of

white light with the various prismatic hues. The general effect of this proceeding will be to diminish the action of the coloured light ; the mixture will indeed present to the eye more light, but it will be paler ; the colour-element will begin to be pushed into the background. Conversely, if we now should subject our mixture of white and coloured light to analysis by a second prism, we should infallibly detect the presence of the white as well as of the coloured light ; or, if no white light were present, that would also

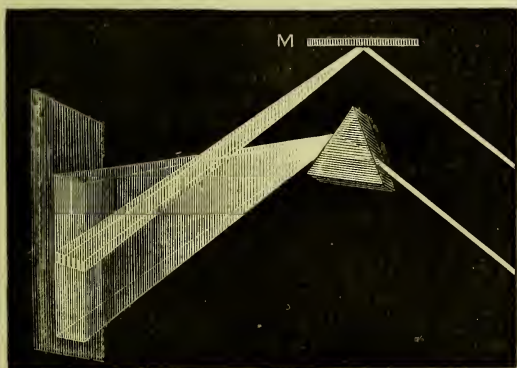


FIG. 6.—Mode of mixing White Light with the Colours of the Spectrum.

be equally apparent. Taking all this into consideration, it is evident that, when a particular colour is presented to us, we can affirm that it is perfectly pure ; viz., entirely free from white light, or that it contains mingled with it a larger or smaller proportion of this foreign element. This furnishes us with our first clue toward a classification of colours : our pure standard colours are to be those found in the spectrum ; the coloured light coming from the surfaces of natural objects, or from painted surfaces, we must compare with the hues of the spectrum. If this is done, in almost every case the presence of more or less white light will be detected ; in the great majority of instances its

preponderance over the coloured light will be found quite marked. To illustrate by an example : if white paper be painted with vermilion, and compared with the solar spectrum, it will be noticed that it corresponds in general hue with a certain portion of the red space ; but the two colours never match perfectly, that from the paper always appearing too pale. If, now, white light be added to the pure spectral tint, by reflecting a small amount of it from the mirror (Fig. 6), it will become possible to match the two colours ; and, if we know how much white light has been added, we can afterward say that the light reflected from the vermilion consists, for example, of eighty per cent. of red light from such a region of the spectrum, mixed with twenty per cent. of white light. If we make the experiment with a surface painted with "emerald green," we shall obtain about the same result, while we shall find that artificial ultramarine-blue reflects about twenty-five per cent. of white light. In all of these cases the total amount of light reflected by the coloured paper is of course taken as 100, and the results here given are to be regarded only as approximations. In every case some white light is sure to be present ; its effect is to soften the colour and reduce its action on the eye ; when the proportion of white is very large, only a faint reminiscence of the original hue remains : we say the tint is greenish-grey, bluish-grey, or reddish-grey. If one part of red light is mixed with sixteen parts of white light, the mixture appears of a pale pinkish hue. The specific effects produced by the mixture of white with coloured light will be considered in Chapter XII. ; it is enough for us at present to have obtained an idea of one of the constants of colour, viz., its purity. The same word, it may be observed, is often used by artists in an entirely different sense : they will remark of a painting that it is noticeable for the purity of its colour, meaning only that the tints in it have no tendency to look dull or dirty, but not at all implying the absence of white or grey light.

Next let us suppose that in our study of these matters we have presented to us for examination two coloured surfaces, which we find reflect in both cases eight tenths red light and two tenths white light. In spite of this, the tints may not match, one of them being much brighter than the other; containing, perhaps, twice as much red light and twice as much white light; having, in other words, twice as great brightness or luminosity. The only mode of causing the tints to match will be to expose the darker-coloured surface to a stronger light, or the brighter surface to one that is feebler. It is evident, then, that brightness or luminosity is one of the properties by which we can define colour; it is our second colour-constant. This word *luminosity* is also often used by artists in an entirely different sense, they calling colour in a painting luminous simply because it recalls to the mind the impression of light, not because it actually reflects much light to the eye. The term "bright colour" is sometimes used in a somewhat analogous sense by them, but the ideas are so totally different that there is little risk of confusion.

The determination of the second constant is practicable in some cases; it presents itself always in the shape of a difficult photometric problem. The relative brightness of the colours of the solar spectrum is one of the most interesting of these problems, as its solution would serve to give some idea of the relative brightness of the colours which, taken together, constitute white light. Quite recently a set of measurements was made in different regions of the spectrum by Vierordt, who referred the points measured to the fixed lines, as is usual in such studies.* Reducing his designations of the different regions of the spectrum to those of our spectral chart, which includes 1,000 parts from A to H (see previous chapter), and supplying the colours from the observations of the present writer, we obtain the following table:

* C. Vierordt, Poggendorff's "Annalen," Band cxxxvii., S. 200.

TABLE SHOWING THE LUMINOSITY OF DIFFERENT REGIONS OF THE PRISMATIC SPECTRUM.

Position.	Luminosity.	Colour.
From 40·5 to 57	80	Dark red.
" 104·5 " 112·71	493	Pure red.
" 112·71 " 138·5	1,100	Red.
" 158·5 " 168·5	2,773	Orange-red.
" 189 " 220·31	6,985	Orange and orange-yellow.
" 220·31 " 231·5	7,891	Orange-yellow.
" 231·5 " 363·11	3,033	Greenish-yellow, yellow-green, and green.
" 389·85 " 493·22	1,100	Blue-green and cyan-blue.
" 493·22 " 558·5	493	Blue.
" 623·5 " 689·5	90·6	Ultramarine (artificial).
" 753·58 " 825·5	35·9	Blue-violet.
" 896·5 " 956	13·1	Violet.

The author finds that with the aid of rotating disks the second constant can often be determined.* Let us suppose that we wish to determine the luminosity of paper painted with vermilion: a circular disk, about six inches in diameter, is cut from the paper and placed on a rotation apparatus, as indicated in Fig. 7. On the same axis is fastened a double disk of black and of white paper, so arranged that the proportions of the black and white can be varied at will.† When the whole is set in rapid rotation, the colour of the vermilion paper will of course not be altered, but the black and white will blend into a grey. This grey can be altered in its brightness, till it seems about as luminous as the red (Fig. 8). If we find, for example, that with the disk three quarters black and one quarter white an equality appears to be established, we conclude that the luminosity of our red surface is twenty-five per cent. of that of the white paper. This

* "American Journal of Science and Arts," February, 1878.

† See Maxwell's "Disks," chapter x.

is of course based on the assumption that the black paper reflects no light ; it actually does reflect from two to six per cent., the reflecting power of white paper being put at 100. The black disk used by the author reflected 5·2 per

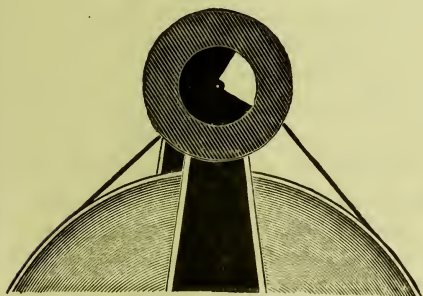


FIG. 7.—Coloured Disk, with Small Black-and-White Disk.



FIG. 8.—Coloured Disk, with Small Black-and-White Disk in Rotation.

cent. of white light ; to meet this a correction was introduced, and a series of measurements made, some of the more important of which are given in the following table :

	Luminosity.
White paper.	100
Vermilion (English)*.	25·7
Pale chrome-yellow †.	80·3
Pale emerald-green *.	48·6
Cobalt-blue †.	35·4
Ultramarine †.	7·6

These results were afterward tested by the use of a set of disks, the colours of which were complementary to those mentioned in the table, and these additional experiments and calculations showed that the original measurements differed but little from the truth. This agreement proved also the correctness of Grassmann's assumption, that the total

* In thick paste. † Washed on as a water-colour. ‡ Artificial, as a paste.

intensity of the mixture of masses of differently coloured light is equal to the sum of the intensities of the separate components.

But to resume our search for colour-constants. We may meet with two portions of coloured light having the same degree of purity and the same apparent brightness, which nevertheless appear to the eye totally different : one may excite the sensation of blue, the other that of red ; we say the *hues* are entirely different. The hue of the colour is, then, our third and last constant, or, as the physicist would say, the degree of refrangibility, or the wave-length of the light. In the preceding chapter it has been shown that the spectrum offers all possible hues, except the purples, well arranged in an orderly series, and the purples themselves can be produced with some trouble, by causing the blue or violet of the spectrum to mingle in certain proportions with the red.

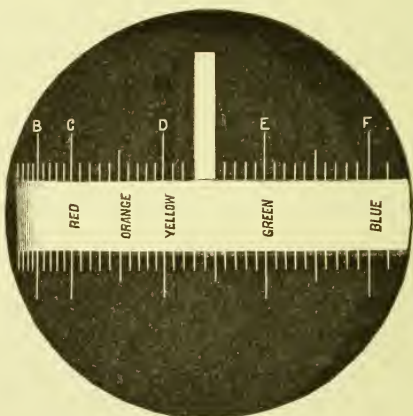


FIG. 9.—Eye-piece with Dalton's Scale.

For the determination of the hue, an ordinary one-prism spectroscope can be used ; it is only necessary to add a little contrivance which enables the observer to isolate at will any

small portion of the spectrum. This object is easily attained by introducing into the eye-piece of the instrument

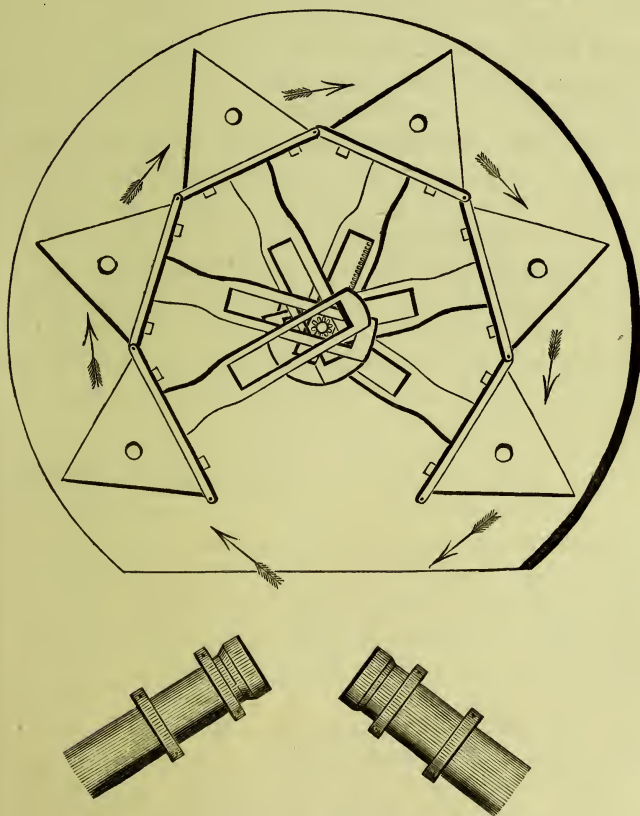


FIG. 10.—Rutherford's Automatic Spectroscope.

a diaphragm perforated by a very narrow slit (see Fig. 9). The observer then sees in the upper part of the field of view the selected spectral colour ; in the lower part of the field the scale is visible, and with its aid the precise position of the prismatic hue can be determined. Instead of using a

scale divided into equal parts, it is often advantageous to employ the plan suggested by Dr. J. C. Dalton, and used by him for determining the position of certain absorption bands. Dr. Dalton employs as a scale a minute photograph which shows the positions of the fixed lines, and divides up the spaces between them conveniently. Fig. 9 exhibits the appearance of the field of view and the scale. For more accurate work Rutherford's automatic six-prism spectroscope can be employed (see Fig. 10*). A diffraction grating can also be used—in those cases where the student of colour is so fortunate as to possess one.† With a very perfect grating of this kind, for which the author was indebted to Mr. Rutherford, the third constant was determined for a number of coloured disks. The following table gives their positions in a normal spectrum having from A to H 1,000 parts ; the corresponding wave-lengths are also given :

Name of the Colour.	Position in the Normal Spectrum.	Wave-length in $\frac{1}{1000000}$ mm.
Vermilion (English).....	387	6,290
Red lead	422	6,061
Pale chrome-yellow.....	488	5,820
Emerald-green.....	648	5,234
Prussian-blue	740	4,899
Cobalt-blue	770	4,790
Ultramarine (genuine).....	785	4,735
Ultramarine (artificial).....	857	4,472
Same, washed with Hoffmann's violet B. B.....	916	4,257

We have seen that the first colour-constant has reference to the purity of the colour, or indicates the relative amount of white light mixed with it. This constant is in all cases

* Fig. 10 is a facsimile of Rutherford's drawing of his six-prism spectroscope ("American Journal of Science and Arts," 1865).

† See Chapter iv. for an account of the grating.

difficult to determine ; probably something might be effected by carrying out practically the idea suggested in Fig. 6, by making the necessary additions to the apparatus there indicated. It would be necessary to measure the relative luminosity of the selected spectral hue and the white light, and then to mix them in proper proportions, till the mixture matched the colour of the painted paper, etc. The second and third colour-constants can be more easily determined.

It may be well here to refer to the terms used to indicate these constants. For the first constant, the word *purity*, in the sense of freedom from white light (or from the sensation of white), is well adapted. The term *luminosity* will be employed in this work to indicate the second constant ; the third constant will generally be referred to by the term *hue*. Colours are often also called intense, or saturated, when they excel both in purity and luminosity ; for it is quite evident that, however pure the coloured light may be, it still will produce very little effect on the eye if its total quantity be small ; on the other hand, it is plain that its action on the same organ will not be considerable, if it is diluted with much white light. Purity and luminosity are, then, the factors on which the intensity or saturation depends. We shall see hereafter that this is strictly true only within certain limits, and that an inordinate increase of luminosity is attended with a loss of intensity of hue or saturation.

Having defined the three constants of colour, it will be interesting to inquire into the sensitiveness of the eye in these directions. This subject has been studied by Aubert, who made an extensive set of observations with the aid of coloured disks.* It was found that the addition of one part of white light to 360 parts of coloured light produced a change which was perceptible to the eye ; smaller amounts failed to bring about this result. It was also ascertained

* Aubert, " Physiologie der Netzhaut," Breslau, 1865.

that mingling the coloured light of a disk with from 120 to 180 parts of white light (from white paper) caused it to become imperceptible, the hue being no longer distinguishable from that of the paper.* Differences in luminosity as small as $\frac{1}{120}$ to $\frac{1}{180}$ could also, under favourable circumstances, be perceived. It hence followed that irregularities in the illumination, or distribution of pigment over a surface, which were smaller than $\frac{1}{180}$ of the total amount of light reflected, could no longer be noticed by the eye. Experiments with red, orange, and blue disks were made on the sensitiveness of the eye to changes of hue or wave-length; thus, the combination of the blue disk with a minute portion of the red disk altered its hue, moving it a little toward violet; on reversing the case, or adding a little blue to the red disk, the hue of the latter moved in the direction of purple.† Similar combinations were made with the other disks. Aubert ascertained in this way that recognizable changes of hue could be produced, by the addition of quantities of coloured light, as small as from $\frac{1}{100}$ to $\frac{1}{300}$ of the total amount of light involved. From such data he calculated that in a solar spectrum at least a thousand distinguishable hues are visible. But we can still recognize these hues, when the light producing them is subjected to considerable variation in luminosity. Let us limit ourselves to 100 slight variations, which we can produce by gradually increasing the brightness of our spectrum, till it finally is five times as luminous as it originally was. This will furnish us with a hundred thousand hues, differing perceptibly from each other. If each of these hues is again varied

* To obtain correct results it is of course necessary to know the luminosity of the coloured disk as compared with the white disk, for in the above results by Aubert they are considered to be equal. With the aid of the table of luminosities previously given, this correction can be made, and it will be found that four or five times as much white light is actually necessary as is indicated above.

† Compare Chapter x.

twenty times, by the addition of different quantities of white light, it carries the number of tints we are able to distinguish up as high as two millions. In this calculation no account is taken of the whole series of purples, or of colours which are very luminous or very dark, or mixed with much white light.

To the above we may add that interesting experiments on the sensitiveness of the eye to the different spectral colours have also been made by Charles Pierce, who found that the photometric susceptibility of the eye was the same for all colours. (See "American Journal of Science and Arts," April, 1877.)

With the aid of Vierordt's measurements previously given, and the determinations by the author of the spaces occupied by the different colours in the spectrum, a very interesting point can now be settled, viz.: we can ascertain in what proportions the different colours are present in white light. The amount of red light, for example, which is present will evidently be equal to the space which it occupies in the spectrum, multiplied by its luminosity, and the same will be true of all the other colours. The author constructed a curve representing Vierordt's results, and from this, taken in combination with his own determinations of the extent of the coloured spaces, obtained the following table:

TABLE SHOWING THE AMOUNTS OF COLOURED LIGHT IN 1,000 PARTS OF WHITE SUNLIGHT.

Red.....	54
Orange-red.....	140
Orange.....	80
Orange-yellow.....	114
Yellow.....	54
Greenish-yellow.....	206
Yellowish-green.....	121
Green and blue-green.....	134
Cyan-blue.....	32

Blue.....	40
Ultramarine and blue-violet.....	20
Violet.....	5
	<hr/>
	1,000

Artists are in the habit of dividing up colours into warm and cold. Now, if we draw the dividing line so as to include among the warm colours red, orange-red, orange, orange-yellow, yellow, greenish-yellow, and yellowish-green, then in white light the total luminosity of the warm colours will be rather more than three times as great as that of the cold colours. If we exclude from the list of warm colours yellowish-green, then they will be only about twice as luminous as the cold. We shall make use of this table hereafter.

It may have seemed strange that the chrome-yellow paper previously mentioned reflected eighty per cent. of light (the reflecting power of white paper being 100), while the table just given states that white light contains only a little more than five per cent. of pure yellow light. It will, however, be shown in a future chapter that chrome-yellow really reflects not only the pure yellow rays, but also the orange-yellow and greenish-yellow, besides much of the red, orange, and green light. By mixture, all these colours finally make a yellow, as will be explained in Chapter X. The high luminosity of some of the other coloured papers is to be explained in a similar manner.

CHAPTER IV.

PRODUCTION OF COLOUR BY INTERFERENCE AND POLARIZATION.

IN Chapter II. we studied the spectral tints produced by a prism and by a grating ; these were found to be pure and brilliant as well as very numerous, and consequently were adopted as standards for comparison. Most nearly allied to these central normal colours are those which are produced by the polarization of light. In this class we meet with a far greater variety of hues than is presented by the solar spectrum ; and, instead of a simple arrangement of delicately shading bands, we encounter an immense variety of chromatic combinations, sometimes worked out with exquisite beauty, but as often arranged in a strange fantastic manner, that suggests we have entered a new world of colour, which is ruled over by laws quite different from those to which we have been accustomed. And it is indeed so ; the tints and their arrangement depend on the geometrical laws which build up the crystal out of its molecules, and on the retardation which the waves of light experience in sweeping through them, so that in the colours of polarization we see, as it were, Nature's mathematical laws laying aside for a moment their stiff awkwardness, and gayly manifesting themselves in play.

The apparatus necessary for the study of these fascinating and often audacious colour-combinations is not necessarily complicated or very expensive. A simple form

of polariscope is shown in Fig. 11. It consists merely of a plate of window-glass at P, which is so placed that the angle, a , is 33° as nearly as possible; at N is a Nicol's prism, and at L a plano-convex lens with a focal length of about an inch. The distance of the prism from the plate

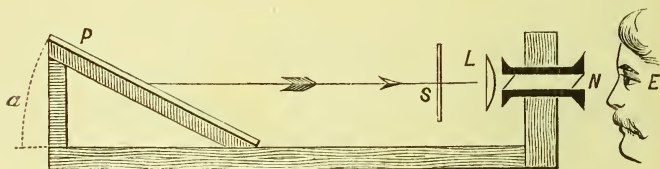


FIG. 11.—Simple Polarizing Apparatus.

of glass is ten inches; the lens is removable at pleasure, the Nicol's prism is capable of revolving around its longer axis. If, now, light from a white cloud be reflected from the plate of glass toward the Nicol's prism, as indicated by the arrow, some of it will ordinarily traverse the prism and reach the eye at E; the prism should now be turned till this light is cut off, and the instrument is then ready for use. Thin slips of selenite or crystals of tartaric acid placed at S, so that they are magnified, display the colours of polarization very beautifully. The arrangement just described constitutes a simple polarizing microscope; if a compound polarizing microscope can be obtained, it will be still more easy to study the colours and combination of colours presented by the crystals of many different salts. By dissolving a grain or two of the substance in a drop of water, and allowing it to crystallize out on a slip of glass, it is possible very easily to make objects suitable for examination.

Thin plates of selenite, obtained by removing successive layers with a penknife, answer admirably if we wish to study the phenomena of chromatic polarization in their simplest forms. It will often be found that nearly the

whole plate presents a single unshaded hue, which bears a close resemblance to a patch of colour taken from some portion of the spectrum. But, however bright the colour may be, it is never free from an admixture of white light, and it is the constant presence of this foreign element which causes the colours of polarization to appear a little less intense than those of the spectrum. With plates which are somewhat thicker the proportion of white light increases, washing out the colour, till only a faint reminiscence of it is left. The more powerful tints, however, quite equal and probably surpass in purity—that is, in freedom from white light—the most intense sunset hues. Among these colours we find many shades of red and purple-red; all the red-orange hues are represented, and the same is true of the other colours found in the spectrum. Besides, there is a range of purples which bridges over the chasm between the violets and reds; faint rose-tints are also present in abundance, and the same is true of the pale greens and bluish-greens. In addition to this, quite thin slips furnish a distinct set of tints which are peculiar in appearance, and which, when once seen, are never forgotten; a singular tawny yellow will be noticed in combination with a bluish-grey; the yellow, such as it is, shading into an orange nearly allied to it, and this again into a brick-red; black and white will be associated with these subdued tints; the general impression produced by these combinations being sombre if not dreary.

These slips of selenite furnish neither beautiful nor complicated patterns, the tints being for the most part arranged in parallel bands, with here and there angular patches, often in sharp contrast with the other masses of colour. There is no noticeable attempt at chromatic composition, except perhaps a little along fractured edges, where we frequently meet with pale grey or white deepening into a fox-coloured yellow, followed by a red-violet, brightening into a sea-green dashed with pure ultramarine, or changing suddenly

into a full orange-yellow, after which may follow a broad field of purple. Just as often all the tints are pale, like those used on maps, with a narrow fringe on the edge, of rich variegated hues. The colour-combinations seldom rise into great beauty, though they often astonish and dazzle by their audacity and total disregard of all known laws of chromatic composition. The brilliancy and purity of these tints are so great, and they are laid on with such an unfaltering hand, that all these wild freaks are performed comparatively with impunity, and it is only when we proceed to make copies of these strange designs that we become fully aware of their peculiarities, and, from an artistic point of view, positive defects.

Crystals of tartaric acid present phenomena which are quite different: here the patterns are rich and often beautiful; the colour is full of gradation, touched on and retouched and wrought out with patience in delicate, complicated forms, which echo or faintly oppose the grand ruling ideas of the composition. We may have a wonderfully shaped mass radiating in curved lines over the entire field, tinted with soft grey and pale yellow, with here and there dashes of colour like the spots on a peacock's tail, glowing like coals of fire; all this being set off by very dark shades of olive-green, dark browns and greys. If the crystals are thin this is their appearance; but as the thickness increases so does the brilliancy of the hues, which are sure to be well contrasted with large masses of deep shade. The soft gradations, the sharp contrasts, the brilliant and pale colours, the dark shadows and the wonderful forms, all combine to lend to these pictures a peculiar charm which is not wholly lost even in copies executed in ordinary pigments.

Common sugar, if allowed time to crystallize out slowly, furnishes appearances somewhat resembling the above, but the designs are more formal and less interesting. Crystals of nitrate of potash present appearances, again, which are totally unlike those above mentioned; here we have a great

number of delicately tinted threads of light ; there will be purples and golden greens or dull olive-greens and carmines, woven together so closely as almost to produce a neutral tint, which will brighten suddenly and display combinations of purple-red with green, dashed here and there with pure ultramarine. These tinted threads of light will be disposed with regularity as though it had been intended to weave them into some wonderful cashmere-like pattern, and then warp and woof had been suddenly abandoned and forgotten.

It would be useless to multiply these descriptions—every salt has its own peculiarities and suggests its own train of fancies ; some glow like coloured gems with polished facets, or bristle with golden spears like the advancing ranks of two hosts in conflict, or suggest a rich vegetation made of gold and jewels and bathed in sunset hues. Artists who see these exhibitions for the first time are generally very much impressed by their strange beauty, and not unfrequently insist that their range of colour-conceptions has been enlarged. It has often seemed to the author that the cautious occasional study of some of these combinations might be useful to the decorator in suggesting new conceptions of the possibilities within his reach.

When polarized light is made to traverse crystals in the direction of their optic axes, phenomena of a different kind are presented. They were discovered in 1813 by Brewster, and, on account of their scientific interest and a certain beauty, have since then greatly attracted the attention of physicists and even of mathematicians. A series of rainbow-like hues, disposed in concentric circles, is seen on a white field ; a dark-grey cross is drawn across the gayly coloured circles, and, after dividing them in four quadrants, fades out in the surrounding white field. By a slight change in the adjustment of the apparatus, the grey cross can be made white ; the rings then assume the complementary tints. Other crystals, again, furnish double sets of rings, the dark

cross being shared by them jointly, or so altered in form as no longer to be recognizable.

These appearances have been considered by many physicists to be extraordinarily beautiful ; it is, however, to be suspected that in this case the judgment was swayed by other considerations than those of mere beauty. The rarity of the phenomenon, the difficulty of exhibiting it, the brilliant list of names identified with it, along with the insight it furnishes as to the molecular constitution of crystals, all combine to warp the judgment, and to seriously influence its final award. In point of fact, the formal nature of the figures, the constant repetition of the rainbow-tints in the same set order, which is that of the spectrum, both exclude the possibility of the charming colour-combinations so frequently presented by many salts when simply crystallized on a slip of glass. The cross and rings are not for a moment, in matter of beauty, to be compared with the appearances presented by crystals of tartaric acid.

Glass which has been heated and then suddenly cooled, or glass which is under strain, exhibits phenomena of colour closely related to the above ; we have as it were a set of distorted crosses and rings which sometimes lend themselves more kindly to the production of chromatic effects than is the case with the normal figures.

In ordinary life the colours of polarization are never seen ; the fairy world where they reign cannot be entered without other aid than the unassisted eye. This is not a matter for regret ; the purity of the hues and the audacious character of their combinations cause their gayety to appear strange and unnatural to eyes accustomed to the far more sombre hues appropriate to a world in which labour and trouble are such important and ever-present elements. The colours even of flowers have a thoughtful cast, when compared with those of polarization.

The colours which have just been considered are produced in a peculiar manner ; the complete explanation is

long and tedious, and has for us no particular interest. The main idea, however, is this : white light is acted on in such a way that one of its constituents is suppressed ; the result is coloured light. For example, if we strike out from white light the yellow rays, what remains will produce on us the sensation of blue ; if we cut off the green rays, the remainder will appear purple. The reason of this will be more fully appreciated after a study of the facts presented in Chapters XI. and XII. To effect this sifting out of certain rays a polarizing apparatus is employed ; when the crystals are removed from it, the colour instantly vanishes. Now, it so happens that there is a class of natural objects capable of displaying exactly the same hues without the intervention of any piece of apparatus—all objects that fulfill a certain condition may be reckoned in this class ; it is merely that their thickness should be very small. Thin layers of water, air, glass, of metallic oxides, of organic substances, in fact of almost everything, display these colours. The most familiar example is furnished by a soap-bubble. When it first begins to grow, it is destitute of colour and perfectly transparent ; it gives by reflection from its spherical surface a distorted image of the window, with the bars all curved, but no unusual hues are noticed till it has become somewhat enlarged.* Then faint greens and rose-tints begin to make their appearance, mingling uneasily together as if subjected to a constant stirring process. As the bubble expands and the film becomes more attenuated, the colours gain in brilliancy, and a set of magnificent blue and orange hues, purples, yellows and superb greens replaces the pale colours which marked the early stages, and by their changing flow and perpetual play fascinate the beholder. If the bubble

* It is not very uncommon to meet with paintings in which a bubble has been represented with window-bars on its surface, where nothing of the kind could have been visible. A friend has mentioned to the author four cases where different artists have introduced window-bars instead of sky and landscape, on the surfaces of bubbles which were in the open air.

has the rare fortune to live to a good old age, at its upper portion a different series of tints begins to be developed ; the tawny yellow, before mentioned, begins to be seen in irregular patches, floating around among the more brilliant hues, a sign that the attenuation has nearly reached its extreme limit ; but, if by some unusual chance it should be a Methuselah among bubbles, pale white and grey tints also are seen, after which it is sure to burst. A long-lived soap-bubble displays every colour which can be produced by polarization. The thin film has a sifting action on white light, which in its final result is the same as in the case of the production of colour by polarized light : certain rays are struck out, and, as before, white light deprived of one of its constituents furnishes coloured light. This elimination is accomplished by the interference of the waves of light involved ; hence, colours produced in this way are called “interference colours.” The colours of polarization are also just as truly interference colours, but they are not usually known under this name. From all this it follows that the colours produced by thin layers, or by very fine particles, always contain some white light, and consequently cannot quite rival in purity or intensity the spectral hues.

The colours of polarization, as we have seen, are never met with outside of the laboratory. Nature, on the other hand, here and there with a sparing hand, displays in small quantity, and as a rarity, the colours of interference. They are used as a wonderful kind of jewelry in the adornment of many birds ; lavishly so in the case of the common peacock, where the breast and tail feathers in full sunshine display flashing, dazzling hues, which make our artificial ornaments appear pale and tame. In contemplating these astonishing hues, or those of that tiny winged jewel, the humming-bird, we are struck by the circumstance that they actually have a metallic brilliancy, which we in vain attempt to rival with our brightest pigments. To compete with them successfully, it is necessary to substitute a sur-

face of silver for the white paper, and to cover it with the purest and most transparent glazes. This appearance of metallic lustre depends on the circumstance that much coloured light is reflected, mingled with only a small quantity of white light, the great bulk of the latter being absorbed by the dark pigment contained in the interior of the feathers. When this dark pigment is absent, we have as before colour ; but, being mingled with much reflected white light, it presents simply an appearance like that of mother-of-pearl.

There is yet another peculiarity of the colours now under consideration, which still more completely separates them from the hues furnished by pigments : it is their variability. These colours, as has been mentioned, are produced by the interference of the waves of light which are reflected from the thin films : the nature of this interference depends partly on the angle at which this reflection takes place, so that, as we turn a peacock's feather in the hand, its colour constantly changes. The same is true of the tints of the soap-bubble, and of interference colours in general—the hue changes with the position of the eye ; as they are viewed more and more obliquely, the tint changes in the order of the spectrum, viz., from red to orange, to yellow, etc.

The brilliant metallic colours exhibited by many insects, particularly the beetles, belong also in this class, so also the more subdued steel-blues and bottle-greens displayed by many species of flies. So commonly does this occur that it suggests the idea that these humble creatures are not destitute of a sense for colour capable of gratification by brilliant hues. If we descend into the watery regions we find their inhabitants richly decorated with colours of the same general origin, the pearly rainbow hues which they display all depending on the interference of light. The same is true of the iridescent hues which so commonly adorn shells externally and internally. In this case candour compels one

to admit that the colours, beautiful as they are, can hardly be a source of pleasure to the occupants or to their friends.

Leaving the animated world, we find the colours of interference shown frequently, but in an inconspicuous manner, by rather old window-glass ; some of the alkali seems to be removed by the rain, and in the course of time a thin film of silica capable of generating these hues is formed. In antique glass which has long remained buried this process is carried much further, so that sometimes the whole plate or vase tends to split up into flakes. Here, owing to successive reflections on many layers, the light which reaches the eye is quite bright, and the colours intense. Crimson, azure, and gold are found in combination ; blue melts into purple or flashes into red ; ruby tints contrast with emerald hues : each change of the position of the eye or of the direction of the light gives rise to a new and startling effect. In other cases broad fields of colour, with much gentle gradation and mingling of tender pearly hues, replace the gorgeous prismatic tints, and fascinate the beholder with their soft brilliancy.

The iridescent hues of many minerals fall into the same general class ; they are beautifully displayed by some of the feldspars, and the brilliant hues found on anthracite coal have also the same origin. The blue films often purposely produced on steel are due to thin layers of oxide of iron which suppress the yellow rays. Other cases might be mentioned, but these will suffice for the present.

CHAPTER V.

ON THE COLOURS OF OPALESCENT MEDIA.

IF white light be allowed to fall on water which is contained in a clear, colourless glass vessel, some of it will be reflected from the surface of the liquid, while another portion will traverse the water and finally again reach the air. These well-known facts are represented in Fig. 12. An eye placed at *E* will perceive the reflected light to be white, and the transmitted light will also appear white to an eye situated at *O*. But, if now a little milk be added to the water, a remarkable change will be produced: light will, as before, be reflected from the surface to the eye placed at *E*, and this surface-light will still be white; but the little milk-globules under the surface and throughout the liquid will also reflect light to *E*—this light will be bluish. From this experiment, then, it appears that the minute globules suspended in the liquid have the power of reflecting light of a bluish tint. In Fig. 12 the light is represented as being reflected only in one direction; but, when the milk-globules are added, they scatter reflected light in many directions, so that an eye placed anywhere above the liquid perceives this bluish appearance.

On the other hand, after the addition of the milk, the light at *O* (Fig. 12), which has passed through the milky liquid, will be found to have acquired a yellowish tint. From this it appears that fine particles suspended in a liquid have the power of dividing white light into two portions, tinted respectively yellowish and bluish. If more milk be

added to the water, white light will mingle in and will finally overpower the bluish reflected light, so that it will hardly be noticed ; as the quantity of milk is increased, the colour of the transmitted light will pass from yellow to orange, to red, and finally disappear, the liquid having become at last so opaque as to cease to transmit light altogether.

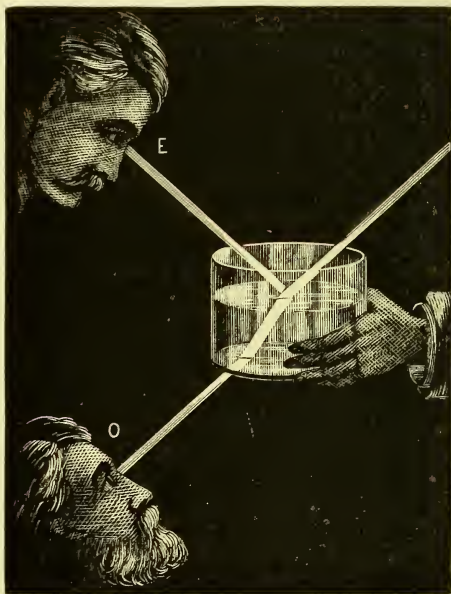


FIG. 12.—Reflection and Transmission of Light by Water.

This very curious action is not confined to mixtures of milk and water, but is exhibited whenever very fine particles are suspended in a medium different from themselves. If an alcoholic solution of a resin is poured with constant stirring into water, very fine particles of resin are left suspended in the liquid, and give rise to the appearances just described. Brücke dissolves one part of mastic in eighty-seven parts of alcohol, and then mixes with water, the water

being kept in constant agitation. A liquid prepared in this way shows by reflected light a soft sky-like hue, the colour of the light which has passed through being either yellow or red, according to the thickness of the layer traversed. The suspended particles of resin are very fine, and remain mingled with the water for months; they are often so fine as to escape detection by the most powerful microscopes.

Some kinds of glass which are used for ornamental purposes possess the same property, appearing bluish-white by reflected light, but tingeing the light which comes through them red or orange-red. The beautiful tints of the opal probably have the same origin, and the same is true also of the bluish, milky colour which characterizes many other varieties of quartz.

Not only liquids and solids exhibit this phenomenon of opalescence, but we find it also sometimes displayed elsewhere; thus, for example, a thin column of smoke from burning wood reflects quite a proportion of blue light, while the sunlight which traverses it is tinted of a brownish-yellow, or it may be, even red, if the smoke is pretty dense.

All these phenomena are probably due to an interference of light, which is brought about by the presence of the fine particles, the shorter waves being reflected more copiously than those which are longer; these last, on the other hand, being more abundantly transmitted. An elaborate explanation of the mode in which the interference takes place would be foreign to the purpose of the present work; we therefore pass on to the consideration of the more practical aspects of this matter.*

It will be well to notice, in the first place, certain conditions which favour not so much the formation as the perception of the tints in question: thus it will be found that

* Compare E. Brücke, in Poggendorff's "Annalen," Bd. 88, S. 363; also Bezold's "Farbenlehre," p. 89.

the blue tint, in the experiments with the liquids, is best exhibited by placing the containing glass vessel on a black surface. This effectually prevents the blue reflected light from being mingled with rays which have been directly transmitted from underneath. Indeed, the mere presence or absence of a dark background may cause the tint which

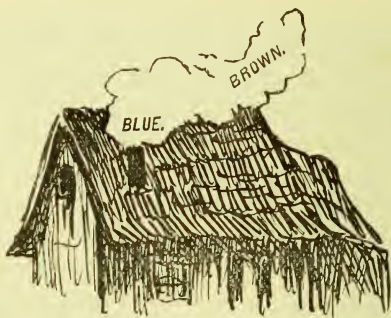


FIG. 13.—Smoke appears Blue on a Dark Background ; Brown on a Light Background.

finally is perceived by the eye to change from yellow to blue, the other conditions all remaining unaltered. Thus in Fig. 13 we have thin smoke seen partly against a dark background, and partly against a sky covered with white clouds: the lower portion is blue, from reflected light, while in the upper portion this tint is overpowered by the greater intensity of the transmitted light, which is yellowish-brown. As a general thing, the reflected and transmitted beams are both present ; dark backgrounds favour the former, luminous ones the latter.

If a thin coating of white paint, such as white lead or zinc-white, is spread over a black or dark ground, the touches so laid on will have a decidedly bluish tint, owing to the causes which have just been considered. If a drawing on dark paper be retouched with zinc-white used as a water-colour, the touches will appear bluish and inharmonious, unless especial care is taken to prevent the white

pigment from being to some extent translucent ; this disagreeable appearance can only be prevented by making each touch dense and quite opaque. For the production of such effects it is not even necessary to go through the formality of laying the white pigment on a dark ground ; white lead mingled with any of the ordinary black pigments gives not a pure but a bluish grey. This is very marked in the case of black prepared from cork, which hence has sometimes been called "beggars' ultramarine." If yellow pigments are mixed with black, the effect is not simply to darken the yellow, as would be expected, but it is converted into an olive-green. This is particularly the case with those pigments which approximate to pure yellow in hue, such as gamboge and aureolin ; the least admixture of dark pigment carries them over toward green. But if these black-and-white or black-and-yellow pigments are combined by the method of rotating disks (see Chapter X.), we obtain pure greys or darker yellow tints, showing that the blue hue is not, as many suppose, inherent in the black pigment, but an accident due to the mode of its employment. The above-mentioned cases are marked examples of the application of these principles to painting ; but in a more subtle way the whole theory of the process of oil-painting takes cognizance of them, and is so adjusted as to avoid difficulties thus introduced, or, more rarely, to utilize them. It is perhaps scarcely necessary to add that the somewhat bluish tone of drawings made with body colour, or of frescoes, is due to these same causes.

Having hinted at the influence which this peculiar optical action exerts on the infancy of a picture, we pass on to consider some of its effects on a painting in its old age. It is well known that old oil-paintings frequently become more or less covered by what seems to be a coating of grey or bluish-grey mould, which, spreading itself particularly over the darker portions, obscures them, so that all details are lost, and the work of the artist entirely destroyed. In-

vestigation has shown that this trouble is caused by an immense number of fine cracks in the painting itself, which seem to act somewhat in the same way as the mixtures which have just been considered, so that the observer is practically looking at the picture through a rather dense haze. By filling these invisible cracks up with varnish the matter is somewhat helped, but much more perfectly by the "regenerations process" of Pettenkofer. This celebrated chemist once by accident used an old, worn-out oil-cloth mat, from which the pattern had mostly disappeared, to cover a beaker containing hot alcohol. On removing the mat, some hours afterward, he was surprised to find that the portion acted on by the alcoholic vapours had been rejuvenated and the pattern restored. It was soon ascertained that the vapours had softened the pigment, and the separated grains had again been fused together. Experiments on old oil-paintings gave similar results, and the process is now in use in some of the largest European galleries.

In many other objects besides those that have been mentioned these peculiar tints can be observed; among minor examples may be mentioned the bluish-grey or greenish-grey tint which marks the course of veins under the skin; the blue or greenish colour of the human eye also owes its tint to the same cause. In these cases an opalescent membrane is spread over a dark background, and the colour is produced in the same manner as in the experiments described at the commencement of this chapter. In blue eyes there is no real blue colouring-matter at all.

It is, however, the sky that exhibits this class of tints on the grandest scale, as well as in the greatest perfection. Our atmosphere, even when perfectly clear, contains suspended in it immense numbers of very fine particles which never settle to the earth, and which the rain has no power to wash down. When they are illuminated by sunlight they reflect white light mixed with a certain proportion of blue, and this blue is seen on a black background, which is

nothing less than the empty space in which the earth is hung. Hence, the blue colour of the sky. This tint on clear days can be traced up tolerably near the sun, indeed, until the brightness of the sky begins to be blinding. An examination of the deepest blue portions of the sky with the spectroscope reveals the presence of much white light, so that the blue colour is very far from being pure or saturated—a fact that young landscape-painters soon have forced on their attention. In clear weather, as long as the sun is at a considerable distance from the horizon, the yellow colour which accompanies the transmission of light through an opalescent medium is not much noticed; but, as the sun sinks lower, its rays traverse an always increasing thickness of the atmosphere, and encounter a greater number of fine particles, so that the transmitted light, late in the afternoon, becomes decidedly yellow or rather orange-yellow.

Having thus briefly considered the production of ordinary sky-tints, let us pass to the aspects assumed by a landscape under the influence of the minute suspended particles. These atoms will of course reflect light toward the observer, and this light will add itself to that which comes regularly from objects in the landscape, producing thus important changes in their appearance. The very thick layer of air intervening between the observer and the most distant mountains will send to the eye a very large amount of whitish-blue light, which will not greatly differ from a sky-tint. This will entirely overpower the somewhat feeble light reflected from portions of the mountain in shade, so that as a result we shall have all the shadows of the mountain represented by more or less pure sky-tints, and these tints will be far more luminous, far brighter, than the original shadows were. No details will be visible in these wonderfully shaped bluish patches. Those portions of the mountains, on the other hand, which are in full sunlight will still visibly send light to the eye through the haze, and

their prevailing tint will be yellowish or orange, or some other warm tone. Not many details will be visible, and the actual colours or local colours of the mountain will not at all appear, or at most will only blend themselves with the soft, warm tints due to the medium. In a word, the contrast between the light and shade will be enormously diminished, so that the general luminosity of the mountain will be hardly less than that of the sky itself, and its colour will be worked out mainly in tints which have the same origin and character with those of the sky. As we approach nearer the mountain, these effects begin slowly to diminish, and in the sunlit portions delicate greens, varied and soft greys, begin to make their appearance, while the shadows lose their heavenly blue, and, darkening, become bluish-grey. Afterward all those parts lying in sunlight display their local tints, somewhat softened, and the coloured light from the shadows begins to make itself felt, and, mingling with the blue reflected light, to produce soft purplish-greys, greenish-greys, and other nameless tints. The sunlit portions of the pine-trees will be of an olive-green or of a low greenish-yellow, the shadows on the same trees being pure grey or bluish-grey without any suggestion of green. On nearer objects these effects are less traceable, and the natural relation between light and shade more and more preserved, so that contrast of this last kind becomes progressively stronger as we turn from the most distant to the nearest objects. All these effects are readily traceable on any ordinary clear day ; they change, of course, with the condition of the atmosphere, and as it becomes misty the blue reflected light changes to grey, the transmitted light not being equally affected.

Late in the afternoon, when the sun is low, its rays traverse very thick layers of the atmosphere, and wonderful chromatic effects are produced. Near the sun the transmitted light is yellowish, but so bright that the colour is not very perceptible ; to the right and left the colour deepens

into an orange, often into a red, which, as the distance from the sun increases, fades out into a purplish-grey, greyish-blue, passing finally into a sky-blue. The warm tints are produced mainly by transmitted light, the cold ones by reflected light, and the neutral hues by a combination of both. Above the sun there is, in clear sunsets, a rather regular transition upward, from the colours due to transmitted, to those produced by reflected light. As the sun sinks lower its rays encounter a greater mass of suspended particles, and the warm tints above mentioned move toward the red end of the spectrum, and also gain in intensity. The presence of clouds breaks up the symmetry of these natural chromatic compositions, and gives rise to the most magnificent effects of colour with which we are acquainted. The landscape itself sympathizes with the sky, and near the sun, chameleon-like, assumes an orange or even red hue ; while at greater distances its cold tints are warmed, even the greens being changed into olive or yellowish hues. Simultaneously the shadows lengthen enormously, bringing thus the composition into grand and imposing masses, and investing even the most commonplace scenery with an air of great nobleness and beauty.

The complete series of sunset hues, from the brightest light to the deepest shade, runs as follows :

1. Yellow.		3. Red.		5. Violet-blue.
2. Orange.		4. Purple.		6. Grey-blue.

This, as it were, normal series is often interrupted by the omission of one or more of the intermediate hues, and sometimes begins as low as the red or even purple.

CHAPTER VI.

PRODUCTION OF COLOUR BY FLUORESCENCE AND PHOSPHORESCENCE.

IN all the cases thus far examined, colour has been produced either by the analysis of white light or by subjecting it to a process of subtraction, as in the examples mentioned in the last chapter. The very astonishing discovery of Stokes, however, has proved that colour can be produced in a new and entirely different way. If, in a darkened room the pure violet light of the spectrum be allowed to fall on a plate or wineglass made of uranium glass, these articles will not reflect violet light to the eye as would be expected, but will glow with a bright-green light, looking in the darkness almost as though they had suddenly become self-luminous. This kind of glass has, then, the extraordinary property of entirely altering the colour of the light that falls on it, and of causing the light to assume a quite different hue. But, as colour depends on wave-length, we are led to ask whether *this* property of the original beam of light is also affected by the uranium glass. Stokes proved conclusively that this is the case, and that in all such experiments the length of the wave is made greater. It would appear that the waves of light act on the atoms which make up (or surround) the molecules of the glass, and set them in vibration; they continue in vibration for some little time afterward, *at a rate of their own selection*, which is always less than that of the waves of light which gave the first impulse. Being in vibration, they act as luminous centres, and com-

municate vibrations to the external ether, and this is the green light that finally reaches the eye. The action takes place not only on the surface of the glass, but deep in its interior, so that, if the experiment be made with a thick cube of the glass, it actually appears milky and almost opaque, owing to the abundant flood of soft green light which it pours out in all directions. It is not even necessary to employ as a source of illumination the pure violet of the spectrum ; sunlight streaming through blue cobalt glass answers as well, and the sharp change from the violet-blue to the milky-green is quite as astonishing.

Under ordinary daylight uranium glass scatters in all directions a bluish-green light, which is due to the cause above mentioned, but the light which passes through its substance is merely tinged yellow. Both these tints make their appearance in daylight, and by their combination communicate to articles made of this glass a peculiar and rather beautiful appearance. Candle-light or gas-light furnishes but a scanty supply of blue and violet rays, hence this kind of illumination robs uranium glass entirely of its charm, and the articles made of it assume a dull yellowish hue which is neither striking nor attractive. There are many salts which have this property in a high degree : among the best known is the platino-cyanide of barium, which presents appearances similar to those above mentioned. Thallene, an organic substance derived from coal-tar, and described by Morton, must also be classed with uranium glass.* Drawings made with this substance on white paper, by daylight appear yellowish, but when placed under a violet or blue illumination flash into sudden brilliancy, and scatter in all directions a strong greenish light. There are many liquids which have the same property, and which display different colours when acted on by violet light, but for an account of them we must refer the curi-

* See "Chemical News," December, 1872.

ous reader to Dr. Pisko's work on the fluorescence of light.*

Before passing from this subject it may be as well to add that phosphorescence also often gives rise to colours which more or less closely resemble those of fluorescence. If tubes filled with the sulphides of barium, strontium, calcium, etc., be placed in a dark room and illuminated for an instant by a beam of sunlight, by the electric light, or by burning magnesium wire, they will display a charming set of tints for some minutes afterward. Some will shine with a soft violet light, others will display an orange or yellow glow; delicate blues will make their appearance, and will contrast well with the red hues, the latter resembling in the darkness living coals of fire. The tints, as such, are very beautiful and suggestive, though of course no direct application can be made of them to artistic purposes.

* "Die Fluorescenz des Lichtes," F. J. Pisko, Vienna.

CHAPTER VII.

ON THE PRODUCTION OF COLOUR BY ABSORPTION.

THE colours produced by the dispersion, interference, and polarization of light have great interest from a purely scientific point of view, and are also valuable in helping us to frame a true theory of colour, but it is to the phenomena of absorption that the colours of *ordinary* objects are almost entirely due. The pigments used by painters, the dyes employed by manufacturers, the colouring-matter of flowers, trees, rocks, and water, all belong here. Let us begin our study of this subject with a fragment of stained glass. When we place the glass flat on a surface of black cloth, and expose it to ordinary daylight, we find that it reflects light to the eye just as a piece of ordinary window-glass would under similar circumstances, and this light is white, not coloured. In this experiment, the rays of light which reach the eye have been reflected from the mere surface of the plate of glass, those rays which penetrate its interior being finally absorbed by the black cloth underneath, and never reaching the eye at all. If we now raise the glass and allow the light of the sky to pass through it and fall on the eye, we find that it has been coloured ruby-red. The light of a candle- or gas-flame is affected in the same way, and a beam of sunlight streaming through the plate of glass falls on the opposite wall as an intensely red, luminous spot. Our first and very natural impression is, that the stained glass has the power of altering the quality of light—that the white light is in some way actually transmuted

into red light. This seems to be the universal impression among those who have not particularly examined the matter. We saw, in Chapter II., that with a prism we could analyze white light, and sort out the waves composing it according to their length, and that the sensation which the waves produced on the eye varied with their length, the longest giving red, the shortest violet. The prism can also be applied to the study of the matter now under consideration. A



FIG. 14.—Red Glass placed over Slit in Black Cardboard.

screen of black pasteboard is to be prepared with a narrow slit cut in its centre ; over the slit a piece of stained glass is to be fastened, as indicated in Fig. 14. If, now, this arrangement be placed in front of a window, matters can be so contrived that white light from a cloud shall fall upon the slit and traverse the stained glass ; it will afterward reach



FIG. 15.—Spectrum of Light transmitted through Red Glass.

the prism which will analyze it. On making this experiment we find that the result is similar to what is indicated in Fig. 15 : the prism informs us that the transmitted beam

consists mainly of red light ; a little orange light is also present. The experiment can, however, be made in a more instructive way, by covering only half of the slit with the plate of glass. On repeating it with this modification, we obtain side by side an analysis of the white light direct from the cloud, and of the light which has traversed the ruby glass ; the result is indicated in Fig. 16, and we see



FIG. 16.—Spectrum of White and Red Light compared.

at a glance that the solution of the whole matter is simply this : the ruby glass is able to transmit the red rays, but it stops all the others ; these last it absorbs—hence we say it produces its colour by absorption. The other rays are in fact converted into heat, and raise the temperature of the glass to a trifling extent. The experiment can be varied somewhat without affecting the result ; if a solar spectrum be projected on a screen, as described in Chapter II., we shall find, when we look at it through the ruby glass, that we can see only the red space, light from the other coloured spaces not being able to penetrate the glass ; and finally, when we hold our plate of glass directly in the paths of the coloured rays, we shall notice that it stops all except those that are red. These simple fundamental experiments prove that the ruby glass does not transmute white light into red, but that it arrests certain rays, and converts them into a kind of force which has no effect on the eye ; the rays which are not arrested finally reach the eye and produce the sensation of colour.

For more careful examinations of the coloured light transmitted by stained glass a spectroscope with one flint-glass prism can advantageously be used. The stained glass is to be fastened so that it covers one half of the slit, and then we shall have, placed side by side, the spectrum due to the glass and a prismatic one for comparison. In this latter the fixed lines will be present, and we can use them as a kind of natural micrometer for mapping down our results. There is, however, another point to be attended to. When we come to examine the red glass carefully with the spectroscope, we find that it not only transmits the red rays powerfully, but that *a little* of the orange rays also passes through with still smaller portions of the green and blue rays. Hence we are dealing not only with spaces in the spectrum, but with the relative intensities of the coloured light filling those spaces. It is difficult, or rather impos-

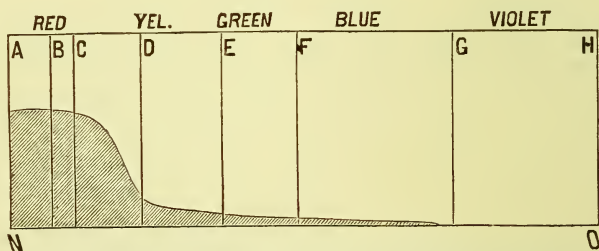


FIG. 17.—Spectrum, showing the Extent and Intensity of the Coloured Light transmitted by Red Glass. The shaded portion represents the transmitted light.

sible, to represent the different intensities by shading on paper; hence physicists have adopted a certain convention which removes this trouble, and enables them to express differences in luminosity readily and accurately. All this is accomplished by drawing a curve, and agreeing that distances measured upward to it shall represent different degrees of luminosity. We agree, then, to let the entire rectangle A H O N, Fig. 17, represent a solar spectrum, with

its different colours properly arranged, and having their natural or normal luminosities, and in this rectangle we draw the curve furnished by the red glass (Fig. 17). We find that it is highest in the red space; but even here it reaches only about half way up, showing that the luminosity of the transmitted red light is only half as great as that of the same light in the spectrum; in the orange space it falls rapidly off, the curve sinking with a steep slope; after that it runs out into the green and blue, almost to the violet, in such a way as to indicate that the red glass transmits minute quantities of these different kinds of coloured light. The luminosity, then, of all the transmitted rays, except the red, being quite feeble, the light which comes through appears pure red. Making an examination of an orange-yellow glass in the same way, we obtain the curve shown in Fig. 18: this glass, it appears, transmits most of the red,

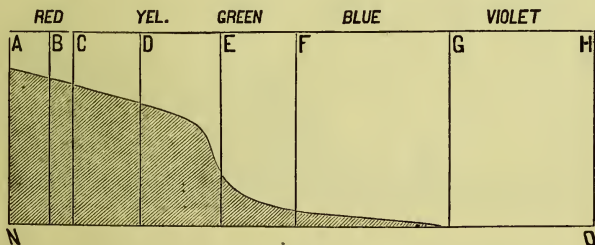


FIG. 18.—The shaded portion shows the amount of light transmitted by an orange-coloured glass.

orange, and yellow rays, with much of the green and a little of the blue. Here, of course, the orange and yellow rays after transmission make up an orange-yellow hue, and the green and red rays by their union reproduce the same colour, as we shall see in Chapter X. Hence the final colour is orange-yellow, without the least tint of red or green. Taking next a green glass, we obtain another curve, Fig. 19, showing that much green light is transmitted, but along

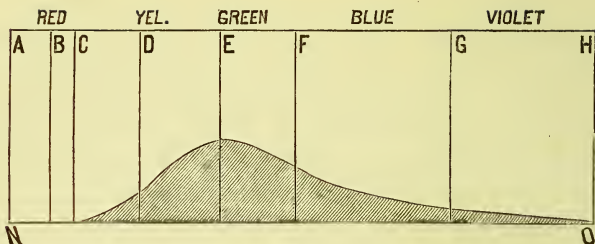


FIG. 19.—The shaded portion represents the amount of light transmitted by green glass.

with it some red and some blue. Blue glass shows the cyan-blue weakened, the ultramarine-blue and violet strong; the green is very weak, so also are yellow and orange; the red is mostly absent, except a feeble extreme red. The result is of course a violet-blue (Fig. 20). A purple glass is

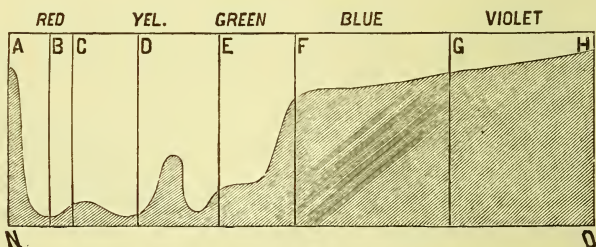


FIG. 20.—The shaded portion represents the amount of light transmitted by blue glass.

found to absorb the middle of the spectrum, i. e., the yellow, green, and cyan-blue; the red and violet are also enfeebled, but are at all events far stronger than the other transmitted rays. We have, then, as a final result, red, ultramarine-blue, and violet, which being mingled make purple. It is evident from these experiments that the colours produced by absorption are not simple, like those furnished by the prism, but are resultant hues, produced by the mixture of many different kinds of coloured light hav-

ing varying degrees of brightness. On this account, and by reason of the tendency of many kinds of stained glass to absorb to a considerable extent all kinds of coloured light presented to them, it happens that stained glass furnishes us with coloured light inferior in purity and luminosity to that obtained by the use of a prism. Nevertheless these colours are the purest and most intense that we meet with in daily life, and far surpass in brilliancy and saturation those produced by dyestuffs or pigments.

There is one property which probably all substances possess which produce colour by absorption, upon which a few words must be now bestowed. If we cause white light to pass through a single plate of yellow glass, the rays which reach the eye will of course be coloured yellow. Add now a second plate of the same glass, and the light which traverses the double plate assumes a somewhat different appearance; it evidently is not so luminous, and its *colour* is no longer quite the same. Using six or eight plates of the yellow glass, we find that the transmitted light appears orange. If the same experiment be repeated, using a considerable number of plates of the same glass, the colour will change to dark red. From this it appears that the colour of the transmitted beam of light depends somewhat on the thickness of the absorbing medium. This change in the case of some liquids is very considerable: thin layers, for example, of a solution of chloride of chromium transmit green light mainly, and so imitate the action of a plate of green glass; thick layers of the same liquid transmit less light in general, but the dominant colour is red, and objects viewed through them look as they would, seen through a plate of dark-red glass. This curious property is easily explained by an examination of the action of the liquid on the prismatic spectrum. In Fig. 21 the curve represents the relative intensity of the coloured light in different portions of the spectrum. If we cut off successively slices of the rectangle, as is done in Figs. 22

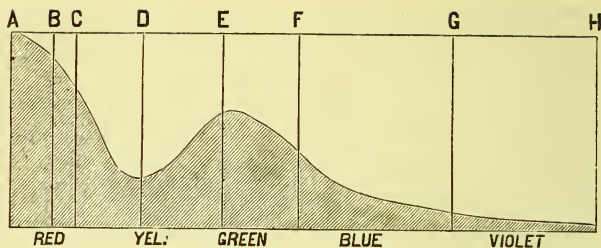


FIG. 21.—The shaded portion represents the amount of light transmitted by chloride of chromium.

and 23, we obtain the curves corresponding to a greater and greater thickness of liquid, and it is plain that at last we shall have the state of things indicated in Fig. 23; the

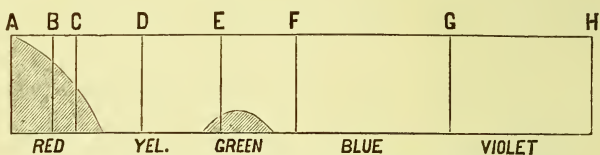


FIG. 22.—Chloride of Chromium; Effect produced by a Thick Layer.

curve is about the same as for red glass (Fig. 17), and the final colour is red. This is an extreme case, but in stained glasses, pigments, dyestuffs, etc., there is generally a ten-

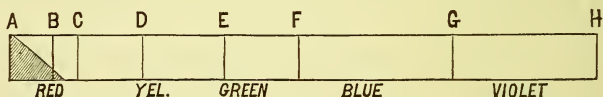


FIG. 23.—Chloride of Chromium; Effect produced by a very Thick Layer.

dency toward the production of effects of this kind, some of which will hereafter be noticed.

The colours of painted glass are similar to those of stained glass in origin and properties; both are intense, rather free from admixture with white light, and capable

of a high degree of luminosity. In these respects they far surpass the colours of pigments, which compared with them appear feeble and dull, or pale. Owing to this circumstance, chromatic combinations may be successfully worked out in stained glass, which would prove failures if attempted with pigments or dyestuffs. Hence also the wonderfully luminous appearance of paintings on glass viewed in a properly darkened room : they surpass in some respects oil or water-colour paintings to such a degree that the two are not to be mentioned together. There is no doubt but that glass-painting offers advantages for the production of realistic effects of colour and light and shade, such as the very narrow scale of oil and water-colour utterly denies ; and yet great artists seem to reject this process, and severely confine themselves to work on canvas or paper, choosing to depend for their effects rather on pure technical skill and artistic feeling.

If we place on a sheet of white paper a fragment of pale-blue glass, it will display its colour, though not so brilliantly as when held so that the light of the window streams through it directly. The reason is very evident : the light which penetrates the glass falls on the paper and is reflected by it back through the glass to the eye. The light then traverses the glass twice, but this is not the only cause of its inferior luminosity, for a double plate of the same glass held before the window appears still far brighter than the single glass on the paper. The other reason is that the paper itself reflects only a small amount of the light falling on it. Upon examining the matter more closely we find also that the blue glass reflects from its surface quite a quantity of white light, which, when mingled with the coloured light, renders it somewhat pale. If, now, we grind up into a very fine powder some of the blue glass, we obtain the pigment known as smalt, and, after mixing it with water, we can wash our white paper with a thin layer of it. When it dries the

paper will be coloured blue, but the hue will be neither so luminous nor so intense as that of the light directly transmitted by the blue glass when held before a window. Its origin, however, is similar: the white light after traversing a layer of the minute blue particles reaches the paper, and is reflected backward once more through them toward the eye. In this process many coloured rays suffer absorption, and only a small portion of the constituents of the original beam finally reach the eye. In the original experiment, where the blue glass was simply laid on the white paper, it sometimes happened that the white light regularly reflected from its first surface mingled itself with the coloured light and caused it to look paler, but it was always possible to arrange matters so that this damaging coincidence did not occur. In the experiment with the blue powder spread on the paper this is impossible, for the surfaces of the little particles lie with all possible inclinations, so that, hold the paper as we will, it is sure to reflect much white along with its coloured light. What we have, then, to expect when pigments in dry powder are spread on white paper is, that they will reflect only a moderate quantity of coloured light to the eye, and that it will be rendered somewhat pale by admixture with white light.

With the aid of a little hand spectroscope these points are readily demonstrated: when we direct the instrument toward our blue paper, we find that all the colours of the spectrum are present in considerable quantities—hence some white light must be reflected from the paper; we also notice that the red, yellow, orange, and green rays are present in less quantity than in an ordinary prismatic spectrum—hence the curve for the smalt-paper is like that given in Fig. 24. In making examinations with the spectroscope of the coloured light reflected from painted surfaces, it is advantageous to use simultaneously, along with the strip of painted paper, one which is white and a third which is black. It has been found by the author that paper painted dead-black

with lampblack, to which has been added just enough spirit varnish to prevent its rubbing off, but not enough to cause it in the least degree to shine, reflects $\frac{5}{100}$ as much light as white paper. Hence if we set the luminosity of white paper as 100, that of dead-black paper will be 5. Now, when a

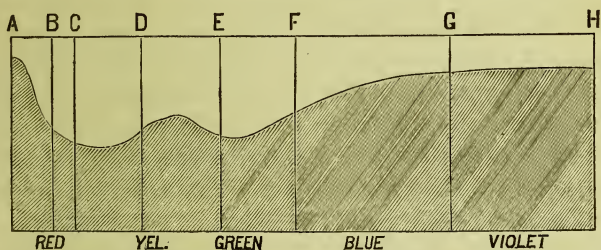


FIG. 24.—Curve for Smalt-paper : the shaded portion represents the light reflected by smalt-paper.

strip of this black paper is placed before the slit of the spectroscope it acts like white paper seen under a feeble illumination, and consequently furnishes a complete though not a very luminous spectrum. By using, then, a black-and-white strip along with the one which has been painted, we can ascertain several facts which may best be explained with the help of an example. Let us first select vermilion in dry powder, and undertake an examination of its optical properties in this way. We find that the red of its spectrum is about as powerful as the red in the spectrum from white paper, and that the other colours, though all present, are not much if any stronger than those from the black paper. This is all we can demand from any pigment : it reflects to the eye its full share of the rays it professes to reflect, and they are not mingled with more white light than is reflected by dead-black paper. Emerald-green when tested in this way proves sensibly inferior to vermilion : examined in dry powder the green space was bright, but less bright than that from white paper ; the other colours had about the same degree of luminosity as those from the black paper,

except the violet, which was not present. Chrome-yellow reflected the red, orange, yellow, and green rays about as brilliantly as white paper; the cyan-blue, ultramarine, and violet, about like black paper. Hence the great luminosity of this pigment, for it reflects not only the yellow rays abundantly, but also all the other rays of the spectrum which are distinguished for luminosity. As before remarked, the sum of these rays makes up yellow. It is plain from these experiments that a painted surface can never be as luminous as one which is white; the most that can be demanded from a painted surface is, that it should reflect its peculiar coloured light as powerfully as a white surface does; the very cause of its furnishing coloured light is, that it fails to reflect all the coloured rays equally well. Hence coloured surfaces are always darker than those which are white. If we set the luminosity of white paper as 100, that of vermilion will be about 25, emerald-green 48, and chrome-yellow as high as 75 or 80.

These experiments can now be repeated with the same pigments covered by a layer of water. The surface of the water being quite flat, the spectroscope can be held in such a way as to avoid the light directly reflected from the water, and it then becomes possible to observe certain changes which the presence of the water brings about. In the case of vermilion we find that the blue and violet portions of the spectrum almost entirely vanish, a little of the yellow, orange, and green spaces remains, and the red is nearly as powerful as before. This proves that the presence of the water has greatly diminished the amount of *white* light reflected from the surfaces of the particles of pigment, but has not much affected the brilliancy of the reflected coloured light. Experiments with emerald-green and chrome-yellow give corresponding results; less light in general is reflected, but it is somewhat purer, there being not so much white light mingled with it. By immersing our pigments in oil or varnish we push these effects still further: the

pigments appear darker, but the colour is richer, and more nearly free from white light. The explanation of these changes is well known to physicists : they depend upon the fact that light moving in a rare medium like the air is abundantly reflected when it strikes on a dense substance like a pigment ; but if the pigment be placed under water we have then light moving in a dense medium (water), and striking on one which is only a little more dense (pigment) : hence but little white light will be reflected from the surface of the small particles. The coloured light which is so abundantly furnished by the pigment, even under water, has its source in reflections which take place in the interior of the somewhat coarsely grained particles of the pigment itself. If the pigment is naturally fine-grained, and also is mixed with a liquid like oil, having about the same optical density as itself, scarcely any light will be reflected from it, coloured or otherwise. Prussian-blue and crimson-lake, ground in oil, are good examples. In order to exhibit their colours it is necessary either to spread them in thin layers over a light surface, or to mix them with a white pigment ; alone by themselves they appear very dark, the Prussian-blue, indeed, almost black. Many other pigments are more or less affected in the same way by the presence of oil or varnish.

From what has been stated above it follows that the medium with which pigments are mixed has an important influence on their appearance. In drawings executed in coloured chalks, and in oil-paintings, we have the two extremes, works in water-colour being intermediate. Hence oil-painting is characterized by the richness of the colouring and the transparency and depth of its shadows, while in pastel drawings the tints are paler, the shadows less intense, and over the whole is spread a soft haze which lends itself readily to the accurate imitation of skies and distances. Changes in the medium are sometimes a source of embarrassment to the painter. This is particularly true in the

process of fresco-painting, and also to some extent in that of water-colour : as long as the pigment is moist it appears darker than afterward when dry, and it is necessary for the artist in laying on each wash to make a proper allowance for these changes ; this is one of the minor causes that render the process of painting in water-colours more difficult than that in oils.

As has already been stated, when we obtain our coloured light from pigments, it is apt to be more mingled with white light than when stained glass is used ; but, besides this, it is inferior to that from stained glass in the matter of luminosity. The range of illumination in our houses is small, so that practically the scale of light at the disposal of the painter in oils or water-colours is quite limited ; in point of fact he is obliged by the necessities of the case to employ means which are quite inadequate : hence the extraordinary care with which he husbands his resources in the matter of light and shade, and his constant struggle for excellence and decision in colouring. Muddy and dirty colours are instantly recognized to be such under a feeble illumination, even though they have passed muster under the blaze of full sunlight. Almost any surface looks beautiful if very brightly illuminated ; the eye is dazzled, and remains unconscious of defects that are instantly exposed under the feebler light of a gallery.

The colours which are exhibited by woven fabrics are due, like those of stained glass, to absorption. In the case of silk and wool the dye penetrates the fibres through and through, so that under the microscope they have much the same appearance as fine threads of stained glass. When white light falls upon a bundle of such coloured fibres, a portion is reflected uncoloured from the surface of the topmost fibres, while another portion penetrates to the rear surfaces of these same fibres and there is again subdivided, some rays penetrating still deeper into the bundle, while others returning to the upper surface emerge coloured.

This process is repeated on each deeper-lying set of fibres, and the result is that a good deal of strongly coloured light is sent to the eye, mingled with a portion due to the surface layers, which is more faintly coloured ; there is in addition a small portion which is quite white. It will be seen that the reflective power of the fibres is an important element in this process, for all the coloured light which reaches the eye is sent there by reflection. If we take *similar* structures of silk and wool, we can compare directly the lustre or reflective power of the individual fibres, with the aid of a lens magnifying ten or fifteen diameters. A silk-cocoon and a piece of white felting answer very well for this purpose, and when they are compared under the microscope it is very evident that the natural lustre of the silk is greatly superior to that of the wool. On comparing in this way the felting with white cotton batting, it will be found that the wool surpasses the cotton in lustre, the latter appearing almost dead-white and free from sparkle. It follows from this that the coloured light which is reflected from silk is more saturated or intense, and appears richer, than that from wool. The fibres of silk also can be made to lie in straight, parallel, compact bundles, which enables them to reflect the white light in definite directions, whereas woollen fabrics reflect it equally well in all directions. It results from this that a fabric of silk is capable, according to circumstances, of exhibiting a rich saturated colour nearly free from white light, or it may reflect much white light and exhibit a pale colour. This sparkling play of colour is beautiful, and causes the more uniform appearance shown by woollen fabrics to appear dull and tame. On the other hand, the superior transparency of the dyed fibres of wool over those of cotton give to the colours of the former material a certain appearance of richness and saturation, and cause the tints of the cotton to appear somewhat opaque.

In velvet the attempt is made to suppress all surface-light, and to display only those rays which have penetrated deeply

among the fibres, and have become highly coloured. This is accomplished by presenting to the light a surface which is entirely composed of the ends of fibres, and consequently which has little or no capacity for reflecting light. The rays then penetrate between the fibres thus set up on end, and, after wandering among them, finally again in some small quantity reach the surface as richly coloured light, which produces its full effect undiminished by any admixture of white light from the surface. In the case of silk-velvet the desired effect is for the most part actually realized : the colours are rich, and an examination with a lens shows that scarcely any of the fibres reflect white light, even when the fabric is held in unfavourable positions. If cotton-velvet is subjected to a similar examination under a lens, it will be found to reflect much surface-light, particularly when not quite new, and the surface will present a broken, rough appearance, quite different from that of its more aristocratic rival.

It would appear that at present it is actually possible to employ for woven fabrics dyes which furnish coloured light having a degree of intensity and purity which is actually undesirable. This is the case with some of the aniline dyes. Dresses dyed with some of them, when seen in full daylight, act on the eye so powerfully that mere momentary inspection gives rise to the phenomenon of accidental colours (see Chapter VIII.). These harsh effects are interesting as conveying certain information that our dyers have already touched, and indeed gone beyond, the greatest allowable limits in the matter of the intensity and purity of their hues. At least this applies to large surfaces, such as complete dresses, etc. In the case of smaller articles, such as ribbons, etc., these intense colours are more allowable, just as the flash of diamonds is more tolerable on account of their insignificant size.

We have seen, thus far, that the colours of pigments and dyestuffs are due to absorption, and to this same cause

we must attribute the colours of most objects which occur in landscapes. Two of these are so important that it will be worth while to devote a few moments to their separate consideration : we refer to the colour of water, and to that of vegetation. The colour of large masses of water, such as lakes and rivers, is so much influenced by that of the sky that many persons consider it to depend wholly on it, and are disposed to doubt whether water has any proper colour of its own. It is quite true that a small quantity of pure water, such as is contained in a drinking-glass, appears perfectly colourless, and that the light from white objects passes through it without suffering sensible absorption. If, however, we allow the white light from a porcelain plate to traverse a layer of pure distilled water two metres in thickness, it will be found to be tinged bluish. This experiment, which was first made by Bunsen, proves that an absorption takes place along the red end of the spectrum, and that water is really coloured in the same sense as a weak solution of indigo. The water of the lake of Geneva is quite pure, being produced mainly by the melting of glaciers ; the granite meal mingled with the water, being coarse, soon settles to the bottom, and leaves it free from turbidity. Hence along the wonderful shores of this lake it is easy to repeat the experiment of Bunsen, and to study the colour of this liquid. White objects, resting on the bottom in the shallow places where the depth is six or eight feet, show very plainly a greenish-blue hue, and the tint can be examined at different depths by lowering a piece of white porcelain with a string. Even on cloudy days, when the sky is overcast and grey, the lake itself displays a wonderfully intense cyan-blue colour, while on clear days, on looking down into its waters, one is tempted to believe that it is a vast natural dyeing-vat. When vegetable matter is present in small quantity the colour of water changes to a bluish-green ; many excellent examples occur among the beautiful lakes of the Tyrol. Decaying organic matter,

on the other hand, tinges water brownish, and lakes or rivers of this colour are apt to assume on cloudy days a silver-grey appearance, while under a clear sky they often appear very decidedly blue. There seems to be some reason to believe that the absorptive action of pure water on white light changes with its temperature, and that warm water is actually more deeply coloured than cold water. Heat has an action of this kind upon many coloured substances, and Wild with his photometer actually found that both distilled and pump water showed somewhat stronger colours on being heated. He accounts in this way for the more intense colour which it is claimed mountain lakes display during the summer months.

The green colour of vegetation offers a rather peculiar case. When we examine with the spectroscope any ordinary green pigment, we find that the red is absent and the blue and violet much weakened, as was the case with em-

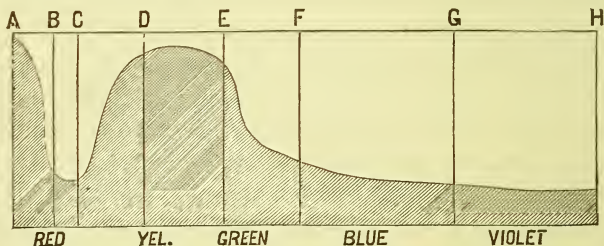


FIG. 25.—The shaded portion represents the light reflected by green leaves.

erald-green. Green leaves, however, furnish a spectrum of a different character: the extreme red is present; then occurs a deficiency of coloured light, which is followed by an orange-red space; next comes the orange, then the yellow, greenish-yellow, and yellowish-green; after this follows a little full green; the rest of the spectrum decreases rapidly in luminosity. Fig. 25 represents this spectrum. The sum of all these colours is a somewhat yellowish green, which is accordingly the colour presented by green leaves

in white light. It will be shown in Chapter X. that a mixture of red and green light furnishes yellow light, which explains the production of a yellowish-green in this somewhat singular way. It follows, from the analysis just given, that green leaves are capable of reflecting a considerable quantity of red light, where surfaces painted with green pigments would not have this power, and consequently would appear black or grey. Hence under the red light of the setting sun foliage may assume a red or orange-red hue. Corresponding to this, when the illumination is of an orange colour, foliage will partake more of this hue than would be the case with ordinary green pigments. Connected with this is also the great change of colour which foliage experiences according as it is illuminated by direct sunlight or by light from the blue sky, the tint in extreme cases varying from a yellow or slightly greenish yellow up to a bluish-green.

Simler has constructed a simple and beautiful piece of apparatus, based on the singular property which living leaves have of reflecting abundantly the extreme red rays of the spectrum ; it is called an *erythroscope*. A plate of blue glass, stained with cobalt, is to be procured, having a thickness such that it will allow the extreme red of the spectrum to pass, but no orange or yellow ; it should also transmit the small band of greenish-yellow just before the fixed line E, and all the green from *b* to F, also all the blue and violet. A plate of rather deeply coloured yellow glass is also needed ; this should be capable of transmitting all the light of the spectrum from the farthest red up to G ; that is to say, it should cut off the violet and blue-violet only. When a sunny landscape is viewed through these two glasses, it assumes a most wonderful appearance : all green trees and plants shine with a coral-red colour, as though they were self-luminous ; the sky is cyan-blue,* the clouds purplish-violet ; the earth and rocks assume various

* Cyan-blue is a greenish-blue.

tints of violet-grey. Pine-trees appear of a dark-red hue ; orange or yellow flowers become red or blood-red ; greens, other than those of the foliage, are seen in their natural tints, or at least only a little more bluish ; lakes preserve their fine blue-green colouring, and the play of light and shade over the landscape is left undisturbed ; the whole effect is as though a magician's wand had passed over the scene, and transformed it into an enchanted garden. For the full realization of these effects it is essential that stray light should be prevented from reaching the eyes, and accordingly the glasses should be mounted in an arrangement of wood or pasteboard which adapts itself to the contours of the face, and excludes as much as possible diffuse light. On comparing the spectrum given by the blue and yellow glasses with that of green leaves, it will be found that the two glasses cut off almost all the green light furnished by the leaves, but allow those green rays of light to pass which the leaves are incapable of supplying.

The colours which metals such as copper, brass, or gold display, are due to absorption. A quantity of white light is reflected from the real surface, but along with it is mingled a certain amount which has penetrated a little distance into the substance of the metal, and there has undergone reflection ; this last portion is coloured. If we cause this mixture of white and coloured light to strike repeatedly on a metallic surface—for example, such as gold—we constantly increase the proportion of light which has penetrated under the surface, and has become coloured. A process of this kind takes place in the interior of a golden goblet ; hence the colour in the inside is deeper and more saturated than on the outside. Some metals, like silver or steel, hardly show much colour till the light has been made to strike repeatedly on their surfaces ; when this is done with silver, the light gradually assumes a yellow colour, while with steel it becomes blue.

The true colour of metals must not be confounded with that which is often given to them by the presence of a surface-film of oxide or sulphide ; such films cause for the most part a bluish appearance, though all the colours of the spectrum may be produced on metals in this way. In fact, the hue in these cases is due to an interference of light caused by the thin layer of oxide, and is quite distinct from the actual colour of the metal. (See Chapter IV.)

Metals, whether coloured or white, are chiefly remarkable for the large quantities of light which they are capable of reflecting. Measurements made by Lambert have shown that the *total amount* of light reflected by white paper is about forty per cent. of the light falling on it. Silver, however, is capable of reflecting ninety-two per cent. ; steel sixty per cent., etc.

Polished surfaces, particularly of metals, have another property which adds to their apparent brilliancy, and increases their lustrous appearance. Those portions of the surface which are turned away from the light often reflect but little, and look almost black. This sharp contrast enhances their brilliant, sparkling appearance, and raises them quite above the rank of surfaces coloured by pigments. In consequence of this, metals cannot be used along with pigments in serious or realistic painting ; they are quite out of harmony, and produce the impression that the painter has sought to help himself by a cheap trick rather than by employing the true resources of art. In those cases where gold was so extensively used during the middle ages for the backgrounds of pictures of holy personages, or even for the adornment of their garments, the object was far more to produce symbolic than realistic representations, and here the presence of the gold was actually a help, as tending to convey the idea that the painting was not the portrait of an ordinary mortal, but rather a childlike attempt to depict and lavishly adorn the ideal image of a venerated and saintly character. On the other hand, this brilliancy of

gold, with its rich colour, preëminently adapts it for the purpose of inclosing paintings and isolating them from surrounding objects. A painted frame or wooden frame, inasmuch as its colour belongs to the same order as those contained in the picture, becomes as it were an extension of it, and is apt to injure the harmony of its colouring ; and, besides this, its power of isolation is inferior to that of gold, on account of its greater resemblance to ordinary surrounding objects.

Having now considered with some detail the colours that are produced by absorption, it may be well to add a few words concerning the attempts that have been made to reproduce colour by the aid of photography. Photographs render accurately the light and shade, why should they not also record the colours, of natural objects? In 1848 E. Becquerel announced that he had been able to photograph the colours of a prismatic spectrum falling on a silver plate which had been treated with chlorine. These colors were quite fugitive, lasting only a few minutes. In 1850 Niépce de Saint-Victor and in 1852 J. Campbell claimed that they had rendered these colours more permanent. In 1862 the former experimenter, by washing the finished plates with a solution of dextrin containing chloride of lead, obtained coloured pictures that lasted twelve hours. In the following year he still further improved his process, the colours lasting three or four days in rather strong daylight. An examination of the details of these memoirs and of the pictures indicates that the colours thus obtained are due to a greater or less reduction of the film of chloride of silver, and are, in fact, produced merely by the interference of light, and consequently have no necessary connection with the hues of the natural objects to which they seem to owe their origin. Hence we must regard this problem as unsolved, and in the present state of our knowledge there

does not seem to be any reason to suppose that it ever will be solved. Why should the red rays when acting on a certain substance produce a red compound, the green and violet rays green and violet compounds, and so on with all the other coloured rays? But photography in colour implies exactly this.

This problem has more recently been handled in an entirely different manner, and with a more hopeful result, from a practical point of view. Suppose we place a red glass before a photographic camera, and photograph some object with brilliant colours—a carpet, for example. We shall obtain an ordinary negative picture, which will be entirely due to the red light sent by the carpet toward the instrument. Portions of the carpet having a different colour will not be photographed at all. Next let us hold before the camera a glass which transmits only the yellow rays (if such glass could be found), and we shall obtain a picture of the yellow constituents of the carpet; the same is to be done with a blue glass. From these three ordinary negatives, three positive pictures are to be made in gelatine, the first being colored with a transparent red pigment, the second with a yellow, the third with a blue pigment. The first sheet of gelatin will contain a red picture, due to the red parts of the carpet; the second and third, similar yellow and blue pictures. When these transparent coloured sheets are laid over each other, we shall have a picture correct in drawing, which will roughly reproduce the colours of the carpet. This gives an idea of the plan proposed in 1869 by C. Cross and Ducos du Hauron, for the *indirect* reproduction of colour by photography. In actual practice the negatives were taken with glasses coloured orange, green, and violet; these negatives were then made to yield blue, red, and yellow positive pictures. This process has been greatly improved by Albert, of Munich, and by Bierstadt, of New York. In the final picture the gelatine is dispensed with, films of colour, laid on by lithographic stones,

being substituted. The selection of the pigments is necessarily left to the judgment of the operator, and in its present state the process is better capable of dealing with the decided colours of designs made by the decorator than with the pale, evanescent tints of Nature.

APPENDIX TO CHAPTER VII.

We give below a list of pigments which, according to Field and Linton, are not affected by the prolonged action of light, or by foul air :

White.

Zinc-white.
True pearl-white.
Baryta-white.
Tin-white.

Red.

Vermilion.
Indian red.
Venetian red.
Light red.
Red ochre.

Yellow.

Cadmium-yellow.
Lemon-yellow.
Strontia-yellow.
Yellow ochre.
Raw Sienna.
Oxford ochre.
Roman ochre.
Stone ochre.
Brown ochre.

Black.

Ivory-black.
Lampblack.
Indian ink.
Graphite.

Orange.

Orange vermilion.
Jaune de Mars.
Orange ochre.
Burnt Sienna.
Burnt Roman ochre.

Green.

Oxide of chromium.
Rinman's green.
Terre-verte.

Blue.

Ultramarine.
Blue ochre.

Violet.

Purple ochre.
Violet de Mars.

Brown.

Rubens's brown.
Vandyck brown.
Raw umber.
Burnt umber.
Cassel earth.
Cologne earth.
Bistre.
Sepia.
Asphalt.

White lead, smalt and cobalt-blue are not affected by light, but are by foul air. The last two are considered permanent in water-colour painting.

According to Field, the tints of the following pigments are not affected by mixture with lime, consequently they are adapted for use in fresco-painting :

White.

Baryta.
Pearl.
Gypsum.
Pure earths.

Red.

Vermilion.
Red lead.
Red ochre.
Light red.
Venetian red.
Indian red.
Madder red.

Yellow.

Indian yellow.
Yellow ochre.
Oxford ochre.
Roman ochre.
Stone ochre.
Brown ochre.
Raw Sienna.
Naples yellow.

Black.

Ivory-black.
Lampblack.
Black chalk.
Graphite.

Orange.

Orange vermilion.
Chrome-orange.
Orange ochre.
Jaune de Mars.
Burnt Sienna.

Green.

Terre verte.
Emerald green.
Mountain green.
Cobalt-green.
Chrome-green.

Blue.

Ultramarine.
Smalt.
Cobalt.

Purple.

Madder purple.
Purple ochre.

Brown.

Vandyck brown.
Rubens's brown.
Raw umber.
Burnt umber.
Cassel earth.
Cologne earth.
Antwerp brown.
Bistre.

As the effect of light on pigments is a matter of considerable importance to artists, particularly to those working with the thin washes used in water-colour painting, a careful experiment on this

matter was made by the present writer. The washes laid on ordinary drawing-paper were exposed during the summer to sunlight for more than three months and a half, and the effects noted; these were as follows :

WATER-COLOUR PIGMENTS THAT ARE NOT AFFECTED BY LIGHT :

<i>Red.</i>	<i>Orange.</i>	<i>Yellow.</i>
Indian red.	Jaune de Mars.	Cadmium-yellow.
Light red.		Yellow ochre.
		Roman ochre.
<i>Green.</i>	<i>Blue.</i>	<i>Brown.</i>
Terre verte.	Cobalt.	Burnt umber.
	French blue.	Burnt Sienna.
	Smalt.	
	New blue.	

The following pigments were all more or less affected; those that were very little changed head the list, which is arranged so as to indicate the relative amounts of damage suffered, the most fugitive colours being placed at its end :

Chrome-yellow becomes slightly greenish.
 Red lead becomes slightly less orange.
 Naples yellow becomes slightly greenish brown.
 Raw Sienna fades slightly; becomes more yellowish.
 Vermilion becomes darker and brownish.
 Aureoline fades slightly.
 Indian yellow fades slightly.
 Antwerp blue fades slightly.
 Emerald green fades slightly.
 Olive green fades slightly, becomes more brownish.
 Rose madder fades slightly, becomes more purplish.
 Sepia fades slightly.
 Prussian blue fades somewhat.
 Hooker's green becomes more bluish.
 Gamboge fades and becomes more grey.
 Bistre fades and becomes more grey.
 Burnt madder fades somewhat.
 Neutral tint fades somewhat.
 Vandyck brown fades and becomes more grey.
 Indigo fades somewhat.
 Brown pink fades greatly.

Violet carmine fades greatly, becomes brownish.

Yellow lake fades greatly, becomes brownish.

Crimson lake fades out.

Carmines fades out.

To this we may add that rose madder, burnt or brown madder, and purple madder, all, are a little affected by an exposure to sunlight for seventy hours. Pale washes of the following pigments were completely faded out by a much shorter exposure to sunlight:

Carmines,	Yellow lake,	Italian pink,
Full red,	Gall-stone,	Violet carmine.
Dragon's blood,	Brown pink,	

CHAPTER VIII.

ON THE ABNORMAL PERCEPTION OF COLOUR, AND ON COLOUR-BLINDNESS.

WE have considered now, with some detail, the various ordinary modes of producing the sensation of colour ; but, in order to render our account more complete, it is necessary to touch on some of the unusual or extraordinary methods. In every case examined thus far, the sensation of colour was generated by the action on the eye of coloured light—that is, of waves of light having practically a definite length. As colour, however, is only a *sensation*, and has no existence apart from the nervous organization of living beings, it may not seem strange to find that it can be produced by white as well as by coloured light, or even that it can be developed in total darkness, without the agency of light of any kind whatever. If the eyes be directed for a few moments toward a sheet of white paper placed on a black background and illuminated by sunlight, on closing them and excluding all light by the hands or otherwise, it will be found that the absence of the light does not at once cause the image of the paper to disappear. After the eyes are closed it will still be plainly visible for several seconds, and will at first be seen quite correctly, as a white object on a black ground ; the colour with some observers then changes to blue, green, red, and finally back to blue, the background remaining all the while black. After this first stage the background changes to white, the colour of the sheet of paper appearing blue-green, and finally yellow. Most of these colours are

as distinct and decided as those of natural objects. If the experiment be made for a shorter time, and under a less brilliant illumination, the eyes being first well rested by prolonged closure, the series of colours will be somewhat different. Fechner, Seguin, and Helmholtz observed that the original white colour passed rapidly through a greenish blue (Seguin, green) into a beautiful indigo-blue ; this afterward changed into a violet or rose tint. These colours were bright and clear, afterward followed a dirty or grey orange ; during the presence of this colour the background changed from black to white, and the orange tint altered often into a dirty yellow-green which completed the series. If, instead of employing white, a coloured object on a grey ground is regarded intently for some time, the eyes will be so affected that, on suddenly removing the coloured object, the grey ground will appear tinged with a complementary



FIG. 26.—Disk with Black and White Sectors for the Production of Subjective Colour.



FIG. 27.—Black and White Spiral on Disk, for the Production of Subjective Colour.

tint ; for example, if the object be red, the after-image will be bluish green. It is not necessary to dwell longer on these phenomena at present, as a portion of Chapter XV. will be especially devoted to them. In both the cases mentioned above, the colour develops itself after the eyes are closed, or at least withdrawn from the illuminated surface. There are, however, cases where very vivid colours can be seen while the eyes are exposed to full daylight. If a disk

of cardboard painted with alternate white and black sectors, like that shown in Fig. 26, be set in rotation while exposed to full daylight, colours will be seen after a few trials. It will be found that a certain rate of rotation communicates to the disk a green hue, a somewhat more rapid rate causing it to assume a rose colour. According to Helmholtz, these effects are most easily attained by using a disk painted with a black spiral, like that in Fig. 27. These phenomena may be advantageously studied by a method which was used by the author several years ago. A blackened disk with four open sectors seven degrees in width was set in revolution by clockwork, and a clouded sky viewed through it. With



FIG. 28.—Subjective Colours seen in Sky, with aid of Rotating Disk.

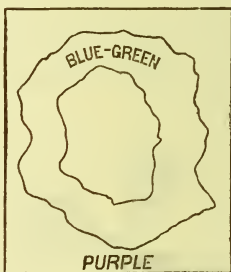


FIG. 29.—Subjective Colours, Ring, etc., seen in Sky with aid of Rotating Disk.

a rate of nine revolutions per second, the whole sky often appeared of a deep crimson hue, except a small spot in the centre of the field of view, which was pretty constantly yellow. Upon increasing the velocity to eleven and a half revolutions per second, the central spot enlarged somewhat, and became coloured bluish green, with a narrow, faint, blue border, indicated by the dotted line; the rest of the sky appeared purple, or reddish purple. (See Fig. 28.) With the exception of fluctuations in the outline of the spot, this appearance remained tolerably constant as long as the rate of revolution was steadily maintained. When the velocity

of the disk was increased, the bluish-green spot expanded into an irregularly shaped blue-green ring, which with a rate of fifteen turns per second mostly filled the whole field of view. (See Fig. 29.) With higher rates all these appearances vanished, and the sky was seen as with the naked eye.* More than one elaborate attempt has been made to found on phenomena of this class a theory of the production of colour, though it may easily be shown that in all such cases the disk really transmits not coloured but white light, and that the effects produced are due to an abnormal state of the retina caused by alternate exposure to light and darkness.

A current of electricity is also capable of stimulating the optic nerve in such a way that brilliant colours are perceived, although the experiment is made in perfect darkness. If the current of a strong voltaic battery be caused to enter the forehead, and travel hence to the hand, according to Ritter, a bright-green or bright-blue colour is perceived, the hue depending on whether the positive current enters the hand or forehead. Helmholtz, in repeating this operation, was conscious simply of a wild rush of colours without order. The experiment is, however, interesting to us, as proving the possibility of the production of the sensation of colour without the presence or action of light.

Recently a substance has been discovered which, when swallowed, causes white objects to appear coloured greenish yellow, and coloured objects to assume new hues. Persons under the influence of *santonin* cannot see the violet end of the spectrum ; and this fact, with others, proves that they have become temporarily colour-blind to violet.

An observation of Tait's, and others by the author, have shown that a shock of the nervous system may produce momentarily colour-blindness to green light. White objects then appear of a purplish red, and green objects of a much

* "American Journal of Science and Arts," September, 1860.

duller green hue than ordinarily.* These effects are evanescent, though quite interesting, as we shall see presently, from a theoretical point of view.

Investigations during the present century have shown that many persons are born with a deficient perception of colour. In some the defect is slight and hardly noticeable, while in others it is so serious as to lead to quite wonderful blunders. This imperfection of vision is often inherited from a parent, and may be shared by several members of the same family. It is remarkable that women are comparatively free from it, even when belonging to families of which the male members are thus affected. The occupations of women, their attention to dress and to various kinds of handiwork where colour enters in as an important element, seem to have brought their sense for colour to a higher degree of perfection than is the case with men, who ordinarily neglect cultivation in this direction. Out of forty-one young men in a gymnasium, Seebeck found five who were colour-blind; but during his whole investigation he was able to learn of only a single case where a woman was to some extent similarly affected. It not unfrequently happens that persons with this defect remain for years unconscious of it. This was the case with some of the young men investigated by Seebeck; and in one remarkable instance a bystander, in attempting to help a colour-blind person who was under investigation, showed that he was himself colour-blind, but belonged to another class! The commonest case is a deficient perception of red. Such persons make no distinction between rose-red and bluish-green. They see in the spectrum only two colours, which they call yellow and blue. Under the name yellow they include the red, orange, yellow, and green spaces: the blue and violet they name, with some correctness, blue. In the middle of the spectrum

* "American Journal of Science and Arts," January, 1877. A similar observation by Charles Pierce was communicated to the author while this work was going through the press.

there is for them a neutral or grey zone, which has no colour ; this, according to Preyer, is situated near the line F. For the normal eye it is greenish-blue ; for them, white. The extreme red of the spectrum, when it is faint, they fail to distinguish ; the rest of the red space appears to them of a saturated but not luminous green ; the yellow space has for them a colour which we should call bright green ; and finally, they see blue in the normal manner. Maxwell found that by the aid of his disks, using only two colours, along with white and black, he was able, by suitable variations in their proportions, to match for them any colour which presented itself ; while the normal eye requires at least three such coloured disks, besides white and black. His experiments led to the result that persons of this class perceive two of the three fundamental colours which are seen by the normal eye. Helmholtz also arrived at the same result. It is possible to render the normal eye to some extent colour-blind to red in the manner followed by Seebeck in 1837, and afterward by Maria Bokowa. These observers wore for several hours spectacles provided with ruby-red glasses ; and this prolonged action of the red light on the eye finally, to a considerable extent, tired out the nerve fibrils destined for the reception of red, so that on removing the glasses they saw in the spectrum only two colours. The second observer called them yellow and blue. Furthermore, the extreme red end of the spectrum was not visible to her, just as is the case with those who are actually blind to red ; all red objects appeared to her yellow, and dark red was not distinguishable from dark green or brown.

Dalton, the celebrated English chemist, suffered from this defect of vision, and was the first to give an accurate description of it ; hence this affection is sometimes named after him, Daltonism. It is very remarkable that, according to the observations of Schelske and Helmholtz, even in the normal eye there are portions which are naturally colour-blind to red, and when this zone of the eye is used the same

mistakes in matching colours are made. Such experiments are somewhat difficult to make without considerable practice, as it is necessary that the colored objects should be viewed, not directly, but by the eye turned aside somewhat. There is a simple means by which persons who are colour-blind to red can to some extent help themselves, and prevent the occurrence of coarse chromatic blunders, such as confusing red with green. Green glass does not transmit red light ; hence, on viewing green and red objects through a plate of this glass it will be found, even by persons who are colour-blind, that the red objects appear much more darkened than those which are green. On the other hand, a red glass will cause green objects to appear darker, but will not affect the luminosity of those having a tint similar to itself. The exact tints of the glasses are important, and they should of course be selected with the aid of a normal eye.

The kind of colour-blindness just described is rather common, and it has been estimated that in England about one person in eighteen is more or less afflicted with it. We pass on now to the consideration of a class of cases that is more rare. Persons belonging to this second class see only two colours in the spectrum, which they call red and blue. They set the greatest luminosity in the spectrum in the yellow space, as is done by the normal eye ; and they easily distinguish between red and violet, but confuse green with yellow and blue with red. In two cases examined by Preyer, yellow appeared to them as a bright red ; this same observer also found that in the spectrum, near the line *b*, the two colours into which they divided the spectrum were separated by a small neutral zone, which was for them identical with grey. A sufficient number of observations have not been accumulated to furnish means of ascertaining with certainty the exact nature of the difficulty under which they labour, though it is probable that they are colour-blind to green light. There are also observations on record of cases of temporary colour-blindness of a third kind, where the violet

end of the spectrum was seen shortened to a very remarkable extent ; and if it should prove that the cause was of a nervous character, rather than due to a deeper yellow colouration of the axial portions of the retina, this would demonstrate the existence of violet colour-blindness.

The subject of colour-blindness is one of considerable importance from a practical point of view, and this defect has no doubt been the occasion of railroad accidents. In 1873-'75 Dr. Favre, in France, examined one thousand and fifty railroad officials of various grades, and found among them ninety-eight persons who were colour-blind—that is, 9·33 per cent. In 1876 Professor Holmgren, in Sweden, examined the entire *personnel* of the Upsala-Gefle line, and out of two hundred and sixty-six persons ascertained that thirteen were colour-blind. These were found in every grade of the service, many of them being required daily to make use of coloured signals. It is singular that in no case had there been previously any suspicion of the existence of the defect. For further information with regard to the practical side of this matter, the reader is referred to the essay of Holmgren, which will be found in the Smithsonian Report for 1877 : a French translation also exists.

In concluding this subject, it may not be amiss to allude to the very remarkable case described by Huddart, of a shoemaker, an intelligent man, where only a trace of the power to distinguish colours seemed to remain.* According to the observations, he was colour-blind to both red and green, and in general seems to have had hardly any perception of colour, as distinguished from light and shade. Curiously enough, recent observations of Woinow show that even in the normal eye there is a condition like this at the farthest limit of the visible field of view ; here all distinctions of colour vanish, and objects look merely white or black, or grey. It is probable that between the case of

* "Philosophical Transactions," lxvii.

Harris, just mentioned, and that of a normal eye possessed of the maximum power of perceiving and distinguishing colours, a great number of intermediate gradations will be found to exist. Slight chromatic defects of vision generally receive no attention, or are explained in some other way. The writer recalls the case of an excellent physicist who for many years had a half suspicion that he was to some extent colour-blind, but rather preferred to explain the discrepancies by the assumption of a difference in nomenclature. Taking up the matter at last seriously, he made an investigation of his own case, and found that he actually was to some extent colour-blind to red. It has been suggested that the very inferior colouring of some otherwise great artists can be accounted for by supposing them to have been affected with partial colour-blindness ; this idea is plausible, but, as it appears to us, totally without proof. There are great numbers of persons who are able to hear distinctly all the notes employed in music, who yet have no talent for it and no enjoyment of it. On the other hand, we know of cases of persons who from infancy have been afflicted with partial deafness, and have nevertheless been musicians, and even composers. It is the same in painting as in music : the possession of a perfect organ is not by any means the first necessity, and it can be proved that even artists who are actually colour-blind to red may still, with but slight external aid, produce paintings which are universally prized for their beautiful colouring. Their field of operations is of course more restricted, and they are compelled to avoid certain chromatic combinations. During the evening, by gas- or lamp-light, we are all somewhat in the condition of persons who are colour-blind to violet ; but yet, with precautions and some patience, it is possible to execute works in colour, even at this time, which afterward stand the test of daylight. It would appear probable, then, that the difficulty with the inferior colourists above alluded to was not so much anatomical or physiological as psychological.

According to a theory recently proposed by Hugo Magnus, our sense for colour has been developed during the last four or five thousand years ; previous to this period it is assumed that our race was endowed only with a perception of light and shade. The evidence which is offered is of a philological character, and tends to show that the ancients either distinguished or described colours less accurately than the moderns. The same kind of reasoning might be applied to proving that children at the present day have but little power of distinguishing tints, as they usually scarcely notice any but the most intense colours. When, however, we study the prehistoric races at present existing on the globe, and living in the same style as their ancestors, we find them quite capable of discriminating colours, and often very fond of them. Going many steps lower, we meet with animals that have the power of perceiving and even imitating a series of colours with accuracy. This is the case with the chameleon, as shown by P. Bert, and also, according to Pouchet and A. Agassiz, with certain kinds of flounders. The skin of the chameleon is provided with an immense number of minute sacs filled with red, yellow, and black liquids ; the animal has the power of distending these star-like vesicles at pleasure, and thus adjusts its colour in a few minutes (after a series of trials) so as to match that of the surface on which it is placed. Its chromatic scale covers red, orange, yellow, and olive-green, and the mixtures of these colours with black, which includes of course an extensive series of browns. The olive-green is made by distending the yellow and black sacs, the effect being similar to that obtained by combining a black and yellow disk. (See Chapter XII.)

Corresponding to this, A. Agassiz has often noticed, when a young flounder was transferred from a jar imitating in colour a sandy bottom to one of a dark-chocolate hue, that in less than ten minutes the black-pigment cells would obtain a great preponderance, and cause it to appear wholly

unlike the yellowish-grey speckled creature which a few moments before had so perfectly simulated the appearance of sand. When removed to a gravelly bottom, the *spots* on the side became prominent.

If our sense for light and shade is old, but that for colour recent and still undergoing development, we should perhaps expect that it would require more time to recognize colour than appearances dependent simply on light and shade ; but, according to the experiments of the writer, forty billionths of a second answers as well for one as for the other act of perception.*

In closing this chapter, it may be well to mention a very simple but beautiful experiment, by which we all can easily place ourselves in a condition somewhat like that of Harris, where all or nearly all sensation of colour had vanished. If some carbonate of soda be ignited in the flame of a Bunsen burner, it will furnish an abundance of pure homogeneous light of an orange-yellow hue. This light is quite bright enough to illuminate objects in a darkened room, but all distinctions of colours vanish, light and shade only remaining. A red rose exhibits no more colour than its leaves ; gayly painted strips of paper show only as black or white or grey ; their colours can not even be guessed at. The human face divested of its natural colour assumes an appearance which is repulsive, and the eye in the absence of colour dwells on slight defects in the clearness and smoothness of the complexion. If now an ordinary gas-burner be placed near the soda flame, and allowed at first to burn with only a small flame, objects will resume their natural tints to some slight extent, and begin again faintly to clothe themselves with pleasant hues, which will deepen as more light is furnished, till they finally seem fairly to

* The amount of time necessary for vision. "American Journal of Science," September, 1871.

glow with radiant beauty. Those who have never witnessed an experiment of this kind have but little conception how great would be to us the loss of our sense for colour, or how dreary the world would seem, divested of the fascinating charm which it casts over all things.

APPENDIX TO CHAPTER VIII.

MAXWELL has published an account of his rather elaborate examination of the case of one of his students, who was colour-blind to red.* An apparatus was employed by which the pure colours of the spectrum could be mixed in any proportion; these colours were then mingled by the colour-blind person, in such a proportion as to produce to his eyes the effect of white. In this way the following equation was obtained: $33\cdot7$ green + $33\cdot1$ blue = white. Maxwell then, employing the same colours, obtained his own or a normal equation, which was: 26 green + $37\cdot4$ blue + $22\cdot6$ red = white. If we combine these equations by subtraction, we obtain: $22\cdot6$ red - $7\cdot7$ green + $4\cdot3$ blue = D; D being the missing colour not perceived by the colour-blind. The sensation, then,

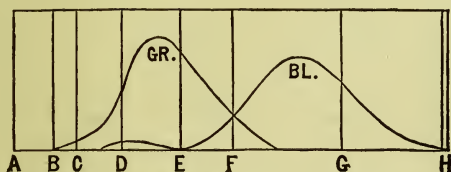


FIG. 30.—Curves of a Colour-blind Person. (Maxwell.)

which Maxwell had in addition to those of the colour-blind person was somewhat like that of a full red, but different from it in that the full red was mixed with $7\cdot7$ green, which had to be removed from it, and $4\cdot3$ of blue substituted. The missing colour, then, according to this experiment, was a crimson-red. Even normal eyes vary a little, and, if this examination had been made by Maxwell's

* "Philosophical Transactions" for 1860, vol. cl., p. 78.

assistant (observer K), the result would have been a red mixed with less blue, consequently a colour much more like the red of the spectrum. From experiments of this kind Maxwell was able to construct the curves of intensity of the two fundamental colours which are perceived by those who are colour-blind to red; these curves are shown in Fig. 30. The letters A, B, C, D, etc., mark the positions of the fixed lines in the solar spectrum; the curved line marked GR exhibits the intensity of the green element, the line marked BL that of the blue or violet. It will be noticed that the green sensation attains its maximum about half way between the lines D and E, that is, in the yellowish green; while the highest point of the other curve is about half way between F and G, that is, in the blue space. Maxwell also constructed similar intensity curves for a normal eye; they are represented in Fig. 31, the

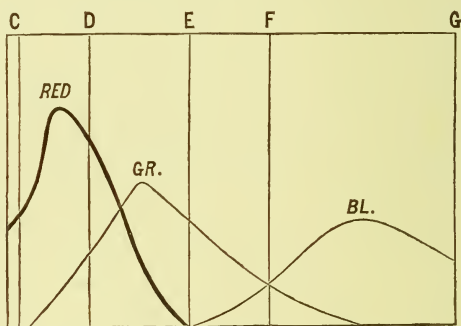


FIG. 31.—Curves of Normal Eye. (Maxwell.)

curve for red being indicated by a heavy line, the others as above. The green and blue curves have about the same disposition as with the colour-blind person, while the red attains its maximum between C and D, but nearer D—that is, in the red-orange space.

A set of observations was also made by Maxwell on the same colour-blind gentleman, with the aid of coloured disks in rapid rotation; and, from the colour equations thus obtained, the positions of the colours perceived by him were laid down in Newton's diagram, in a manner similar to that explained in the appendix to Chapter XIV. In Fig. 32, V shows the position assumed for red or vermilion; U, that of ultramarine-blue; and G, that of emerald-

green. They are placed according to Maxwell's method, at the three angles of an equilateral triangle. W would be the position of white for a normal eye, and Y that of chrome-yellow. D is the position of the defective colour, which Maxwell was able to imitate by mingling, by the method of rotating disks, 86 parts of vermilion and 14 of ultramarine-blue. A line drawn from D through W contains along its length the various shades of grey and the white of the colour-blind. The grey which they perceive when green and

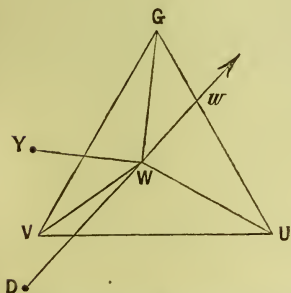


FIG. 32.—Newton's Diagram for a Person Colour-blind to Red. (Maxwell.)

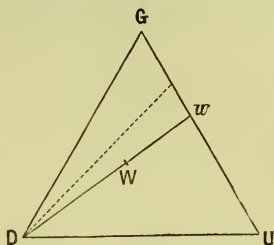


FIG. 33.—Newton's Diagram for a Person Colour-blind to the Fundamental Red.

blue are mixed lies at w ; the white of white paper, i. e., a more luminous grey, was on the same line but considerably farther along outside.

It may perhaps be as well to add to the above one or two remarks concerning the construction of Newton's diagram for the colour-blind. Let us suppose that the pure colours of the spectrum are employed, and that the missing colour is the fundamental red; we then place the fundamental green at G, Fig. 33, the fundamental blue or violet at U, and the missing red at D. Then along the line UG will lie mixtures of blue and green, and at w will be the white of the colour-blind person. Along the line DG will be situated various shades of green, from dark green to bright green, the latter colour predominating as we approach G. Along the line DU we shall have various shades of blue, from bright blue to dark blue, the colour being very dark near D and very bright near U. A line like the dotted one (Fig. 33) will contain various shades of green, from light green to dark green, but none of them so intense as

those situated along the line DG ; in other words, they all will be mingled with what the colour-blind call white.

If the defective colour-sensation is supposed still red, but to be only partially absent, the diagram takes the form indicated in Fig. 34; that is, red, instead of occupying the position at one of the angles of an equilateral triangle, will be moved up toward the centre to R' . White will also be shifted from W to w , and the white of a person thus affected would appear to the normal eye of a somewhat greenish-blue hue. Between D and R' lie, so to speak, mixtures of red with darkness, and along the line $R'G$ will be various mixtures of red and green, in which, according to a normal eye, the green element quite predominates; that is to say, their orange is more

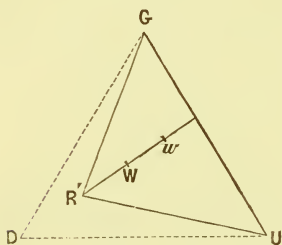


FIG. 34.—Newton's Diagram for a Person partially Colour-blind to Red.

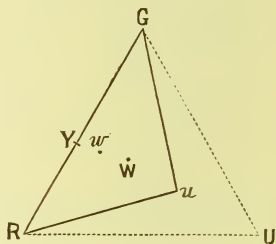


FIG. 35.—Newton's Diagram for Lamp-light Illumination.

like our yellow, their yellow like our greenish yellow, etc. Along the line $R'U$ will be their mixtures of red and blue, or a series of purples, which will be more bluish than ours.

The condition of the normal eye by lamp-light is shown in Fig. 35. The blue or violet is moved from U , its position by daylight, up to u ; white is moved from W to w —that is, into a region that would be called by daylight yellow. Yellow itself, Y , is not far from this new representative of white, and consequently by candle-light appears always whitish. In the purples, along the line Ru , the red element predominates; and in the mixtures of green and blue, along the line $G u$, the green constituent has the upper hand.

If we were colour-blind to every kind of light except red, then the colour diagram would assume a form similar to that shown in Fig. 36, D representing the darkest red perceptible to eyes so constituted. This sensation would be brought about by pure feeble red

light, or by a mixture of intense green and blue light, or by either of the latter. As we advance from D toward R, the red light gains in brightness, and out at *w* becomes very bright and stands for white. When a red glass is held before the eyes, something approximating to this kind of vision is produced.

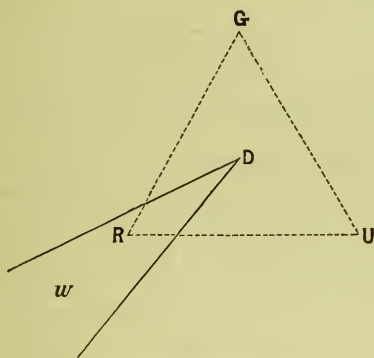


FIG. 36.—Newton's Diagram for Persons Colour-blind to Green and Violet.

CHAPTER IX.

THE COLOUR THEORY OF YOUNG AND HELMHOLTZ.

IT is well known to painters that approximate representations of all colours can be produced by the use of very few pigments. Three pigments or coloured powders will suffice, a red, yellow, and a blue ; for example, crimson-lake, gamboge, and Prussian blue. The red and yellow mingled in various proportions will furnish different shades of orange and orange-yellow ; the blue and yellow will give a great variety of greens ; the red and blue all the purple and violet hues. There have been instances of painters in water-colours who used only these three pigments, adding lampblack for the purpose of darkening them and obtaining the browns and greys. Now, though it is not possible in this way to obtain as brilliant representatives of the hues of nature as with a less economical palette, yet substitutes of a more or less satisfactory character can actually be produced in this manner. These facts have been known to painters from the earliest ages, and furnished the foundation for the so-called theory of three primary colours, red, yellow, and blue. The most distinguished defender in modern times of this theory was Sir David Brewster, so justly celebrated for his many and brilliant optical discoveries. He maintained that there were three original or fundamental kinds of light, red, yellow, and blue, and that by their mixture in various proportions all other kinds of coloured light were produced, in the manner just described for pigments. Brewster in fact thought he had demonstrated

the existence in the spectrum itself of these three sets of fundamental rays, as well as the absence of all others ; and his great reputation induced most physicists for more than twenty years to adopt this view, Airy, Melloni, and Draper alone dissenting. This theory of the existence of three fundamental kinds of light, red, yellow, and blue, is found in all except the most recent text books on physics, and is almost universally believed by artists. Nevertheless, it will not be difficult to show that it is quite without foundation. If we look at the matter from a theoretical point of view, we reach at once the conclusion that it can not be true, because outside of ourselves there is no such thing as colour, which is a mere sensation that varies with the length of the wave producing it. Outside of and apart from ourselves, light consists only of waves, long and short—in fact, of mere mechanical movements ; so that Brewster's theory would imply that there were in the spectrum only three sets of waves having three different lengths, which we know is not the case. If we take up the matter experimentally, we meet with no better result. According to the theory now under consideration, green light is produced by mixing blue and yellow light. This point can be tested

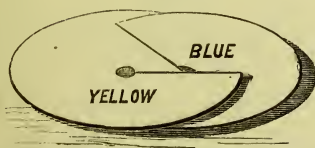


FIG. 37.—Maxwell's Disks. Blue and Yellow Disks in the Act of being combined.

with Maxwell's coloured disks. A circular disk, painted with chrome-yellow and provided with a radial slit, is to be combined with one prepared in the same way and painted with ultramarine-blue. Fig. 37 shows the separate disks, and in Fig. 38 they are seen in combination. If the compound disk be now set in quite rapid rotation, the two kinds

of coloured light will be mingled, and the resultant tint can be studied. It will not be green, but yellowish grey or

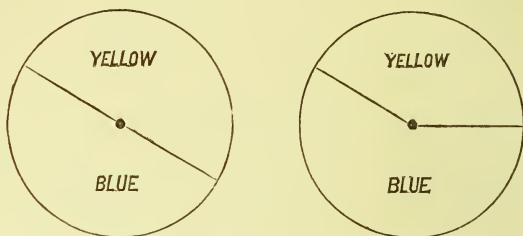


FIG. 88.—Blue and Yellow Disks in Combination.

reddish grey, according to the proportions of the two colours. These disks of Maxwell are ingeniously contrived so as to allow the experimenter to mingle the two colours in

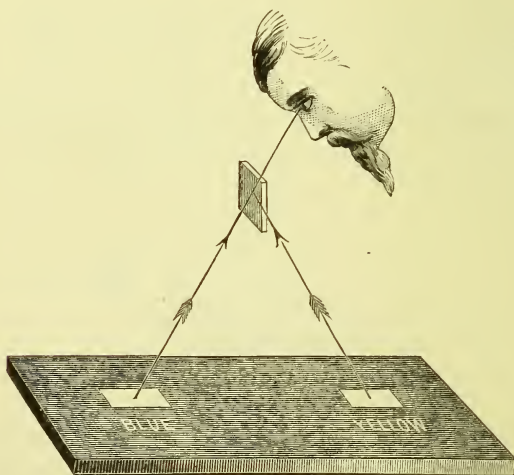


FIG. 89.—Apparatus of Lambert for mixing Coloured Light.

any desired proportion ; but, vary the proportions as we may, it is impossible to obtain a resultant green hue, or in-

deed anything approaching it. Another way of making this experiment is simply to use a fragment of window-glass of good quality, as was done by Lambert and Helmholtz. This apparatus is shown in Fig. 39. The glass is supported in a vertical position about ten inches above a board painted black, and on either side of it are placed the coloured papers. The blue paper is seen directly through the glass, while the light from the yellow paper is first reflected from the glass and then reaches the eye. The result is that the two images are seen superimposed, as is indicated in Fig. 40. The relative luminosity or brightness of the two im-

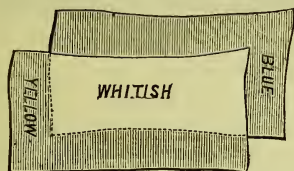


FIG. 40.—Result furnished by the Apparatus.

ages can be varied at will ; for instance, moving the papers further apart causes the blue to predominate, and bringing them nearer together produces the reverse effect. In this manner the resultant tint may be made to run through a variety of changes, which will entirely correspond to those obtained with the two circular disks ; but, as before, no tendency to green is observed. Helmholtz has pushed this matter still further, and has studied the resultant hues produced by combining together the pure colours of the spectrum. The following experiment, which is easy to make, will give an idea of the mode of proceeding : A blackened screen of pasteboard is pierced with two narrow slits, arranged like those in Fig. 41. The light from a window is allowed to shine through the two slits and to fall on a prism of glass placed just before the eye, and distant from the slits about a metre. Then, as would be expected, each slit

furnishes a prismatic spectrum, and owing to the disposition of the slits, the two spectra will overlap as shown in Fig. 42, which represents the red space of one spectrum falling

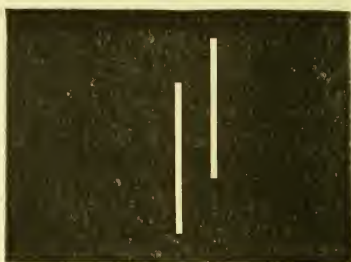


FIG. 41.—Two Slits arranged for mixing Two Spectra.

on the green space of its companion. By moving the slits further apart or nearer together, all the different kinds of light which the spectrum contains may thus be mingled. Using a more refined apparatus, Helmholtz proved that the union of the pure blue with the pure yellow light of the spectrum produced in the eye the sensation, not of green, but of white light. Other highly interesting results were also obtained by him during this investigation; these will be

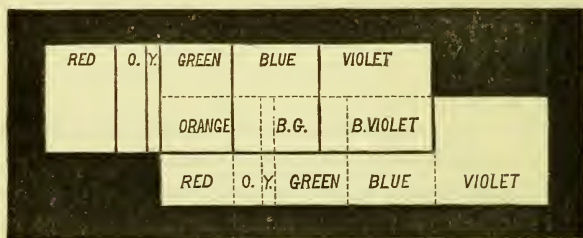


FIG. 42.—Two Overlapping Spectra. Red and Green are mixed, also Violet and Blue, etc.

considered in the following chapter, but in the mean while it is evident that this total failure of blue and yellow light to produce by their mixture green light is necessarily fatal

to the hypothesis of Brewster. Helmholtz also studied the nature of the appearances which misled the great English optician, and showed that they were due to the fact that he had employed an impure spectrum, or one not entirely free from stray white light.

As has been remarked above, there can be in an objective sense no such thing as three fundamental colours, or three primary kinds of coloured light. In a totally different sense, however, something of this kind is not only possible, but, as the recent advances of science show, highly probable. We have already seen in a previous chapter that in the solar spectrum the eye can distinguish no less than a thousand different tints. Every small, minute, almost invisible portion of the retina of the eye possesses this power, which leads us to ask whether each atom of the retina is supplied with an immense number of nerve fibrils for the reception and conveyance of this vast number of sensations. The celebrated Thomas Young adopted another view: according to him, each minute elementary portion of the retina is capable of receiving and transmitting three different sensations; or we may say that each elementary portion of its surface is supplied with three nerve fibrils, adapted for the reception of three sensations. One set of these nerves is strongly acted on by long waves of light, and produces the sensation we call red; another set responds most powerfully to waves of medium length, producing the sensation which we call green; and finally, the third set is strongly stimulated by short waves, and generates the sensation known as violet. The red of the spectrum, then, acts powerfully on the first set of these nerves; but, according to Young's theory, it also acts on the two other sets, but with less energy. The same is true of the green and violet rays of the spectrum: they each act on all three sets of nerves, but most powerfully on those especially designed for their reception. All this will be better understood by the aid of the accompanying diagram, which is

taken from Helmholtz's great work on "Physiological Optics." In Fig. 43, along the horizontal lines 1, 2, 3 are

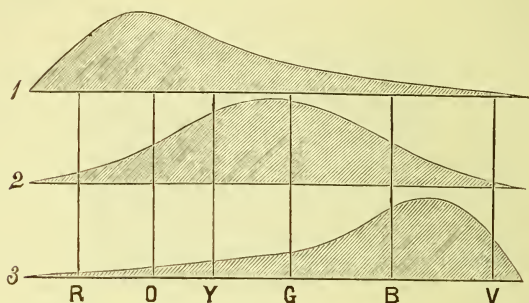


FIG. 43.—Curves showing the Action of the Different Colours of the Spectrum on the Three Sets of Nerve Fibrils. (Helmholtz.)

placed the colours of the spectrum properly arranged, and the curves above them indicate the degree to which the three kinds of nerves are acted on by these colours. Thus we see that nerves of the first kind are powerfully stimulated by red light, are much less affected by yellow, still less by green, and very little by violet light. Nerves of the second kind are much affected by green light, less by yellow and blue, and still less by red and violet. The third kind of nerves answer readily to violet light, and are successively less affected by other kinds of light in the following order: blue, green, yellow, orange, red. The next point in the theory is that, if all three sets of nerves are simultaneously stimulated to about the same degree, the sensation which we call white will be produced. These are the main points of Young's theory, which was published as long ago as 1802, and more fully in 1807. Attention has within the last few years been called to it by Helmholtz, and it is mainly owing to his labours and those of Maxwell that it now commands such respectful attention. Before making an examination of the evidence on which it rests,

and of its applications, it may be well to remember, as Helmholtz remarks, that the choice of these three particular colours, red, green, and violet, is somewhat arbitrary, and that any three could be chosen which when mixed together would furnish white light. If, however, the end and middle colours of the spectrum (red, violet, and green) are not selected, then one of the three must have two maxima, one in the red and the other in the violet; which is a more complicated, but not an impossible supposition. The only known method of deciding this point is by the investigation of those persons who are colour-blind. In the last chapter it was shown that the most common kind of this affection is colour-blindness to *red*, which indicates this colour as being one of the three fundamental sensations. But, if we adopt red as one of our three fundamental colours, of necessity the other two must be green and violet or blue-violet. Red, yellow, and blue, for example, will not produce white light when mingled together, nor will they under any circumstances furnish a green. Red, orange, and blue or violet would answer no better for a fundamental triad. In the preceding chapter it was also shown that colour-blindness to green exists to some extent, though by no means so commonly as the other case. Hence, thus far, the study of colour-blindness has furnished evidence in favour of the choice of Young, and its phenomena seem explicable by it.

Let us now examine the explanation which the theory of Young furnishes of the production of the following colour-sensations, which are not fundamental, viz. :

Orange-red.	Yellow.	Bluish-green.
Red-orange.	Greenish-yellow.	Cyan-blue.*
Orange-yellow.	Yellowish-green.	Ultramarine-blue.

Starting with yellow, we find that, according to the theory under consideration, it should be produced by the joint

* Cyan-blue is a greenish-blue.

stimulation of the red and green nerves ; consequently, if we present simultaneously to the eye red and green light, the sensation produced ought to be what we call yellow. This can be most perfectly accomplished by mixing the red and green light of the spectrum ; it is possible in this way to produce a fair yellow tint. The method of rotating disks furnishes, when emerald-green and vermilion are employed, a yellow which appears rather dull for two reasons : first, because the pigments which we call yellow, such as chrome-yellow or gamboge, are, as will hereafter be shown, relatively more brilliant and luminous than any of the red, green, blue, or violet pigments in use ; so that these bright-yellow pigments stand in a separate class by themselves. This circumstance influences our judgment, and, finding the resultant yellow far less brilliant than our (false) standard, chrome-yellow, we are disappointed. The second reason is, that green light stimulates, as before mentioned, the violet as well as the green nerves ; hence all three sets of nerves are set in action to a noticeable extent, and the sensation of yellow is mingled with that of white, and consequently is less intense than it otherwise would be. When the green and red of the spectrum are mingled, we have at least not to contend with a false standard, and only the second reason comes into play, and causes the yellow thus produced to look as though mingled with a certain quantity of white. It was found by the lamented J. J. Müller that green light when mingled with any other coloured light of the spectrum diminished its saturation, and caused it to look as though at the same time some white light had been added. This is what our fundamental diagram (Fig. 43) would lead us to expect ; it is quite in consonance with the theory of Young and Helmholtz.

Having now accounted for the fact that the yellow produced by mixing red and green light is not particularly brilliant, it will be easy to show how several of the other colour-sensations are generated. If, for instance, we dimin-

ish the intensity of the green light in the experiment above mentioned, the resultant hue will change from yellow to orange, red-orange, orange-red, and finally to pure red. These changes are best followed by using the coloured light of the spectrum, but may also be traced by the help of Maxwell's disks (Fig. 38), or by the aid of the glass plate of Helmholtz (Fig. 39). On the other hand, if, in the experiment now under consideration, the green light be made to preponderate, the resultant yellow hue will pass into greenish yellow, yellowish green, and finally green. This accounts for the production of more than half the colour-sensations in the list above given, and the remaining ones, such as ultramarine, cyan-blue, and bluish green, can be produced in the same way by mingling in proper proportions green and violet light, using any of the methods above mentioned.

In the cases thus far considered we have presented to the eye mixtures of two different kinds of coloured light, or, to speak more accurately, two kinds of light differing in wave-length ; it now remains for us to account for the production of colour-sensations in those cases where the eye is acted on only by one kind of coloured light, or by light having one wave-length. In the case of red, green, or violet light, the explanation of course lies on the surface : the red light stimulates powerfully the red nerves and produces the sensation we call red, and so of the others. But this does not quite exhaust the matter ; for, according to the theory of Young and Helmholtz, this same red light also acts to some extent on the green and violet nerves, and simultaneously produces to some small degree the sensations we call green and violet. The result then, according to the theory, ought to be the production of a strong red sensation, mingled with much weaker green and violet sensations ; or, in other words, even when the eye is acted on by the pure red light of the spectrum, this red light ought to appear as though mingled with a little white light, even if

none is actually present. Experiment confirms this theoretical conclusion, and here again decides in favour of the correctness of our theory. The simplest way of making the experiment would be to temporarily remove, were it possible, the green and violet nerves from a portion of the retina of the eye, and then to throw on the whole retina the pure red light of the spectrum. This red light ought then to appear more intense and saturated when falling on the spot from which the green and violet nerves had been removed than when received on the rest of the retina, where all three kinds of nerves were present. Now, though we can not actually remove the green and violet nerves from a spot in the retina, yet we can by suitable means tire them out, or temporarily exhaust them, so that they become to a considerable extent insensitive. If a small spot of the retina be exposed for a few moments to a mixture of green and violet light so combined as to appear bluish green, the green and violet nerves will actually become to a considerable extent inoperative; and, when the eye is suddenly turned to the red of the spectrum, this spot of the retina will, if we may use the expression, experience a more powerful and purer sensation of red than the surrounding unfatigued portions, where the red will look as if diluted with a certain amount of white light. From this experiment of Helmholtz it appears, then, that it is actually possible to produce by artificial means colour-sensations which are more powerful than those ordinarily generated by the light of the spectrum—a point to which we shall return in the following chapter.

Having accounted now for the production of the colour-sensations red, green, and violet by red, green, and violet light, and noticed an interesting peculiarity connected with this matter, we pass on to the others. Taking up the yellow of the spectrum, we find that it can be produced by the action on the eye of waves of light intermediate in length between those which give the sensations red and green.

These waves are too short to act very powerfully on the red nerves, and too long to set into maximum activity the green nerves, but they set both into moderate action ; the result of this joint action of the two sets is a new sensation, which we call yellow. Furthermore, it may be remarked that the waves of the light called yellow are far too long to produce any but a feeble effect on the violet nerves ; they affect them less than green light does. From this it results that the sensation of yellow, when directly produced by the yellow light of the spectrum, is less mingled with that of white, and is purer than is the case when it is brought about by mixing red light with green in the manner before described. And this explanation may serve to account for the fact that it is impossible, by mixtures of red and green light taken from the spectrum, to produce a yellow light as pure and brilliant as the yellow of the spectrum. Let us suppose, in the next place, that, instead of presenting to the eye the yellow of the spectrum, we act on it by the light belonging to one of the other spaces—the blue, for example. The explanation is almost identical with that just given for the yellow : the waves constituting blue light being too short to powerfully affect the green nerves, and too long to accomplish this with the violet nerves, both green and violet nerves are moderately affected, giving the sensation we call blue. Meanwhile the blue light produces very little action on the red nerves, and hence very little of the sensation of white is mingled with that of blue ; and consequently this blue hue is more saturated than when produced by the actual mixture of green and violet light. In fact, J. J. Müller found that green light, when mingled with light from any other part of the spectrum, produced a hue which was less saturated and more whitish than the corresponding tint in the spectrum which the mixture imitated. The production of all the other colour-sensations obtained by looking at the spectrum is explained in the same way by our theory. From all this one interesting

conclusion can be drawn, viz. : that there are two distinct ways of producing the same colour-sensation ; for we have seen that it may be accomplished either by presenting to the eye a mixture of green and violet light, or simply one kind of light, the waves of which are intermediate in length between those of green and violet. The eye is quite unable to detect this difference of origin, although a prism reveals it instantly.

Having examined thus, with a degree of detail which may have seemed tedious, the mode in which colour-sensations are accounted for by the theory of Young and Helmholtz, we pass to another point. In order to give more exactness to this theory, it is necessary to define with some degree of accuracy the three fundamental colours ; for there is a great variety of reds, greens, and violets. Helmholtz, as the result of his first investigation, selected a red not far from the end of the spectrum, a full green and violet ; in other words, the tints chosen were the middle and end colours of the spectrum. Maxwell, who made a series of beautiful researches on points connected with Young's theory, was led to adopt as the fundamental colours a red which in the spectrum lies between the fixed lines C and D, and is distant from C just one third of the distance between C and D. This is a scarlet-red with a tint of orange, and is represented by some varieties of vermilion. His green is situated between E and F, being distant from E by one quarter of the distance between E and F. This colour finds among pigments an approximate representative in emerald-green. Instead of adopting a full violet, Maxwell selected a violet-blue midway between the lines F and G, which is represented tolerably by artificial ultramarine-blue. By subjecting the results of experiments on the spectrum to calculation, it is possible to fix on the position of one of the fundamental colours, viz., the green. Thus Charles S. Pierce, using data given in Maxwell's paper, obtained for this colour a slightly different result from that just men-

tioned.* According to his calculations, the fundamental green has a wave-length of 524 ten-millionths of a millimetre, and is situated between the lines E and *b*, being one third of the distance E *b* from E, whereas Maxwell's green is just beyond *b*. J. J. Müller, who conducted an important investigation on this subject by a quite different method, arrived at a somewhat different result for the position of the green, and assigned to it a wave-length of 506·3 ten-millionths of a millimetre. This position in the spectrum is nearer the blue than the positions given by Maxwell and Pierce, and the tint is more of a bluish green. Again, von Bezold, basing his calculations on the experimental results of Helmholtz and J. J. Müller, reached a conclusion not differing much from those of Maxwell or Pierce. He selects a green in the *middle* of the normal spectrum between E and *b*, but nearer *b*. None of these results differ very greatly; in fact, the differences can hardly be well indicated in a spectrum of the size of this page. All these greens may be imitated by using the pigment known as emerald-green, alone or mixed either with a small quantity of chrome-yellow or cobalt-blue. Hence all these green hues are of the most powerful or, as artists would say, overpowering character.

The exact determination of the other two fundamental colours is a more difficult matter, so that even the advocates of Young's theory have not entirely agreed among themselves upon the exact colours, Maxwell taking ultramarine-blue, Helmholtz and J. J. Müller violet, as the third fundamental. These fundamental colours are among the most saturated and intense of those furnished by the spectrum. Compared with them, the blue of the spectrum is a feeble tint, so that it has often been remarked by Rutherford that, in comparison with the other colours, it appears of a slaty hue. The greenish yellow is also feeble; and, as is well

* "Proceedings of the American Academy of Arts and Sciences, 1873."

known, pure yellow is found in the spectrum in very small quantity and of no great intensity. The orange-yellow is also much weaker than the red, and the orange only becomes strong as it approaches redness in hue. From this it very naturally follows that, if a normal spectrum is cast on a white wall in a room not carefully darkened, scarcely more than the three fundamental colours will be discerned, red, green, and blue-violet; the other tints can with some difficulty be made out, but at first sight they strike the unprejudiced observer simply as the places where the three principal colours blend together. The representatives of the fundamentals among pigments are also those which surpass all others in strength and saturation. One of the fundamental colours, red, is used without much difficulty in painting and decoration; the other two are more difficult to manage, particularly the green. The last colour, even when subdued, is troublesome to handle in painting, and many artists avoid it as far as possible, or admit it into their work only in the form of low olive-greens of various shades. When the tint approaches the fundamental green, and is at the same time bright, it becomes at once harsh and brilliant, and the eye is instantly arrested by it in a disagreeable manner.

NOTE TO CHAPTER IX.

YOUNG does not appear to be the first who proposed red, green, and violet as the three fundamental colours. As far back as 1792 WÜNSCH was led to the same result by his experiments on mixtures of the coloured rays of the spectrum. The title of his work is "*Versuche und Beobachtungen über die Farben des Lichtes*" (Leipsic, 1792). An abstract of the contents is contained in the "*Annales de Chimie*," LXIV., 135.

A. M. MAYER has recently called attention to the way in which Young was led to adopt red, green, and violet as the three fundamental colours, and has shown that Young at first "selected red,

yellow, and blue as the three simple colour-sensations; second, that he subsequently modified his hypothesis, and adopted red, green, and violet as the three elementary colour-sensations, showing that up to the date of this change of opinion all of his ideas on the subject were hypothetical, and not based on any observations of his own or others; third, that this change of opinion as to the three elementary colours was made on the basis of a misconception by Wollaston of the nature of his celebrated observation of the dark lines in the solar spectrum, and also on the basis of an erroneous observation made by Young in repeating Wollaston's experiment; fourth, that Young subsequently tested his hypothesis of colour-sensation, and found that it was in accord with facts reached by experiment, and that these experiments then vindicated his hypothesis and raised it to the dignity of a theory." ("American Journal of Science and Arts," April, 1875.)

Fig. 43 (page 114) shows the intensities of the three primary sensations, red, green, and violet, as *estimated* by Helmholtz. The intensities were afterward measured by Maxwell, and found to differ slightly in the case of different eyes. In Fig. 44 the letters C D E F G denote the fixed lines of the solar spectrum; the curve R R R, the

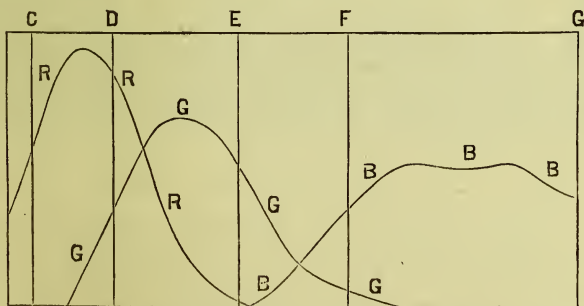


FIG. 44.—Curves showing the Intensity of the Fundamental Sensations in Different Parts of the Solar Spectrum. (Maxwell.)

intensity of the sensation of red in different parts of the spectrum; G G G is the curve for the green, and B B B that for the violet-blue sensation. Fig. 31 (page 104) shows the same curves as obtained by another observer. ("Philosophical Transactions" for 1860, vol. cl.)

CHAPTER X.

ON THE MIXTURE OF COLOURS.

THOSE who watch a painter at work are astonished at the vast number and variety of tints which can be made by mixing in varying proportions a very few pigments : from red and yellow there is produced a great series of orange tints ; yellow and blue furnish a multitude of green hues ; blue and red, a series of purples. The results seem almost magical, and we justly admire the skill and knowledge which enable him in a few seconds accurately to match any colour which is within the compass of his palette. As we continue our observations we soon find that the matter is more complicated than it appeared at first sight, each pigment having a particular set of properties which it carries into its mixtures, and these properties being by no means fully indicated by its mere colour. Thus, some blue pigments furnish fine sets of greens, while others, as beautiful and intense, yield only dull olive-greens ; some reds give glowing purples, while from others not less bright it is possible to obtain only dull, slaty purples. Before touching on these complicated cases it will be well to study this subject under its simplest aspects, and to content ourselves for the present with making an examination of the effects which are produced by mixing *light* of different colours. This can not be brought about by mixing pigments, as was for a long time supposed. In some cases the mixture of pigments gives results more or less like those produced by

the mixture of coloured light, but as a general thing they differ, and in some cases the difference is enormous. In the previous chapter, for instance, it was shown that while the mixture of yellow with blue pigments produced invariably a green hue of varying intensity, the mixture of blue with yellow light gave a more or less pure white, but under no circumstances anything approaching green. The mixture of two masses of coloured light can easily be effected in a simple manner so as to be exhibited readily to a large audience. Two magic lanterns are to be employed, as shown in Fig. 45, the usual slides being replaced by plates

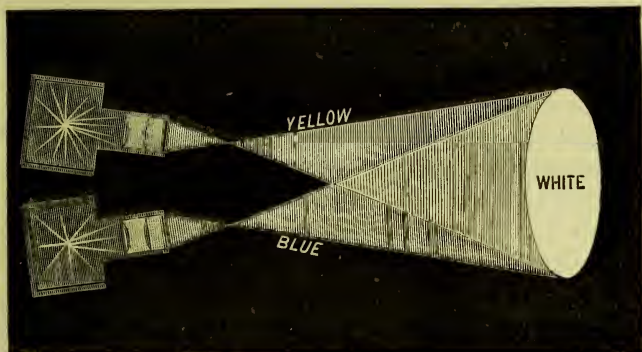


FIG. 45.—Two Magic Lanterns casting Yellow and Blue Light on the same Screen, where it forms White.

of coloured glass, as indicated. Each lantern then will furnish a large bright circle of coloured light, which can be projected on a white screen, the room in which the experiments are made being first darkened. In this way it will be found that violet-blue light when mixed with green light gives blue or greenish-blue light, according to the proportions of the two constituents; green with red gives various hues of orange or whitish yellow, instead of a set of dull, indescribable shades of greenish, reddish, or brownish grey, as is the case with pigments. These and many

other beautiful experiments on the mixture of coloured light can easily be made ; and even the effects produced by varying the intensity of either of the masses of coloured light can readily be studied by gradually diminishing the brightness of one of the coloured circles, the other remaining constant.

To all these experiments it may be objected that we are not using coloured light of sufficient purity ; that our yellow glass transmits, as was shown in Chapter VII., not only yellow but red, orange, and green light ; and that the other stained glasses are not much better off in this respect. Hence, to meet all such objections, physicists have been finally obliged to conduct their researches in this direction on the pure coloured rays of the spectrum. The difficulties encountered in the use of this method are much greater, but the results so obtained are far more precious. Very beautiful investigations of this character have been made by Helmholtz, Maxwell, and J. J. Müller. The general character of their results is something like this : By mixing two kinds of pure coloured light they obtained, as a general thing, light having a colour different from either of the original ingredients ; for example, red and yellowish green gave an orange hue which looked in all respects like the pure orange of the spectrum ; also, in this new orange it was impossible by the *eye* to detect the presence of either red or yellowish-green light. This was true of all mixtures ; in no case could the original ingredients be detected by the eye. In this respect the eye differs from the ear ; for by practice it is possible with the unaided ear to analyze up compound sounds into the elements which compose them, at least to some extent. It was also ascertained that the same colour could be produced in several different ways—that is, by combining together different pairs of spectral colours. Thus, violet with cyan-blue gave an ultramarine hue, but violet gave the same colour when mixed with bluish-green, or even with green ; in the last case the tint

was somewhat whitish. By mixing certain colours of the spectrum, it was found that one new colour or colour-sensation could be produced which originally was not furnished by the plain pure spectrum itself; we refer to purple, or rather to the whole class of purples, ranging from violet-purple to red-purple. These are produced by mixing the end colours of the spectrum, red and violet, in varying proportions. Furthermore, mixtures of certain colours of the spectrum gave rise to white; this was true, for example, of red and bluish-green, and of yellow and ultramarine-blue. The white in these two cases, though so different in origin, had exactly the same appearance to the eye. Again, by mixing three or more spectral colours no new hues were produced, but simply varieties of those which could be obtained from two colours.

Such is the general character of the results obtained by mixing together masses of pure coloured light; we propose now to enter a little more into detail respecting this very interesting matter, and to examine the laws which control the production of the resultant hues.

It was ascertained by Müller, who worked under the direction

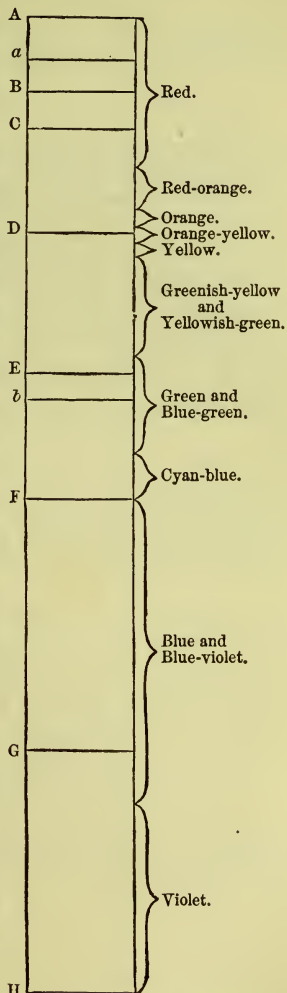


FIG. 46.—Prismatic Spectrum.

of Helmholtz, that all the colours of the spectrum, Fig. 46, from red to yellowish-green, gave by mixture resultant hues which were always identical with some of the colours situated between red and yellowish-green, thus :

TABLE I.

Red and yellowish-green gave.....	Orange or yellow.*
Red and yellow gave.....	Orange.
Orange and yellowish-green gave.....	Yellow.

The effect of the mixture in these cases was to produce colours which were, to all appearance, as pure as the corresponding colours of the spectrum itself.

Furthermore, all colours of the spectrum from violet to bluish-green furnished mixtures corresponding to the colours contained between these limits, thus :

TABLE II.

Bluish-green and ultramarine-blue gave...	Cyan-blue.
Bluish-green and violet gave.....	Cyan-blue or ultramarine-blue.*
Violet and cyan-blue gave.....	Ultramarine-blue.

In these cases also the resulting tints could not be distinguished from the corresponding spectral colours. The results thus far are simple in character, and easily remembered by any one who recollects the arrangement of the colours of the spectrum.

On the other hand, *green*, when mixed with any colour of the spectrum, gave a resultant colour, which was less saturated or intense, and appeared more whitish, than the corresponding spectral tint, thus :

TABLE III.

Green and red gave.....	$\left. \begin{array}{l} \text{Orange,} \\ \text{Yellow,} \\ \text{Yellowish-green,} \end{array} \right\} \text{whitish.}$
-------------------------	--

* According to the proportions.

Green and yellow gave.....	Yellowish-green—whitish.
Green and cyan-blue gave.....	Bluish-green—whitish.
Green and violet gave.....	{ Ultramarine-blue, Cyan-blue, Bluish-green, } whitish.
Yellowish-green and bluish-green gave.....	Green—very whitish.

Müller made a careful determination of the position in the spectrum of the green which had the greatest effect in diminishing the saturation, and consequently was most influential in generating pale or whitish tints. It was situated between the fixed lines *b* and *F*, at one third the distance between *b* and *F*, measured from *b*. This colour is a bluish-green, and can be imitated by mixing emerald-green with a small quantity of cobalt-blue. According to Müller, as already stated, this is the fundamental green: its wavelength is 506·3 ten-millionths of a millimetre.

Having considered the effects produced by mixing the colours of the spectrum situated on either side of the green, and also the effects produced by green itself in mixture, it remains to examine the mixtures of the colours located right and left of green, thus:

TABLE IV.

Red and ultramarine-blue gave...	Violet—slightly whitish.
Red and cyan-blue gave.....	Ultramarine or violet—whitish.
Orange and violet gave.....	Red—whitish.
Red and violet gave.....	Purple—whitish.
Orange and ultramarine gave....	Purple—whitish.

These results may at first sight not seem as simple and obvious as those mentioned above, but, when the arrangement of the colour-diagram* has been explained, it will be seen that they are strictly analogous to the cases before given.

It may have been noticed by the reader that the series of pairs given in the tables thus far do not entirely exhaust

* See Chapter XIV.

all possible combinations of the spectral colours. In the cases which remain, however, the effect of mixture is not the production of coloured but of white light, thus :

TABLE V.

Red and bluish-green * gave.....	White.
Orange and cyan-blue gave.....	White.
Yellow and ultramarine gave.....	White.
Greenish-yellow and violet gave.....	White.

Hence these are called complementary colours, and, on account of their importance, a separate chapter will be devoted to them. Green finds no simple complementary colour in the spectrum ; it requires a mixture of red and violet, or the colour called purple.

These experiments, as will be easily understood, have furnished us with a great deal of valuable information, which could not have been derived by studying the mixtures of pigments on the painter's palette. They supply us with material which can be used in unraveling many colour-problems, presented by nature or art, which otherwise would be quite beyond our grasp. The experiments themselves unfortunately are quite difficult, and for their proper execution require knowledge and skill as well as much patience. There is, however, another method of mixing coloured light to which no such objections apply, for it is simple and quite within the reach of all who are interested in this subject. We refer to the method of rotating disks which has already once or twice been mentioned.† If a disk of cardboard be painted, as indicated in Fig. 47, with vermilion and a bluish-green pigment, and then set in rapid rotation, these colours will be mixed (in the eye of the observer), and the whole disk will assume a new and uniform tint, which will be that due to a mixture of the coloured light sent out from the two halves of the disk (Fig. 48). When

* Or rather green-blue.

† See Chapter IX.

we analyze this experiment, we find that what actually does take place is this : At any one particular instant a certain portion of the retina of the eye will be affected with red light ; the disk then turns and presents to the same portion of the retina bluish-green light ; then follows red, then bluish-green, etc. Hence the retina is really acted on by alternate presentations of the two masses of coloured light, the intervals between these substitutions being something less than one fiftieth of a second. Now, it so happens that these alternate presentations have the same effect on the eye as simultaneous presentations. This is not the least valuable result of the spectral experiments above described,

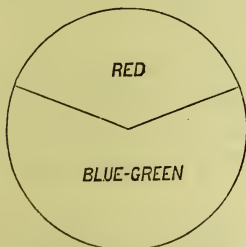


FIG. 47.—Disk painted with Vermilion and Blue-green.



FIG. 48.—Appearance presented by Red and Blue-green Disk when in Rapid Rotation.

for it enables us by an easy method to pursue our colour-investigations without having direct recourse to the spectrum. There is one respect in which the mixture by rotating disks actually does differ from that where the presentation is simultaneous. If we simultaneously present to the eye two masses of coloured light, it is plain that the luminosity of the mixture will be equal to the sum of the luminosities of the two components (or at least must approximate to it) ; thus, if the luminosity of our red light be 25, and that of our greenish-blue 30, the luminosity of the tint of mixture will be 55. If, however, these two masses of light act on the eye alternately, as is the case with rotating

disks, the luminosity of the mixture-tint will be not the sum but the mean of the separate luminosities ; that is, $27\frac{1}{2}$.*

This method of mixing colours was mentioned in the second century, in the "Optics" of Ptolemy.† It was

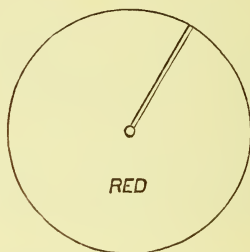
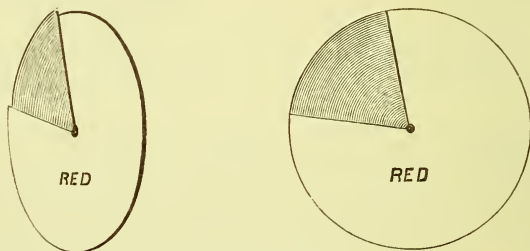


FIG. 49.—One of Maxwell's Disks.

rediscovered by Musschenbroek in 1762, and finally greatly improved by Maxwell. The last-named physicist modified the disks, so that it became possible easily to mix the colours in any desired proportion. This important improve-



FIGS. 50 and 51.—Two Views of a Pair of Maxwell's Disks in Combination.

ment is effected simply by cutting a slit through the disk from the centre to the circumference, as indicated in Fig. 49. The slit enables the experimenter to combine two or even more disks on the same axis, and to adjust them so

* Compare the results obtained by the author and given in Chapter III.

† "Bibliographie Analytique," by J. Plateau (1877).

that they present their respective surfaces in any desired proportion. (See Figs. 50 and 51.) The relative proportions of the two colours can then be obtained, as was done by Maxwell, by placing a graduated circle around the disks. The author finds it better to apply a graduated circle of pasteboard to the face of the disk, this circle being made a little smaller than the disk itself; the centring is insured by its contact with the axis on which the disk is fastened. (See Fig. 52.) Maxwell divided his circle into

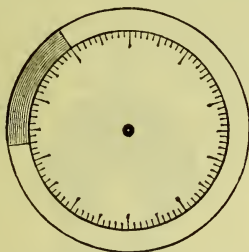


FIG. 52.—Mode of measuring the Colours on the Disks.

100 instead of 360 parts; this is convenient, and tenths of a division can readily be estimated by the eye. There is another very important feature connected with Maxwell's disks: they can easily be arranged so as to furnish colour-equations, which are of great use in chromatic studies. For example, returning to our compound disk of red and bluish-green, and remembering that these colours are complementary, it is evident that, if we give to the red and bluish-green surfaces the proper proportions, we can from them produce white, or, what is the same thing, a pure grey. But a pure grey can also be produced by rotating a white and black disk similarly arranged. Hence, in an experiment of this kind, we place on the axis, first, the disks of vermilion and bluish-green, and then on the same axis smaller disks of black and white pasteboard, cut in a similar manner with radial slits. By repeated trials we can

arrange the coloured disks so that they furnish a grey as neutral and pure as that due to the black and white disks ; and these last can be arranged so that the grey furnished by them is as *luminous* as that given by the other two. In an experiment of this kind it was found that to produce a pure grey it was necessary to take 36 parts of vermilion and 64 parts of bluish-green. This grey was in all respects exactly matched by 21·3 parts of white and 78·7 parts of black. The disk when stationary presented the appearance indicated in Fig. 53 ; when in rotation, that of a pure, uni-

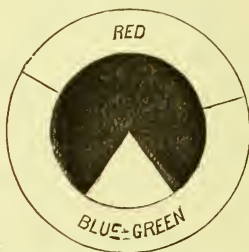


FIG. 53.—Large Disk of Red and Blue-green arranged for the Production of a Pure Grey, Small Disk of Black and White furnishes the same Grey.

form grey. All this can be put in the form of an equation by writing $36 \text{ red} + 64 \text{ blue-green} = 21\cdot3 \text{ white} + 78\cdot7 \text{ black}$. We have here expressed the proportions in which it is necessary to take these particular colours for the production of a grey ; the luminosity of this grey is also expressed in terms of black and white paper. According to our equation, if we set the luminosity of white paper equal to 100 and that of black paper equal to nothing, then the luminosity of the grey will be equal to 21·3 per cent. of that of white paper. It is not strictly true that the luminosity of black paper is equal to nothing, or that it reflects no light at all. Some careful experiments were made by the author on this point, and the following result reached : If black pasteboard is prepared by painting its surface with lamp-

black in powder to which just enough spirit varnish has been added to cause it to adhere closely, but not to shine, then a uniform surface will be obtained, which reflects a small but definite amount of the light falling on it. If, as before, we set the luminosity of white pasteboard as 100, then that of this kind of black paper will be 5.2; or, in other words, it reflects about five per cent. as much light as white pasteboard. This knowledge enables us to correct the equation just given; instead of 21.3 white, we should write 25.4.

In the above example we have taken the case of two complementary colours, and have obtained a measure for the white or grey light which they furnish by mixture;

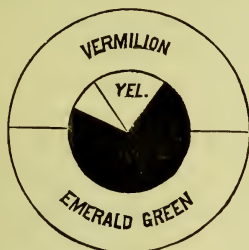


FIG. 54.—Vermilion and Emerald-green Disks arranged to produce a Yellow by Rotation. This yellow is imitated by small chrome-yellow, black, and white disks, as arranged in the figure.

when the resultant tint is not grey, but some decided colour, we can in a similar way assign to it a numerical value. Take the case of vermilion and emerald-green: Disks painted with these colours can be made to furnish a whitish yellow, as demanded by Young's theory, and we can express the value of this yellow in terms of chrome-yellow; that is, by darkening chrome-yellow and rendering it pale. This we accomplish by combining chrome-yellow with a black and a white disk. As the result of an experiment of this kind, the author obtained the equation: Verm. 51 + em.-green 49 = ch.-yel. 20 + white 8 + black 72.

The compound disk properly arranged is seen in Fig. 54. The reader may be somewhat surprised to notice that it was necessary to dull the chrome-yellow so greatly before making it similar in colour to the yellow produced by mixing the green and red light ; it must, however, be remembered that chrome-yellow does not quite belong to the same set of colours of which vermilion and emerald-green are members ; that is to say, if we represented the red space of a normal spectrum with vermilion, and the green space with emerald-green, then chrome-yellow would be too bright or luminous for the yellow space, and we should have to substitute for it a less brilliant yellow pigment.

In the same manner, with the aid of properly painted disks, we can make a series of experiments on the mixture of other colours, and satisfy ourselves of the correctness of the results already given in this chapter. For instance, by combining a yellow with a vermilion disk in various proportions, we obtain a series of orange or orange-yellow hues, which are as saturated in appearance as the original constituents. Red lead with a yellowish-green disk gave a fair yellow, and the same yellowish-green disk when combined with vermilion furnished a fine orange or yellow, according to the proportions. These correspond to the results given in Table I. In the same way those contained in the other tables can be verified. Naturally, some care must be exercised in the selection of the pigments with which the disks are painted ; thus, the author finds that the pure red of the spectrum can be imitated by vermilion washed over with carmine. Vermilion itself corresponds to the red space of the spectrum about half way between C and D ; red lead answers for a red-orange situated nearer still to D, etc. The parts of the spectrum which these and other pigments represent are indicated in Chapter III., to which the reader is referred for further information.

In preparing a set of disks for accurate experiments, it will be necessary of course to compare their colours care-

fully with those regions of the spectrum which they are intended to represent. This can be done with the aid of the spectroscop in the method indicated in Chapter III. A set of disks with carefully determined colours is quite valuable, not only for experiments of this kind, but also to enable us to produce a vast variety of tints at will, which can be recorded and afterward accurately reproduced when necessary.

We pass on now to the description of a beautiful and simple piece of apparatus contrived by Dove, for mixing the coloured light furnished by stained glass, and called by him a dichroöscope. This consists of a box 81 millimetres long, 75 high, and 70 broad; three sides are open, but can be closed by opaque slides or by plates of coloured glass. (See Fig. 55, which shows the box in perspective.) Fig. 56

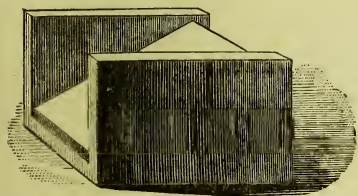


FIG. 55.—The Box of Dove's Dichroöscope. The plates of coloured glass are removed and the three sides left open. The six plates of window-glass are shown.

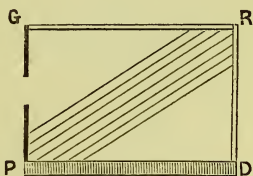


FIG. 56.—The Dichroöscope shown in section.

is a vertical section, in which GR and RD are plates of coloured glass; GP is an opaque slide made of blackened cardboard, in which a square aperture has been cut; PR represents a set of six glass plates made from window-glass of the best quality; these are of course colourless. At SS, Fig. 57, is a silvered mirror, and at N a Nicol's prism. The action of the apparatus is as follows: Let us suppose that GR is a plate of green glass, and RD one of red; then the light from the sky, striking on the mirror SS, is reflected through RD and the plates PR, and

finally reaches the eye ; it will of course be coloured red. But light from the sky also falls on the plate of green glass, G R, penetrates it, is reflected from the glass plates at P R, and also reaches the eye. The eye, then, will be simultaneously acted on by red and green light ; and, if the Nicol's prism at N be removed, this mixture will be seen, but we shall have no means of regulating the proportions of the red and green light. But, by restoring the Nicol's prism to its place, and rotating it, it is possible to mix the red and green light in any desired proportion.* When the appa-

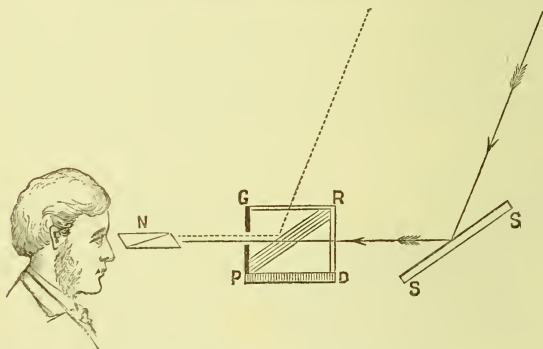


FIG. 57.—The Dichroscope as arranged for use.

ratus is provided with red and green glass as above indicated, a dull yellow will sometimes be given without the use of the Nicol's prism ; with its aid, this can always be accomplished ; the yellow will pass into greenish-yellow or orange, according as the proportions of the two constituents are varied. It is best to employ glasses the tint of which is not too dark, as we do not readily recognize dark yellow as such. The author easily obtained pieces of green

* Many beautiful experiments with polarized light can be made with this little apparatus ; for an account of them the reader is referred to Pogendorff's "Annalen," ex., p. 265, or to the "American Journal of Science," vol. xxxi., January, 1861.

and purple glass which gave pure white ; yellow and blue glass also did the same. If the hue of the yellow glass was too deep, the white was always tinged pinkish. Red and yellow gave orange ; green and yellow, yellowish-green ; red and blue, purple. All these results are quite in accordance with those obtained by mixing the coloured light of the spectrum.

In the previous chapter we have described a method which was contrived long ago by Lambert for mixing the coloured light from painted surfaces (see Fig. 39, page 110). The light from the blue paper is transmitted directly to the eye, and that from the yellow paper reaches the eye after reflection ; their action is of course simultaneous. By moving the two pieces of paper nearer together or farther apart, it is possible to vary their apparent brightness, and thus to regulate the proportion of blue and yellow light which reaches the eye ; the yellow will predominate when the papers are near together, the blue as they are moved further apart. Chrome-yellow (the pale variety) and ultramarine-blue, when combined in this apparatus, give an excellent white, and emerald-green and vermilion give a yellowish or orange tint, according to the arrangement. It is difficult to obtain a good representative of violet among the pigments in use by artists ; the author finds that some samples of the aniline colour known as " Hoffmann's violet B B " answer better than any of the ordinary pigments. If a deep tint of its alcoholic solution be spread over paper, and combined in the instrument with emerald-green, a blue, a greenish-blue, or a violet-blue can readily be produced. It is evident that a multitude of experiments of this character can be made, the number of colours united at one time being limited to two. The results of course agree with Young's theory.

Another method of mixing coloured light seems to have been first definitely contrived by Mile in 1839, though it had been in practical use by artists a long time previously.

We refer to the custom of placing a quantity of small dots of two colours very near each other, and allowing them to be blended by the eye placed at the proper distance. Mile traced fine lines of colour parallel to each other, the tints being alternated. The results obtained in this way are true mixtures of coloured light, and correspond to those above given. For instance, lines of cobalt-blue and chrome-yellow give a white or yellowish-white, but no trace of green ; emerald-green and vermilion furnish when treated in this way a dull yellow ; ultramarine and vermilion, a rich red-purple, etc. This method is almost the only practical one at the disposal of the artist whereby he can actually mix, not pigments, but masses of coloured light. In this connection we are reminded of an interesting opinion of Ruskin which has some bearing on our subject. The author of "Modern Painters," in his most admirable "Elements of Drawing," says : "Breaking one colour in small points through or over another is the most important of all processes in good modern oil and water-colour painting. . . . In distant effects of a rich subject, wood or rippled water or broken clouds, much may be done by touches or crumbling dashes of rather dry colour, with other colours afterward put cunningly into the interstices. . . . And note, in filling up minute interstices of this kind, that, if you want the colour you fill them with to show brightly, it is better to put a rather positive point of it, with a little white left beside or round it, in the interstice, than to put a pale tint of the colour over the whole interstice. Yellow or orange will hardly show, if pale, in small spaces ; but they show brightly in fine touches, however small, with white beside them."

This last method of mixing coloured light is one which often occurs in nature ; the tints of distant objects in a landscape are often blended in this way, and produce soft hues which were not originally present. Even near objects, if numerous and of small dimension, act in the same manner. Thus the colours of the scant herbage on a hillside

often mingle themselves in this way with the greenish-grey tints of the mosses and the brown hues of the dried leaves ; the reddish- or purplish-brown of the stems of small bushes unites at a little distance with their shaded green foliage ; and in numberless other instances, such as the upper and lower portions of mosses, sunlit and shaded grass-stalks, and the variegated patches of colour on rocks and trunks of trees, the same principle can be traced.

There is another mode of mingling coloured light, which is not much used by physicists, though it is of constant occurrence in nature. We refer to the case where two masses of coloured light fall simultaneously on the same object. Sunsets furnish the grandest examples of these effects, the objects in a landscape being at the same time illuminated by the blue sky and the orange or red rays of the sinking sun. Minor cases happen constantly ; among them the commonest is where a coloured object reflects light of its own tint on neighboring objects, thus modifying their hues and being in turn modified by them. The white or grey walls of a room are often very wonderfully tinted by coloured light which is cast on them in nebulous patches by the carpet, window-curtains, or other coloured objects that happen to be present. In all cases where the surface receiving the manifold illumination is white or grey, or but slightly coloured, the laws for the mixture of coloured light which have been explained above hold good ; when, however, this surface has a distinct colour of its own, the phenomena are modified in a manner which will presently be noticed.

We pass on now to compare the results which are obtained by mixing coloured *lights* with those which are given by the mixture of coloured *pigments*. It was for a long time supposed that these were identical, and that experiments on mixtures of coloured light could be made with the aid of the painter's palette. Lambert appears to have been the first to point out the fact that the results in

the two cases are not always identical. Thus the celebrated experiment of combining blue with yellow light, and obtaining not green but white, was first made by him with the apparatus shown in Fig. 39, page 110. The same fact was afterward independently discovered by Plateau, and finally by Helmholtz, who, using it as a starting-point, made an examination of the whole subject. When we study this matter with some attention, we find that in mixing pigments two different effects are produced. Suppose we mix chrome-yellow and ultramarine-blue, both in dry powder. If we rub this mixture on paper, we shall produce a uniform and rather dull green. An examination even with a moderately powerful microscope will fail to reveal the separate particles of the two pigments. Yet we know that there must be a superficial layer, made up of a mosaic work of blue and yellow particles placed side by side. These two sets of particles send light of their own colour to the eye, which there undergoes a true mixture, and gives as the resultant hue a yellowish-grey. Thus far the result entirely corresponds with that produced by mixing two masses of coloured light. The second and more important effect is brought about by light which penetrates two or more layers of particles. Here the light undergoes absorption in the manner explained in Chapter VII.: the yellow particles absorb the blue and violet; the blue particles, the red, orange, and yellow rays. The green light is absorbed also by both sets of particles, but not nearly so much as the other rays. From all this it follows that chrome-yellow and ultramarine-blue jointly absorb all the colours which are present in white light, except green; hence green light, as the result, is reflected back from the surface, and reaches the eye of the observer. This green light is finally mingled with the yellowish-grey light before mentioned. When dry pigments are employed, both of the effects just described are always present. If the pigments are used as water-colours, the light from the surface is diminished, and with

it the first of these effects ; and a still further diminution of it takes place if the pigments are ground up in oil. From all this it is evident that by *mingling two pigments* we obtain the resultant effect of two acts of absorption due to the two pigments : white light is twice subjected to the process of subtraction, and what remains over is the coloured light which finally emerges from the painted surface. On the other hand, the process of *mixing coloured light* is essentially one of addition ; and, this being so, we find it quite natural that the results given by these two methods should never be identical, and often should differ widely. From this it follows that painters can not in many cases directly apply knowledge acquired from the palette to the interpretation of chromatic effects produced by nature, for these latter often depend to a considerable extent on the



FIG. 58.—Two Apertures in Black Cardboard covered with Red and Green Glass (natural size.)

mixing of masses of differently coloured *light*. This fact is now admitted in a general way by intelligent artists, but probably few who have not made experiments in this direction fully realize how wide are the discrepancies which exist between the results given by the two different modes of mixture. A few years ago Dove described a method of studying this subject with the aid of stained glass ; and, as it would be difficult to devise a simpler or more striking mode of making such experiments, we will give his process in full.

In a blackened piece of cardboard two apertures are cut, about a third of an inch broad, as indicated in Fig. 58. Over these apertures are fastened pieces of stained glass—for instance, red and green; light from a white cloud is then made to traverse the glasses. At P, Fig. 59, is an

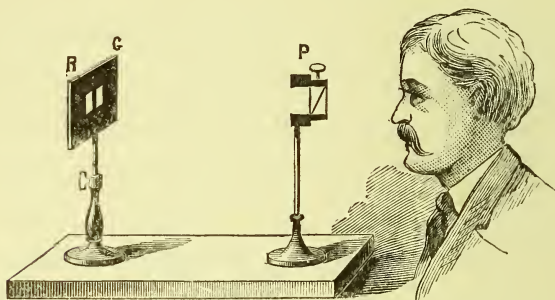


FIG. 59.—Mode of using Dove's Apparatus. R G is cardboard with red and green glass. at P is the prism of calc spar.

achromatic prism of calc spar, which doubles each of the little patches of coloured light, so that the observer on looking through the prism actually sees two red images of

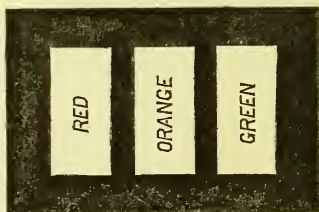


FIG. 60.—The Appearance presented when Red and Green Light are mixed by Dove's Apparatus.

exactly equal brightness, and also two similar green images. Now, by revolving the calc-spar prism the experimenter can cause one of the red images to overlap one of the green, and thus it is possible to mingle the red and green

light from the coloured glasses. In one experiment made by the present writer the colour of this mixture was orange (see Fig. 60). Upon removing the glasses from the instrument, placing them one over the other and allowing white light to pass through them, the effect due to the double absorption manifested itself; but now the colour of the transmitted light was not orange, or even brown, but dark green. If these two glasses had been ground to powder, mixed with oil, and then the mixture painted on canvas, it would have exhibited not an orange but a dark-green hue. We give below the results of a set of experiments which were recently made by the writer, and which illustrate the differences to be encountered in the two modes of proceeding:

RESULTS GIVEN BY DOVE'S APPARATUS.

Colours of Glass.	Result obtained by mixture of Light.	Result obtained by Absorption.
Red and green.....	Orange.	Dark green.
*Red and green.....	Pale yellow.	Black.
Yellow and blue.....	White.	Fine green.
*Yellow and blue.....	Pinkish-white.	Fine olive-green.
Red and blue.....	Violet-purple.	Deep red.
Yellow and dark purple...	Yellow.	Deep orange.
*Yellow and dark purple..	Pale orange.	Dark brown.
Purple and green.....	White.	Dark green.
Yellow and red.....	Yellow, slightly orange.	Deep orange-red.
*Yellow and red.....	Orange.	Red.
Yellow and bluish-green...	Yellow.	Yellowish-green.
*Yellow and blue-green...	Yellowish-white.	Rich yellowish-green.
**Yellow and blue-green..	Pale greenish-yellow.	Olive-green.
Purple and blue-green....	Pale blue-green.	Dark violet.
Purple-violet and green...	Pale violet-blue.	Black.

These are not experiments selected so as to show wide dif-

* Sample more deeply tinted.

ferences ; they comprise the entire set that was made on the occasion referred to, and are simply transcribed from the author's note-book. Yet it will be seen that in not a single case do the two methods furnish the same result ; and as a general thing they differ so entirely that it would be quite impossible even to predict the nature of one of the sets of tints from a knowledge of the other. These experiments, then, exhibit the wide difference between the effects produced by mixture of light and the absorption of light ; but, as has already been remarked, when pigments are mixed on the palette, the resultant hue depends partly on the process of true mixture and partly on that of absorption, the latter of course predominating. Hence the results in the table, though instructive, are not necessarily strictly applicable to the painter's palette, which is best studied by another method.

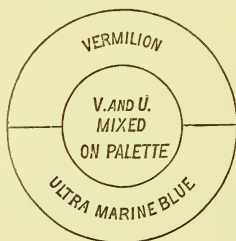


FIG. 61.—Disk for showing the Difference between mixing Coloured Light and Coloured Pigments. The outer disk is painted with the pure pigments, the small disk with a mixture of the same pigments.

For an examination of this matter the author adopted the following mode of proceeding : Two tolerably deep washes of water-colour pigments were prepared—for instance, vermilion and ultramarine-blue—with which two of Maxwell's disks were separately painted. Afterward an equal number of drops of the same washes were mingled on the palette, and a third and smaller disk painted with this mixture. The disks were placed on a rotation apparatus,

arranged as in Fig. 61, the vermilion and ultramarine covering each one half of the larger disk ; the smaller one, exhibiting the result furnished by the palette, being placed in the centre. When the compound disk was rotated, the colours of its outer portion underwent true mixture, and it was easy to compare the resultant tint with that furnished by the palette. In the experiment referred to the result was as follows : The larger disk became tinted red-purple, alongside of which the smaller disk seemed grey, so dull and inferior was its colour. The real colour of the smaller disk was a dull violet-purple. It will be noticed, then, that not only was the colour much darker and less saturated, but it had been moved from a red-purple to a violet-purple. Next, in order to ascertain how much the pigments had been darkened by mixture on the palette and otherwise changed, a black disk was combined with the vermilion and ultramarine disks, and various amounts of black introduced into the red-purple mixture by rapid rotation. It was found impossible in this way to bring the colour of the larger disk to equality with that of the smaller one, it remaining always too saturated in hue. Some white was then added to the large disk, and equalization finally effected. It was then found that twenty-one parts of vermilion, twenty parts of ultramarine, with fifty-one parts black and nine parts white, made a tint by rotation which was identical with that given by mixing up the vermilion and ultramarine on the palette. The large amount of black which it was necessary to add strikingly illustrates the general proposition that every mixture of pigments on the painter's palette is a stride toward blackness. We give now the results of the other experiments :

TABLE SHOWING THE EFFECTS OF MIXING PIGMENTS BY ROTATION AND ON THE PALETTE.

Pigments.	By Rotation.	On the Palette.
Violet ("violet-carmine")..... } Yellow-green (Hooker's green)..... }	Yellowish-grey.	Brown.
Violet ("violet-carmine")..... } Yellow (gamboge)..... }	Pale yellowish-grey.	Sepia-grey.
Violet ("violet-carmine")..... } Green (Prussian-blue and gamboge)... }	Greenish-grey.	Grey.
Violet ("violet-carmine")..... } Prussian-blue..... }	Blue-grey.	Blue-grey.
Violet ("violet-carmine")..... } Carmine..... }	Pink-purple.	Dull red-purple.
Gamboge..... } Prussian-blue..... }	Pale greenish-grey.	Full blue-green.
Carmine..... } Hooker's green..... }	Yellowish-orange (flesh-tint).	Brick-red.
Carmine..... } Green..... }	Pale reddish (flesh-tint).	Dark-red.

It will be noticed that in only one case do the results of the two methods coincide ; in all the others the tints from the palette are not only much darker, but also different. Colour-equations were then obtained for the eight cases above given in exactly the manner indicated for vermilion and ultramarine-blue ; and as they present the facts in an exact manner, showing how much black it was necessary to introduce, and how far the proportions of the two component colours had to be varied, they are given below :

Mixture on Palette.	Mixture by Rotation.
50 violet + 50 Hooker's green.. =	{ 21 violet + 22·5 Hooker's green + 4 vermilion + 52·5 black.
50 violet + 50 gamboge..... =	54 violet + 20 gamboge + 26 black.
50 violet + 50 green..... =	50 violet + 18 green + 32 black.
50 violet + 50 Prussian-blue... =	47 violet + 49 Prussian-blue + 4 black.

50 violet + 50 carmine.....	=	{ 36 violet + 37 carmine + 8 ultramarine + 19 black.
50 gamboge + 50 Prussian-blue.	=	{ 12 yellow (gamboge) + 42 Prussian-blue + 41 green + 4 black.
50 vermilion + 50 ultramarine..	=	{ 21 vermilion + 20 ultramarine + 51 black + 9 white.
50 Hooker's green + 50 carmine	=	{ 23.5 yellow-green (Hooker's green) + 8 carmine + 52 vermilion + 16 black.
50 carmine + 50 green.....	=	50 carmine + 24 green + 26 black.

It will be noticed that the amount of black which it was necessary to introduce, in order to darken the *true mixture of the colours* so as to match the *mixture of the pigments*, was a very variable quantity, ranging from four to fifty-two per cent. It is for this reason that artists are so careful in their selection of pigments for the production of definite tones, particularly when they are to be luminous in quality. In four of these experiments it was found impossible to bring about equality without adding to the two original constituents a third colour, and in one case white had to be added; so that, in more than half the cases examined, the original colours were found incapable of reproducing by a true process of mixture the tint obtained on the palette without the aid of a foreign element. These experiments serve, then, to show that the results furnished by the palette can not be relied on to guide us in the interpretation or study of effects in nature depending on the mixture of coloured light.

We propose now to consider the results which are produced when a coloured surface is exposed to a coloured illumination and at the same time to white light. Effects of this kind are very common in nature, and are frequently purposely selected by artists as themes; in a minor degree they are always present to some extent, even when we seek to avoid them. With the knowledge which we have now gained, it is possible for us to recognize the fact that in such cases the resultant tint of the surface will depend on

three circumstances : first, on the colour which it assumes owing to the presence of the white light—that is to say, which it has owing to its natural or, as artists call it, “local colour”; secondly, on the colour communicated to it by that portion of the coloured light which is reflected unaltered from its surface ; and to these there must be added, thirdly, the effects produced by the coloured light which penetrates below the surface, and is reflected after undergoing a certain amount of absorption. It is quite easy to make satisfactory experiments on this matter with the aid

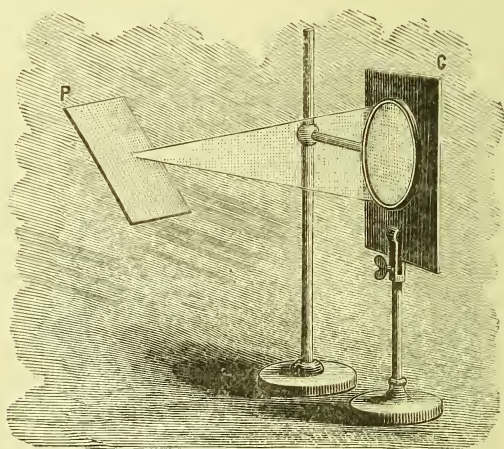


FIG. 62.—White light from a window falls on stained glass at G, and is then concentrated by the lens on a sheet of white or coloured paper at P.

of a simple arrangement contrived by the author. At a distance of some eight or ten feet from a window, a lens, with a focal length of about five inches, is placed on a table, in such a way as to concentrate the white light from the window. In front of the lens a plate of coloured glass is held, and the result is that we obtain a bright beam of coloured light, which can be thrown on any coloured surface, such, for example, as painted paper (see Fig. 62). If

the walls of the room are white, the paper will at the same time be exposed to a white illumination ; and, by turning it or removing it farther from the lens, the proportions of this double illumination can be varied at will. We will describe two experiments that were made with this arrangement : Yellow light was obtained by using a plate of glass which transmitted light having to the eye a pure yellow hue, without any tendency to orange-yellow or greenish-yellow. In this beam of light a piece of paper, painted with a very intense, deep hue of artificial ultramarine, was held. The portion illuminated by the yellow light appeared almost quite *white*, showing that a true mixture of the colours had taken place. It is well known that it is difficult to decide about the actual colour of a spot when it is surrounded by a coloured field ; hence, in order to avoid deception by contrast, it is well in these experiments to observe the spot which has received the double illumination through an aperture cut in black paper, which is to be held in such a way as to permit a view only of this spot. This precaution was taken in the present case, and also in all the experiments that are given below. The ultramarine paper was then removed, and its place supplied by some which had been painted with Prussian-blue. The spot now appeared of a bright *green* colour, which proved that an action had taken place similar to that produced by mixing pigments on the palette. The explanation is as follows : The yellow glass transmits yellow, green, orange, and red light ; and, as was explained in the previous chapter, these lights taken together make a light which appears to us yellow. That portion of this compound yellow light which penetrates the Prussian-blue undergoes a process of absorption ; the green constituent, however, is not absorbed, and consequently is reflected rather abundantly from the paper. But some of the yellow light is reflected unaltered from the immediate surface of the paper ; this mixes with the blue light (due to the white illumination), and makes white ; so that what we

finally have is green mixed with more or less white. In the experiment where the ultramarine paper was used, no doubt some absorption took place, but it was not sufficient to modify the result materially ; the blue and yellow light simply united, and formed white light. Below are given, in the form of tables, a large series of experiments made recently by the author ; and an examination of them will show that for the most part the resultant tint depends rather on a true mixture of coloured lights, and that absorption acts only as a minor agent in modifying the results :

TABLE I.

Yellow Light falling on Paper painted with	
Carmine gave.....	Red-orange.
Vermilion gave.....	Bright orange-red.
Orange * gave.....	Bright orange-yellow.
Chrome-yellow gave.....	Bright yellow.
Gamboge gave.....	Bright yellow.
Yellowish-green † gave.....	Yellow.
Green ‡ gave.....	Bright yellow-green.
Blue-green § gave.....	Yellow-green (whitish).
Cyan-blue gave.....	Yellow-green.
Prussian-blue gave.....	Bright green.
Ultramarine-blue gave.....	White.
Violet ¶ gave.....	Pale reddish tint.
Purple-violet ** gave.....	Orange (whitish).
Purple †† gave.....	Orange.
Black ‡‡ gave.....	Yellow.

* Mixture of red lead and Indian-yellow.

† Mixture of gamboge and Prussian-blue.

‡ Mixture of emerald-green with a little chrome-yellow.

§ Mixture of emerald-green with a little cobalt-blue.

|| Mixture of cobalt-blue and emerald-green.

¶ Hoffmann's violet B. B.

** Hoffmann's violet B. B. and carmine.

†† Hoffmann's violet B. B. and carmine.

‡‡ Lampblack.

TABLE II.

Red Light falling on
Paper painted with

Carmine gave.....	Red.
Vermilion gave.....	Bright red.
Orange gave.....	Red-orange and scarlet.
Chrome-yellow gave.....	Orange.
Gamboge gave.....	Orange.
Yellowish-green gave.....	Yellow and orange.
Green gave.....	Yellow and orange (whitish).
Blue-green gave.....	Nearly white.
Cyan-blue gave.....	Grey.
Prussian-blue gave.....	Red-purple or blue-violet.
Ultramarine-blue gave.....	Red-purple or blue-violet.
Violet gave.....	Red-purple.
Purple-violet gave.....	Red-purple.
Purple gave.....	Purple-red or red.
Black gave.....	Dark red.

TABLE III.

Green Light falling on
Paper painted with

Carmine gave.....	Dull yellow.
Vermilion gave.....	Dull yellow or greenish-yellow.
Orange gave.....	Yellow and greenish-yellow.
Chrome-yellow gave....	Yellowish-green.
Gamboge gave.....	Yellowish-green.
Yellowish-green gave...	Yellowish-green.
Green gave.....	Bright green.
Blue-green gave.....	Green.
Cyan-blue gave.....	Blue-green.
Prussian-blue gave.....	Blue-green, cyan-blue.
Ultramarine-blue gave..	Cyan-blue, blue.
Violet gave.....	Cyan-blue, blue, violet-blue (all whitish).
Purple-violet gave.....	Pale blue-green, pale blue.
Purple gave.....	Greenish-grey, grey, reddish-grey.
Black gave.....	Dark green.

TABLE IV.

Blue Light falling on
Paper painted with

Carmine gives.....	Purple.
Vermilion gives.....	Red-purple.
Orange gives.....	Whitish-purple.

Chrome-yellow gives	Yellowish-grey, greenish-grey.
Gamboge gives.....	Yellowish-grey, greenish-grey.
Yellowish-green gives.....	Blue-grey.
Green gives	Blue-green, cyan-blue.
Blue-green gives.....	Cyan-blue, blue.
Cyan-blue gives	Blue.
Prussian-blue gives	Blue.
Ultramarine-blue gives	Blue.
Violet gives.....	Ultramarine, violet-blue.
Purple-violet gives.....	Blue-violet.
Purple gives.....	Violet-blue, purple-violet.
Black gives.....	Dark blue.

These experiments, taken as a whole, show that, in calculating for the effects produced by illuminating coloured surfaces by coloured light, we must be guided mainly by the laws which govern mixtures of coloured lights, rather than by those which can be deduced from experience with pigments ; they are certainly useful in teaching us, when studying from nature, fearlessly to follow even the most evanescent indications of the eye, utterly regardless of the fact that they disobey laws which we have learned from the palette.

We pass on now to consider the changes in tint which take place when coloured surfaces are illuminated by lamp-light or gas-light. If we undertake to make experiments in this direction simply by viewing coloured surfaces by lamp-light in a room illuminated with it, correct results can not be obtained ; for by this very method we have practically rendered ourselves colour-blind to a certain extent, and have become incapable of judging correctly of quite a series of hues. Gas-light is deficient in the violet, blue, and bluish-green rays ; hence its resultant tint is not white, but orange-yellow. If we are immersed in this light, it will appear to us white, and our judgment of all colours will be more or less disturbed : yellow surfaces will appear white or whitish ; blue surfaces, more greyish-blue, or, if pale,

even pure grey. The actual changes effected by artificial illumination may readily be studied by the following simple method, contrived by the author : A camera-obscura is placed in a room illuminated by ordinary daylight ; in front of it, at a short distance, is placed a gas-flame or lamp-flame, in such a way that the lens of the camera is capable of forming an image of it of about half the natural size. (See Fig. 63.) This image is now allowed to fall on coloured stuffs or on coloured paper placed behind the lens of the camera at S ; it can be viewed, as indicated, through

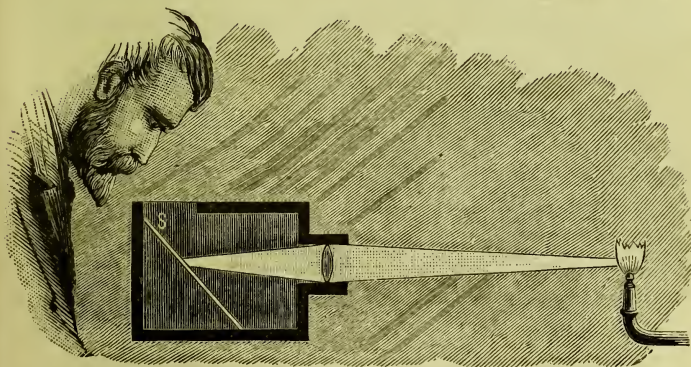


FIG. 63.—Light from Gas-flame is concentrated by Lens of Camera and falls on Coloured Paper.

the top of the camera, and the resultant tint noted. In the experiments made by the author a gas-flame was employed, along with a set of painted disks, representing the principal colours. The disks, fourteen in number, were the same as described in the following chapter, and constituted together seven pairs, the colours of which were complementary, two and two. Below are the results :

1. A carmine disk when illuminated by the gas-flame assumed an intense red hue, even more brilliant than by daylight ; the complementary disk, painted blue-green, appeared of a yellowish-green, not saturated, but rather pale.

2. Vermilion appeared of an intense fiery red ; its complement, green-blue, lost in strength, and became yellowish-green and rather pale.

3. Orange appeared brilliant ; cyan-blue, the complement, became greenish-yellow and lost in saturation.

4. Yellow became brilliant, showing a tendency toward orange ; its complement, blue, appeared white, or rather pure grey. On the same occasion disks painted with chrome-yellow were examined : two of them were rendered somewhat orange-yellow ; the third was brought to almost a full orange hue by the gas-light. A disk painted with gamboge-yellow acquired something of an orange tint under the gas-light.

5. Greenish-yellow was brought to a pure yellow ; its complement, artificial ultramarine-blue, appeared violet.

6. *Greenish*-yellow became pure yellow ; its complement, violet, was converted into a strong red-purple.

7. Full green passed into a bright, strong yellowish-green ; its complement, purple, assumed an intense purplish-red hue, displaying less blue than by daylight.

These are the actual changes produced by the artificial illumination as they appeared to an eye placed in ordinary daylight, and consequently able correctly to note the several tints. When the disks were examined at night by gas-light, in many cases a different result was reached. The carmine and vermilion disks still appeared very brilliant, the tint in the case of the former being a pure red, while the vermilion showed a tendency to red-orange. The orange disk seemed to be changed in tint to a redder orange hue ; the yellow, on the contrary, appeared paler. The greenish-yellow disks did not show much change. The full green was intense, appearing perhaps more bluish than by daylight. Blue-green was liable to be confused with blue, cyan-blue and blue with green ; artificial ultramarine-blue appeared more purplish than by daylight ; violet became purple, and purple a very red purple. Some other disks

were also examined on this occasion : gamboge and chrome-yellow showed a loss in saturation, looking whitish ; indigo appeared dull greenish-grey ; Prussian-blue was confused with blue-green ; genuine ultramarine-blue still was always blue with a slight tendency to purple ; cobalt-blue exhibited this same tendency, which reached a maximum in French-blue. All the blues appeared much duller and greyer than by daylight.

By comparing these two sets of experiments, it will be seen how greatly the judgment of colour was influenced by the circumstance that the prevailing illumination was yellow, and that hence a certain shade of yellow stood for white, and gave a false standard to which all the colours were referred. This was particularly noticeable in the case of the yellow disks ; in point of fact, as the first set of observations showed, they reflected to the eye much yellow light, and, as far as the mere physical action went, ought to have produced the sensation of a strong, brilliant yellow hue ; but, as all surfaces which professed to be white were really (owing to the gas-light) yellow, this competition caused the yellow disks to appear pale. Another case illustrates this disturbed judgment even better. In the first set of experiments it was found that the blue disk when illuminated by gas-light really assumed a pure grey hue without any trace of blue ; but at night, although it must have sent to the eye this same pure grey light, it always appeared either blue, greenish-blue, or bluish-green ; in other words, the blue disk, when held near the gas-flame, sent to the eye white light, which appeared *blue*, by contrast with the prevailing yellow illumination. It is hardly necessary to add that these causes affect our judgment of paintings and decorations at night to a very considerable degree, the blues being rendered less conspicuous, the blue-greys being mostly abolished, and the yellows losing in apparent intensity. Genuine ultramarine-blue is less affected than the other blues, cobalt and artificial ultramarine-blue becoming pur-

plish, and Prussian-blue quite greenish. It hence follows that paintings in which the blue tones are rather overdone appear often better by gas-light ; but this is hardly the case when the green hues are of somewhat too great strength, the evil seeming often to be exaggerated by artificial illumination, which must of course be due to an act of the judgment, as the greens really assume a more yellowish appearance by gas-light or lamp-light, as was proved by the first set of experiments. From this it follows that, if the chromatic composition of a picture is quite right for daylight, it will be more or less wrong when viewed by gas-light ; hence it would be desirable to illuminate picture galleries at night with some kind of artificial *white* light, a problem which the future will no doubt solve.

All the appearances which have thus far been considered could be satisfactorily observed and studied by a person possessed of only a single eye. Let us now turn our attention for a moment to some very remarkable phenomena which occur when different colours are presented to the right and left eye. This is a case which happens occasionally, particularly when we look at the reflection from polished surfaces or from water. In order to simplify matters, let us take a case where, for instance, yellow light is presented to the right and blue light to the left eye. It is very easy to make an experiment of this kind with the aid of the stereoscope. Selecting one of the common paper slides, we colour it as indicated in Fig. 64, and then view it with the stereoscope. We have already seen that blue and yellow light when presented to the same eye undergo mixture on the retina and produce the sensation we call white. This would lead us very naturally to suppose that, if blue light were presented to the right eye and yellow to the left, the two sensations would be united in the brain and would call up that of white. The effect is, however, of a much more complicated character. Viewed in the

stereoscope the figure will appear at one moment blue, then yellow, as though it had no permanent colour of its own ; sometimes, again, the observer seems to see one colour through the other, and is distinctly conscious of the presence of both occupying apparently the same place, thus giving rise to the idea that the object might have at the same time two distinct colours. Meanwhile the little drawing assumes a highly lustrous appearance, as though it were made of polished glass ; this is quite beautiful, and strikes with some astonishment those who see it for the first time. After some little practice has been gained, the blue and yellow colours will melt into a lustrous blue-grey or pure grey tint now and then for a few seconds, when again the

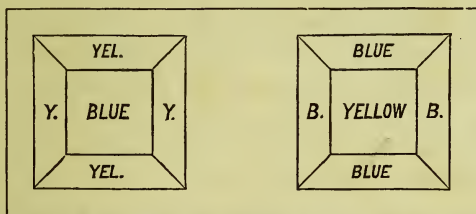


FIG. 64.—Slide for the Stereoscope, the Right and Left Hand being differently coloured.

contradictory and confusing phantoms just mentioned will make their appearance. Taken altogether, the effect is quite wonderful, and suggestive of something like a new sensation. There has been a good deal of controversy as to whether a true blending or mixture of the two colours actually does take place in the brain. The experiments of De Haldat and Dove, and afterward of Lubeck, Foucault, and Régnault, all point to this result. The results obtained by the author are also favorable to this view. But it must be confessed that the mixture obtained by this method differs in one respect from those previously described. For, when coloured light is mixed with the aid of rotating disks or by Lambert's method, we see only the resultant tint, the

two components disappearing entirely to give place to it. On the other hand, in this binocular mixture of colours, the presence of each of the original colours is all the while to some extent felt, and we are disposed to say that we see a neutral or grey hue which has evidently been made out of blue and yellow. Careful experiments by the author proved that the tint of the true mixture often differed from that obtained by the use of the stereoscope ; colours which were pale, however, united more readily than intense ones, and gave less divergent results.* The binocular mixture of colours always produces more or less lustre ; it is not even necessary to employ distinct colours, the same effect being brought about by the mixture of a light and dark shade of the same colour, or simply by the binocular union of white and black, as was shown by Dove. The lustrous appearance of waves, ripples, and broken reflections in water is in each case mainly produced in this way, and hence, strictly speaking, can not be imitated by artists, who are necessarily obliged to present the same colours, the same light or dark shades, impartially to both eyes. It is for reasons similar to the above that a somewhat lustrous appearance is communicated to an oil painting by varnish, or to a water-colour drawing by glass ; the eye sees the picture through the light slightly reflected from the glass or varnish, and is enabled apparently to penetrate beneath the mere surface of the pigment, and this slight illusion falls in with and helps the design of the artist.

* " American Journal of Science," May, 1865.

CHAPTER XI.

COMPLEMENTARY COLOURS.

IN the previous chapter we found that the mixture of two masses of coloured light in some cases produced white light ; this was, for example, true of mixtures of ultramarine-blue and yellow, or of red and greenish-blue. Any two colours which by their union produce white light are called complementary. An accurate knowledge of the nature and appearance of the complementary colours is important for artistic purposes, since these colours furnish the strongest possible contrasts. The best, in fact the only, method of becoming acquainted with the appearance of colours which are complementary is by actually studying them with the aid of suitable apparatus. The results thus obtained should be at the time registered, not in writing, but by imitating as far as possible the actual tints with brush and palette. By the aid of polarized light it is possible to produce with ease and certainty a large series of colours which are truly complementary. There are quite a number of instruments for accomplishing this, but perhaps the simplest and best is that which was contrived by Brücke for this express purpose, and called by him a schistoscope. (See Fig. 65.) This little apparatus is merely a combination of a low-power simple microscope with a polariscope, and can easily be constructed. Starting from below, P is a piece of white cardboard, which is fastened to the stand as indicated, and is consequently capable of being turned so as to reflect upward more or less white light, as may be required. N is

a Nicol's prism, which polarizes the light thus reflected ; it is attached to a blackened stage, S. At A is a small square aperture two millimetres in size. C is a crystal of calc spar ; L is a convex lens of a focus such as to cause the two images of the square opening furnished by the calc spar just to touch each other. G and G are polished wedges of glass, the angles being 18° ; for rough experiments they may be dispensed with. In order to use this apparatus,

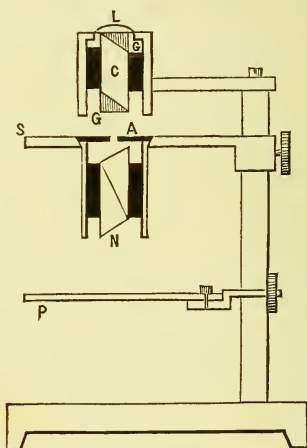


FIG. 65.—The Schistoscope, for the production of Complementary Colours. (Brücke.)

the tube containing the calc spar is to be moved till distinct vision is obtained of the square opening in the stage by the eye placed at L, or rather of the *two* square openings which will be seen ; the tube is then to be revolved till one of these images disappears entirely, and is to be left in this position. Besides the instrument it is necessary to provide a large number of thin slips of selenite or crystalized sulphate of lime. If a clear transparent piece of this substance is procured, it will be easy with a penknife to split off two or three hundred thin slips, and then with the aid of the instrument to select those which are worth pre-

serving. To observe the colours it is only necessary to lay one of the slips on the stage between the calc-spar prism and the Nicol's prism, and then to turn the selenite till two brightly coloured squares are seen, as is indicated in Fig. 66. These two squares will always have colours which are



FIG. 66.—Complementary Colours as exhibited by the Schistoscope of Brücke.

complementary. The object of preparing a large number of the slips of selenite is the production of a large series of complementary tints. The thinner slips furnish colours that are more saturated ; those which are thick give pale colours, or colours mixed with much white light. It will be found in this way that the following pairs of colours are complementary :

TABLE OF COMPLEMENTARY COLOURS.

Red.....	Green-blue.*
Orange.....	Cyan-blue.

* Following Helmholtz, most writers give bluish-green as the complement to red. These observations of Helmholtz were made on the spectrum, the field being small and only a single eye employed. Extended observations with coloured disks, the hue of which can be studied in a more natural way and with both eyes simultaneously, have convinced the present writer that the complement of vermilion is a very green blue, and even the complement of carmine is a very green blue rather than a blue-green.

Yellow.....	Ultramarine-blue.*
Greenish-yellow.....	Violet.
Green.....	Purple.

In Fig. 67 these complementary colours are arranged in a circle. They are of course only a few of the pairs that can be noticed. The tints situated between red and orange will have complements lying between greenish-blue and cyan-blue; those between orange and yellow, again, will find complements between cyan-blue and ultramarine-blue, etc. As before remarked, it is a good plan to copy the results with water-colours; this fixes the facts in the memory far better than mere momentary inspection.

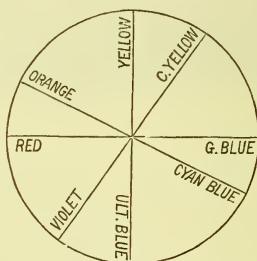


FIG. 67.—Complementary Colours arranged in a Circle.

To study the complementary colours with the aid of the spectrum is a much more troublesome process; still, it is of interest for us to know that the results are the same as when polarized light is employed. Another point now deserves consideration. It might be supposed that the luminosity or apparent brightness of colours which are complementary would be the same, but this is far from being true; yellow, for example, is much more luminous than its complementary blue, and the difference between greenish-yellow and violet is still greater. Helmholtz, using the pure col-

* The complement of genuine ultramarine-blue is yellow, that of artificial ultramarine being a greenish-yellow. The artificial pigment, or French-blue, is a violet-blue.

ours of the spectrum, ascertained that the order of the luminosities of the complementary colours is about that given in the following table :

Yellow.

Orange and green about the same.

Red and cyan-blue about the same.

Ultramarine-blue.

Violet.

From this it follows that a violet which appears to the eye quite dark is able to balance a bright greenish-yellow, and form with it white, and the same is true of ultramarine-blue and yellow ; red and its complement green-blue have about the same luminosities ; orange is somewhat brighter to the eye than its complement cyan-blue. There is another way of stating these facts : we can say that in mixtures violet has a greater power of saturation than any of the colours ; next follows ultramarine-blue, then red and cyan-blue, etc.

The method of studying complementary colours with the aid of polarized light and plates of selenite is simple and beautiful, but there are many cases which it does not reach ; above all, it fails to furnish us with the means of ascertaining the complementary tints in just those instances which are of particular interest, viz., the pigments. This happens because the colours furnished by the plates of selenite are for the most part quite like those of the spectrum, only mixed more or less with white light. We should seek in vain among them for good representatives of olive-greens or chocolate-browns and many other common tints. One of the problems that present themselves most frequently is to ascertain the complementary colour of some particular pigment or mixture of pigments. For the rough solution of such questions a method given by Dove can be employed : A small square of paper, an inch or less in size, is to be painted with the pigment in question and placed on a sheet

of black paper, and viewed through an achromatized prism of calc spar. This is shown in Fig. 68, and has the property

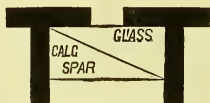


FIG. 68.—Achromatic Prism of Calc Spar.

of furnishing when held before the eye two equally bright images of objects viewed through it. It is used in this experiment instead of a plain calc-spar prism, because it gives a greater separation of the two images, and thus allows the employment of larger squares of coloured paper. As the finding of the colour which is complementary to any given one depends entirely on experiment, a second piece of paper, also an inch square, is now to be painted with the colour which it is supposed will be complementary to the first, and the two painted papers are to be combined together with the aid of the calc-spar prism. Let us suppose that we wish to obtain the complement of a dull reddish-brown. The red-brown square is placed on the black paper; beside it we lay a piece painted with a dull bluish-green grey, and arrange matters so that an image of the red-brown paper falls on one furnished by the blue-grey paper. If the two colours are complementary, their joint image will be white, or rather pure grey. If, instead of pure grey, it shows a tendency to reddish-grey or bluish-grey, the colour of the second slip of paper must be modified accordingly. This operation is facilitated by constantly comparing the tint obtained with that of a slip of pure grey paper, placed on the same sheet of black paper. When the process is finished, the appearance will be that indicated in Fig. 69.

The practical objections to this mode of experimenting are, that the calc spar reduces the luminosities of the coloured papers, and that, owing to the imperfect means of

comparison, one is too apt to accept as pure grey any approximation to this tint. For all accurate work it is far better to employ Maxwell's disks in the manner now to be described.* Let us suppose that we wish to obtain the



FIG. 69.—Red-brown and Blue-grey are combined in the central Image, and form a Pure Grey. Below is a Grey placed for comparison.

complement to a somewhat dark vermillion-red. The details in an actual experiment were as follows: A disk was painted with the tint in question, and combined with two others painted with emerald-green and ultramarine-blue, as it was known beforehand that the desired colour would be a bluish-green of some kind. See Fig. 70, which shows also smaller black and white disks placed on the same axis for the purpose of obtaining a pure grey for comparison. It will be noticed that the red colour has been made to occupy just one half of the disk, or 50 parts; the remaining 50 parts are to be divided up between the blue and green, as is found by experiment necessary. The result showed

* For an account of Maxwell's disks, see previous chapter.

that 50 parts of red were neutralized by 31 parts of emerald-green and 19 parts of artificial ultramarine-blue; the three colours gave a grey identical with that furnished by 13 parts white and 87 black. Putting this in the form of an equation, we have : 50 red + 31 em.-green + 19 ult.-blue = 13 white + 87 black.



FIG. 70.—Emerald-green and Ultramarine-blue Disks arranged so as to neutralize Red and produce with it a Pure Grey. Central Black and White Disk for the production of a Pure Grey.

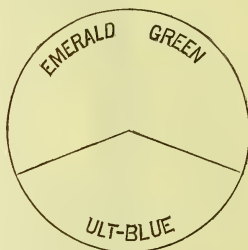


FIG. 71.—Disks of Emerald-green and Ultramarine-blue arranged so as to give a Colour Complementary to Red.

The next operation is to mix emerald-green and ultramarine-blue in the proportion of 31 to 19, which will evidently give us the correct complement of our red. As these two colours in the last experiment occupied exactly one half of the disk, it evidently will be necessary to double them if they are to be spread over a whole disk; accordingly, we combine them together, taking 62 parts of the green and 38 of the blue. (See Fig. 71.) This compound disk when set in rapid rotation gives us accurately the complementary colour of our red. It is seldom in practice that so complete a result as this can be obtained; for it is evident that, if the red colour had been more luminous, it would have been impossible to balance 50 parts of it with 50 parts of the blue and green, however arranged; the resultant tint would always have been a *reddish*-grey. Conversely, if the red had been less luminous, a similar

difficulty would have occurred: the resultant tint would have always been somewhat bluish green instead of pure grey.

We give now an actual experiment which illustrates the way in which the matter usually falls out, and shows at the same time the nature of the result to be expected. It was desired to obtain the complement to a dull yellow, somewhat like the tint of brown pasteboard. A disk was painted with this colour and combined with one of artificial ultramarine-blue, the small black and white disks of course being present. When this arrangement was set in rotation, it was found impossible to produce a pure grey, however the proportions of the blue and yellow disks were varied; at the best the tint furnished was a purplish-grey. This of course indicated the necessity of adding some green to the blue: a disk of emerald-green was now added, when it was found that 43 parts yellow, combined with 43 parts ultramarine-blue and 14 parts emerald-green, gave a grey identical with that furnished by 24 parts of white and 76 black. The equation then reads: $41 \text{ yellow} + 45 \text{ blue} + 14 \text{ green} = 24 \text{ white} + 76 \text{ black}$. From this it follows that, by mixing ultramarine-blue and emerald-green in the proportion of 45 to 14, a colour complementary to our yellow could be obtained. We then divide up 100 in this ratio, and assign 76·3 parts to the blue and 23·7 to the green, combine the blue and green disks in this ratio, and by rotation obtain the complementary colour, which is a fine blue. This blue is, however, somewhat darker than the true complement of our yellow, for in the first experiment the yellow did not occupy fully one half of the disk, or 50 parts, but only 41 parts; if we had made it fill half the disk, the other colours would not have been luminous enough to balance it, and grey would not have been produced. It is easy for us to calculate how much too dark the tint is which we have obtained as the complement of the yellow: if we call the luminosity of the true complement 100, then that which we

actually obtain is 69·5.* Hence, in using this complement, we must always allow for the fact that it is less luminous than the true complement in the degree above indicated. Furthermore, no better result could be obtained with the disks of blue and green which were used ; to improve the result, it would have been necessary to alter them so that they would become able to reflect more blue and green light to the eye. On the other hand, if they had originally reflected too much green and blue light, this might have been diminished with the aid of a black disk, and the true complement accurately obtained. Hence it follows that we can obtain the *true* complement to a given colour with accuracy only in those cases where we have at our disposal representatives of this complementary colour which are sufficiently intense—that is, at the same time luminous and saturated. The practical effect of this is, that we can not directly obtain the complementary tints of the most intense of the warmer pigments, such as carmine, vermilion, red lead, chrome-yellow ; the colder pigments, like emerald-green, cobalt-blue, Prussian-blue, ultramarine, etc., all falling considerably below them in intensity.

For many purposes it is convenient to possess a set of disks arranged in pairs and representing the main complementary colours. It would of course require much time and patience to construct a set in which the colours were quite correct in the matter of hue and also in that of luminosity ; and in such a set, with the pigments at our disposal, the red and orange hues would be quite dull, and the yellows little more than browns or olive-greens, for the reason above given. The author recently constructed a set in which the hues were nearly correct, and the luminosities as favourable as could be obtained without too much expenditure of time and trouble. Their relative intensities as pairs were also determined, as well as the amounts of white light which they furnished when combined in pairs.

* See appendix to this chapter.

TABLE OF COMPLEMENTARY DISKS.

Colour.	Intensity.	Colour.	Intensity.	Amount of white light furnished by the combination.
Carmine	100	Blue-green.	68·6	25
Vermilion.	100	Green-blue	56·2	25·3
Orange	100	Greenish-blue.	88·7	27·2
Yellow	100	Blue.	64·5	25·6
Greenish-yellow.	89·7	French-blue	100	28·9
<i>Greenish-yellow.</i>	88·7	Violet	100	32·2
Green	100	Purple.	86·9	25·7

It will be noticed that an attempt was made to have the set so arranged as to furnish in each case, as far as possible, about the same amount of white light, so that in this respect the disks should have nearly the same rank. For an account of the pigments that were used, the reader is referred to the appendix to the present chapter. With the aid of this set of complementary disks, hundreds or even thousands of pairs of complementary colours can be quickly produced. This is effected by combining any pair either with white or with black, or with both. For instance, all the reds darker than carmine can be obtained by combining the carmine disk with different proportions of a black disk, the corresponding complementary colours being furnished by the blue-green disk similarly treated; in the same way, the reds paler than carmine and their complements are to be obtained by the addition of a white disk; and finally, all the complementary red and blue-green *greys* are yielded by adding a white and a black disk to either of the two coloured disks. Hence it will be seen that, though a set of disks of this kind costs some trouble at the start, yet afterward it more than repays the labour, by quickly supplying us with a vast range of colours which are either truly com-

plementary in all respects, or defective only in the matter of luminosity to a calculable extent.

We come now to a matter which at first sight will seem strange. We have seen that every colour has its complementary colour, but more than this is true : every colour has many different complementary colours. This may best be illustrated by an experiment. Let us suppose we wish to study the colours which are complementary to that of our green-blue disk : We combine this disk with one of vermilion, to which it is complementary, so that we have 50 parts of green-blue and as much vermilion as is found necessary. Now, as considerably less than 50 parts of vermilion will represent the complement of our green-blue, we fill up the blank space left by the vermilion with black. After being adjusted so as to give a grey, the disk was found to be arranged as indicated in Fig. 72. It was found, namely, that 50 parts of green-blue were just balanced and neutralized by 27 parts of vermilion, leaving 23 parts of the disk to be occupied by black. To render visible *this*

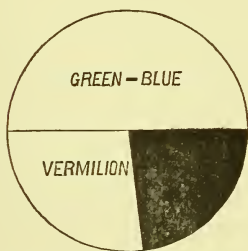


FIG. 72.—Green-blue and the complementary amount of Vermilion.



FIG. 73.—This Disk by rotation gives one of the Complements of Green-blue.

complement of the green-blue, we combine a black and vermilion disk in the proportion 23 to 27, or, what is the same thing, in that of 46 to 54, and rotate it. (See Fig. 73.) This furnishes us with a somewhat dark vermilion-red ; it is one of the complements of the green-blue. If we now replace the

black in Fig. 72 by white, the proportions still remaining as 46 to 54, we produce a light-reddish flesh tint, quite different in appearance from the dark-red colour before obtained, but still accurately complementary to our green-blue, since it contains the same amount of red. If the 46 parts of black are gradually replaced by white, a series of tints will be obtained differing in luminosity, but all reddish, and all complementary to the same green-blue. The set of complementary disks above described furnishes great facilities for studying the different appearances assumed by pairs of complementary colours under these circumstances.

Another point now deserves attention. Suppose that we select by daylight two painted surfaces with colours that are strictly complementary—for instance, red and green-blue. Afterward, if we view these two surfaces by lamp-light or gas-light, it will not at all follow that the colours will still neutralize each other and remain complementary. It is easy to experiment on this matter with the aid of our set of complementary disks. By daylight it was found that 41 parts of carmine neutralized 59 parts of green-blue and gave a true grey : by gas-light these colours were no longer complementary, but, in the above-mentioned proportions, furnished a pretty strong red-purple. Experimenting still by gas-light, the red was reduced to 29 parts and the green-blue increased to 71, when the tint of the mixture became less red, but still neutralization could not be effected : the two colours had by gas-light ceased to be complementary, and it was found necessary to add 13·5 parts of green to reestablish this relation between them. The same fact was observed with the following pairs of complementary colours :

Vermilion	and	green-blue.
Orange	“	cyan-blue.
Yellow	“	blue.

With the pair greenish-yellow and ultramarine-blue, the effect was reversed: it was necessary by gas-light to reduce the greenish-yellow somewhat and to replace a portion of it by orange. The pairs greenish-yellow and violet, green and purple, remained complementary alike by daylight and gas-light. The following table shows the results when the disks were arranged so as to appear complementary by daylight and by gas-light:

Colours.	By daylight.	By gas-light.
40·7 carmine and 59·3 green-blue.....	Grey.	Red-purple.
36 vermilion and 64 green-blue.....	"	Purplish-red.
47 orange and 53 cyan-blue	"	Purplish-red.
39·2 yellow and 60·8 blue.....	"	Greyish-purple.
52·7 greenish-yellow and 47·3 French-blue *.....	"	Greenish-grey.
53 <i>greenish-yellow</i> and 47 violet.....	"	Grey.†
46·5 green and 53·5 purple.....	"	Grey.†

Below follow the proportions when the disks appeared complementary by gas-light:

Colours.	By daylight.	By gas-light.
29 carmine, 57 green-blue, and 14 green....	Strong green.	Grey.†
27 vermilion, 57 green-blue, and 16 green ...	" "	"
37 orange, 50 cyan-blue, and 13 green	Strong green-grey.	"
37·5 yellow, 56 blue, and 6·5 green.....	Greenish-grey.	"
45 greenish-yellow, 48 French-blue, 7 orange.	Purplish.	"
52 <i>greenish-yellow</i> , 48 violet.....	Grey.	"
47 green, 53 purple.....	"	"

These changes depend on two causes. First, the composi-

* Artificial ultramarine-blue.

† Really a dark yellow, which *appeared* by gas-light grey.

tion of gas-light is different from that of white light ; the violet, blue, and greenish-blue rays in gas-light are comparatively feeble, and, owing to this circumstance, the disks must of course present a different appearance when illuminated with it, the violet, blue, and green-blue pigments appearing relatively darker. This circumstance would, however, merely require us to use more of these hues, and would not necessitate the introduction of foreign colours. The second cause is that by gas-light we are able to effect neutralization only when the mixture of the two colours has a tint similar to that of the general illumination itself, which in this case is not white, but yellow, inclining toward orange. It follows from these experiments that if red or orange is to be contrasted with its complement by gas-light, it will be necessary to make the contrasting colour more greenish than would be allowable by daylight ; the same is true to a less extent of orange-yellow and of yellow itself.

Leaving these practical matters for a moment, let us turn our attention to a couple of theoretical points which are not without interest. In a previous chapter we have seen that colour varies with the length of the waves of light : knowing this, we are very naturally led to inquire whether there is any fixed relation between the lengths of waves which produce upon us the sensations of complementary colours. Upon studying the matter with the help of a chart of the normal spectrum, we find that no such relation exists, owing to the circumstance that the change in colour in different parts of the spectrum is not directly proportional to the change in wave-length, as was pointed out in a previous chapter. Helmholtz found that the relation which does exist is not a fixed one for all the different pairs of complementary colours, but that it varies considerably. With some of the pairs this relation is as 1 to 1·2, in others as 1 is to 1·333 ; or, using the musical notation, we would say that the relation varies from that existing between a note and its fourth to that between a note and

its diminished third. This is one of the many facts which are fatal to any chromatic theory that has a musical basis for its foundation.

The other matter demanding our attention is the mode in which the phenomena of complementary colours are explained by the theory of Thomas Young. In a previous chapter we saw that a mixture of red, green, and violet light, when presented to the eye, produced the sensation of white ; and in the present chapter we have found that this same sensation can be produced by the mixture merely of *two* properly selected colours. Now, according to Young's theory, the sensation of white is produced when the three sets of nerve-fibrils with which the retina is provided are stimulated to about the same degree of activity ; hence it must follow that *two* colours can stimulate all the three sets of nerves as effectually as the *three* fundamental colours. It is this fact that we are called on to account for, and the explanation in the principal cases is as follows :

Red and green-blue are complementary colours, because red light stimulates the red nerves, and green-blue light both the green and violet nerves ; the joint action of the three sets gives white light. Orange and cyan-blue is the next pair : orange light sets in action the red nerves powerfully, also somewhat the green nerves ; cyan-blue sets in action the green and the violet nerves ; all three sets of nerves acting, the result is the sensation of white. The case is much the same with yellow and genuine ultramarine-blue : both colours stimulate two sets of nerves ; that is, the yellow acts on the red and green nerves, the blue on the green and violet nerves. With green and purple the first colour acts of course on its own set of nerves, the second on the red and violet nerves. All this is strictly in accordance with the principles of Young's theory, as will be found by reference to the chapter in which it is treated.

This explanation enables us to understand a fact which otherwise might appear quite strange, viz. : that if we take

away from white light any colour, the light which remains will have the complementary hue. Thus, if we strike out from white light the orange rays, the remainder will appear of a rather pale cyan-blue. The table of complementary colours explains this result ; thus,

Red and green-blue make	White.
Orange and cyan-blue make	White.
Yellow and blue make	White.
Green-yellow and violet make	White.
Green and purple make	White.

All these five pairs of colours are present in white light. If we remove from it orange, then cyan-blue is the only colour which is not neutralized ; all the other colours balance up and make white light, which mixes with and pales the uncombined cyan-blue. The explanation is the same in all the other cases. It follows from this that the complementary colours produced by the method of striking out a colour are rendered rather pale by the presence of a considerable amount of white light. This is the reason why the complementary colours obtained by the use of polarized light are always rather pale. The presence of this white light, as will be shown in the following chapter, actually somewhat alters the tint of the coloured light mixed with it ; red is made to incline to purple, orange to red, purple and ultramarine to violet.

Before closing this chapter it may be well to make some remarks concerning the complement of pure yellow, and the complements of the several varieties of the more common blue pigments. In different works the complement of yellow is given as indigo-blue, ultramarine-blue, or simply as blue. *Genuine* ultramarine-blue is complementary to pure yellow, the complement of artificial ultramarine-blue being a decidedly greenish-yellow. Gamboge gives a yellow which is slightly orange ; its complement is the pig-

ment known as cobalt-blue. The complement of Prussian-blue was determined and found by the author to be a somewhat orange-yellow; it was made by mixing with a rotating disk 65 parts of pale chrome-yellow with 35 parts of vermilion. The complement of indigo, used as a water-colour pigment, was also determined with care, and found to correspond quite closely with that of Prussian-blue; it hence follows that indigo may be considered to be the same as darkened Prussian-blue, and not to represent, as some authors have suggested, darkened ultramarine-blue. The term indigo was applied by Sir Isaac Newton to designate the more refrangible blue of the spectrum; to this it does not really at all correspond in any respect, and in the present work the term ultramarine-blue is substituted for it. If the different blues be arranged in the order of the spectrum, we shall have cyan-blue, indigo or Prussian-blue, cobalt-blue, genuine ultramarine and artificial ultramarine, the last being a violet-blue. Among the yellow pigments the somewhat orange-tinted chrome-yellow is complementary to indigo and Prussian-blue; chrome-yellow with a still more orange hue has a complement nearer to cyan-blue.

APPENDIX TO CHAPTER XI.

THE mode of calculating the relative intensities of pigments which are complementary is quite simple, and is here illustrated by an example. Let us suppose that 25 parts of a certain red neutralize 75 parts of a green-blue. The compound disk will then appear as in Fig. 74. It is evident that the intensity of the green-blue is only one third of that of the red, since it takes three times as much green-blue as red to effect neutralization. Let I be the greater intensity and I' the lesser; then we have—

$$25 I = 75 I'$$

Making the greater intensity 100, we have—

$$25 \times 100 = 75 \text{ I'}$$

$$\text{I'} = 33\cdot3$$

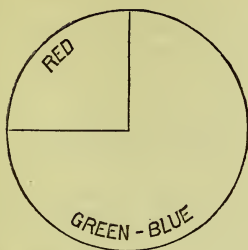


FIG. 74.—Disk with 25 Parts Red and 75 Parts Green-blue.

That is, if we call the intensity of our red 100, that of the green-blue will be only 33·3. In the case given in the present chapter we have—

$$41 \text{ I} = 59 \text{ I'}$$

$$41 \times 100 = 59 \text{ I'}$$

$$\text{I'} = 69\cdot5$$

PIGMENTS USED IN THE SET OF COMPLEMENTARY DISKS.

Carmine as a water-colour; for its complementary green-blue, a mixture of cobalt-blue and emerald-green.

Vermilion as a water-colour; for its complement the same as above, the proportions being changed.

For the first two pairs, then, we can employ two of our most intense and saturated pigments; this, however, is not possible with orange and yellow, without producing disks of a rank different from the preceding, or obtaining disks which show greater differences in luminosity than any which have been tolerated in the table given in the present chapter. Thus a fine orange colour was mixed from red lead and Indian-yellow, which would have been considered by most painters, as I suppose, a fair companion for the carmine and vermilion; or, if objection had been made, it would have been rather to its want of intensity. Placing the intensity of this orange as 100, the intensity of its complement (made of cobalt-blue and emerald-green) was only 47, a figure smaller than any in the table.

These two colours, however, furnished a white such as could be obtained by mixing, with the aid of disks, 36 parts of white with 64 of black; this number is considerably higher than those allowed in the table. The combination then was rejected, because it was faulty in two respects, and a dull-looking orange substituted for it. This dull, rather poor-looking orange balanced its complementary cyan-blue well, and with it gave 27 per cent. of white light, which was fully up to the average, and proved that in the matter of luminosity it belonged in the set rather than the disk just mentioned.

A similar experience was encountered with yellow. Two beautiful disks were prepared with gamboge and cobalt-blue. Setting the intensity of the gamboge as 100, that of the cobalt was 90, which was nearly what was wanted. The combination, however, gave on rotation a white which was about 100 per cent. too bright, showing that the two disks belonged in a set such as would be furnished by pigments twice as bright as those employed by me; but no such pigments exist. This is only another illustration of the fact, already several times mentioned, that our bright-yellow pigments, such as gamboge, chrome-yellow, cadmium-yellow, etc., can not properly be reckoned as the equal companions of the other pigments ordinarily found on the painter's palette. This circumstance affects our judgment, and we are surprised at the lack of brilliancy of the yellow space even in the prismatic spectrum, and at the fact that mixtures of red and green light produce yellow light of so inferior a character. On the other hand, the possession of such exceptional pigments as the bright yellows and orange-yellows enables the artist at will to extend his scale of brilliancy in an upward direction much farther than otherwise would be possible.

The greenish-yellows were made with gamboge mixed with a little Prussian-blue, the pigments being laid, not on drawing-paper, but on rather absorbent cardboard, which dulled the colours to a desirable extent. For violet, "Hoffmann's violet B. B." was employed, none of the violet pigments used by artists being of the slightest use on account of their very dull appearance and poverty in the matter of violet light. The green was made by mixing a little chrome-yellow with emerald-green; the purple was "Hoffmann's violet R. R. R."

CHAPTER XII.

ON THE EFFECT PRODUCED ON COLOUR BY A CHANGE IN LUMINOSITY, AND BY MIXING IT WITH WHITE LIGHT.

IN our study thus far of coloured surfaces it has been tacitly assumed that their action on the eye is a constant one, and that a red surface, for example, will always appear red to a healthy eye as long as it remains visible. In point of fact, however, this is not quite true, for it is found that coloured surfaces undergo changes of tint when they are seen under a very bright or very feeble illumination. Artists are well aware that scarlet cloth under bright sunshine approaches orange in its tint; that green becomes more yellowish; and that, in general, a bright illumination causes all colours to tend somewhat toward yellow in their hues. Helmholtz, Bezold, Rutherfurd, and others have made similar observations on the pure colours of the prismatic spectrum, and have found that even *they* undergo changes analogous to those just indicated. The violet of the spectrum is very easily affected: when it is feeble (that is, dark), it approaches purple in its hue; as it is made stronger, the colour changes to blue, and finally to a whitish-grey with a faint tint of violet-blue. The changes with the ultramarine-blue of the spectrum follow the same order, passing first into sky-blue, then into whitish-blue, and finally into white. Green as it is made brighter passes into yellowish-green, and then into whitish-yellow; for actual conversion into white it is necessary that the illumination should

be dazzling. Red resists these changes more than the other colours ; but, if it be made quite bright, it passes into orange and then into bright yellow.

It is remarkable that these changes take place with the *pure* colours of the spectrum ; but the explanation, according to the theory of Young and Helmholtz, is not difficult. Let us illustrate it by an example, taking the case of green light, which, as we have seen, acts most powerfully on what we termed the green nerves, less powerfully on the red and violet nerves. Now, as long as the intensity of our green light is small, it acts almost entirely on its own peculiar set of nerves ; but, when the green light is made brighter, it begins to set into action also the red and to a lesser extent the violet nerves ; the result of this is that the sensation of white begins to be mingled with that of green, all three sets of nerves being now to some extent in action. As in this process the violet nerves lag behind, the main modification of the colour at this stage is due to the action of the red nerves, which cause it to appear more yellowish ; hence it changes first to a yellowish-green, then to greenish-yellow, and finally, if the light is very bright, to a whitish-yellow. Corresponding to this, when red light is made very bright, the red and the green nerves are set into action, the result being that the colour changes in appearance from red to yellow. In this case the violet nerves play a secondary part, and their action merely causes this yellow to appear somewhat whitish. When pure violet light is made quite bright, immediately the green nerves begin to add their action to that of the violet, and the tint quickly changes from violet to ultramarine-blue ; the red nerves are soon also stimulated, and, in connection with the green, furnish the sensation of yellow ; this yellow, mixing with that of the ultramarine-blue before mentioned, gives as a resultant tint a whitish-grey with a faint tint of blue or violet-blue. The explanation of the changes which the intermediate colours of the spectrum undergo is analogous to that

just given. The tendency in all cases is to the production of a yellowish-white, or to a white, if the coloured light be very bright. If its brightness be more moderate, the colour will still appear paler and as though mixed with a certain amount of yellow. Artists, by taking advantage of these facts, are able to represent in their paintings scenes under high degrees of illumination. According to Aubert, the whitest white paper is only 57 times brighter than the darkest black paper ; and it is within these narrow limits that the painter is compelled to execute his design : hence the necessity of employing illusions like the one just mentioned. Many effects in nature are beautiful and striking, as much on account of their high degree of luminosity as for any other reason. The artist is not able to transfer to his canvas the brightness, which in this case is really the attractive element ; but by the use of pale colours, well modulated, he suggests a flood of light, and we are delighted, not so much with the pale tints as with the recollections they call up.

We have just examined the remarkable alterations which the pure colours of the spectrum undergo when their luminosity is made very great, and pass now to the changes which occur when the intensity of coloured light is made very feeble. Von Bezold has made some interesting observations of this character on the colours of the spectrum. With a very bright prismatic spectrum he was able to see a pure yellow near D and a whitish-blue near F, the other colours being in their usual positions. When the illumination was only moderately bright, the yellow space diminished and became very narrow ; the ultramarine-blue vanished, and was replaced by violet. With less illumination, the orange-yellow space assumed the colour of red lead, and the yellow vanished, being replaced by a greenish tint ; the cyan-blue was replaced by green, the blue and ultramarine-blue by violet. The spectrum at this stage presented scarcely more than the three colours, red, green, and violet. With

a still lower illumination, the violet vanished, the red became red-brown, and the green was visible as a pale-green tint; then the red-brown disappeared, the green still remaining, though very feeble. With still less light, even this suggestion of colour vanished, and the light appeared simply grey.

The tendency in these experiments is evidently just the reverse of what was observed where the illumination was very bright. In that case the coloured light as it increased in brightness gradually set all three sets of nerves into action, and the result was white or yellowish-white; but here the action of the coloured light as it grows feebler is more and more confined to a single set of nerves. From this it results that those colour-sensations which are due to the joint action of two sets of nerves speedily diminish when the colour is darkened, and are replaced by the primary sensations, red, green, or violet. The sensation of orange is produced by those light-waves in the spectrum which have a length such as to enable them to stimulate the red nerves strongly and the green nerves to a lesser degree; hence, when orange-coloured light is made very weak, it fails to act on the green nerves while still feebly stimulating the red, and consequently the sensation of orange passes over into red. For similar reasons the sensations of yellow and greenish-yellow pass into green, as do also those of greenish-blue and cyan-blue; in the same way the sensations of blue, ultramarine-blue, and violet-blue pass into violet. It is quite evident that these changes furnish another argument in favour of Young's theory of colour, and also tend to approve the selection of red, green, and violet as the fundamental colour-sensations.

In the experiment of Von Bezold just mentioned, after the spectrum had been darkened to a certain degree only three colours remained—red, green, and violet; this dark red, however, as far as sensation goes, is somewhat changed in character, and, according to the unpublished experiments

of Charles Pierce, has become somewhat purplish ; the same is true of the green, which is more bluish ; the violet alone is unchanged. Now, just these same effects can be produced by mixing small quantities of violet with red or green ; hence the final effect of darkening on all the colours of the spectrum is virtually to mix them with increasing quantities of violet light. The cause of these peculiar changes, according to the theory of Young and Helmholtz, resides in the fact that the violet nerves act more powerfully, relatively to the red and green nerves, when the light is feeble. For example, if we present to the eye pure green light, it will stimulate the green nerves strongly, the red and violet to a much less degree : we thus obtain a certain sensation, and call it green. If now we greatly diminish the intensity of the green light, it will of course affect the green nerves to a minor degree ; but, besides this, it has now less action on the red than on the violet nerves, so that virtually we have a mixture of green and violet, which will cause the green to appear bluish-green. The same explanation holds good for the red, dull red light producing less effect on the green than on the violet nerves.

The change which colour undergoes when darkened is interesting from a practical point of view ; and accordingly the author made a series of experiments on this subject, using for that purpose coloured disks and the method of rotation. In these experiments we do not deal with the pure colours of the spectrum, but with surfaces painted with brilliant pigments, which correspond more nearly to the cases that present themselves to the artist and decorator. A black disk was in each case combined with a coloured disk, as indicated in Fig. 75 ; a smaller disk of the same colour being either attached to the axis for comparison or held from time to time near the rotating disk. It was ascertained by previous experiments that the amount of white light reflected by the black disk was small ; if we set the amount of light reflected by white cardboard as 100,

then the black disk which was employed on this occasion reflected two per cent. of white light, or $\frac{1}{50}$. The colour of the painted disks was in every case as intense, saturated,



FIG. 75.—Chrome-yellow and Black Disks in combination.



FIG. 76.—The disk of Fig. 75 when in rotation becomes coloured olive-green.

and brilliant as possible. The results obtained by rotation—that is, by reducing the luminosity of the colours by mixing black with them—are briefly indicated below :

TABLE I.

Name of Colour.	Effect of reducing its Luminosity.
Fundamental red (carmine and vermilion).	Not changed, or made <i>slightly</i> purplish.
Vermilion.	
Red lead	More red, less orange-red.
Orange	Brown.
Chrome-yellow or gamboge.	Olive-green.
Greenish-yellow	More greenish.
Yellowish-green	More pure green.
Fundamental green	Not changed, or made <i>slightly</i> more bluish.
Emerald-green	More green, less blue-green.
Blue-green	More green, less bluish.
Cyan-blue.	More greenish.
Prussian-blue.	Dark grey-blue (not changed).
Cobalt-blue	Dark grey-blue (not changed).
Ultramarine-blue (artificial).	More violet, less blue.
Violet.	Dark violet.
Purple.	More violet, less red.
Carminc	Not much changed.

It will be noticed that these results correspond more or less closely with those of Von Bezold, before given.

Some of the changes in the experiments just mentioned were so great as to be quite astonishing, and might well tempt the beholder to believe that the black disk exercised some peculiar influence on the result ; this, however, was not the case, as the same results can be obtained without the black disk by simply reducing the illumination of the coloured disks by holding before the eye two Nicol's prisms, and turning them so as gradually to cut off the coloured light. On the other hand, if the tints that are obtained by using the black disk give the true appearances of surfaces painted with pure pigments, but viewed under a feeble illumination, then accurate copies of them ought, when powerfully illuminated, to appear once more brightly coloured, and of the original tints. This was found to be the case, for example, with gamboge, where the change in colour by darkening was from a slightly orange-yellow to a fine olive-green. The olive-green colour was carefully copied with water-colours on a slip of paper, and afterward held in bright sunlight ; this caused it to appear yellow, and made its colour resemble that of the gamboge disk placed near it, but in the shade.

The general result of these experiments is, that, if the illumination is feeble, the colours become weaker, and there is on the whole a general tendency toward a darkish blue ; just as in the reverse case, where the colours are made very bright, there is a tendency toward a whitish-yellow. This average tint can best be studied by observing moonlight effects : here the more luminous colour appears to be a somewhat greenish-blue, the darker shades more like an ultramarine-blue. With regard to this delicate point, the painters of moonlight landscapes are as good an authority as we have, and the best of them are very decided as to the prevalence of various shades of blue, greenish-blue, and violet-blue. Similar effects, though smaller in degree, are ob-

served on dull, cloudy days, when the prevailing tint is a bluish-grey. Indeed, as Helmholtz remarks, simply viewing a sunlit landscape through a pale-blue glass suggests the idea of a cloudy day ; while reversing the process, and viewing a landscape on a dull, cloudy day through a pale-yellow glass, gives the impression of sunshine. Corresponding to this, accidental streaks of yellow ochre or sawdust on the shaded pavement often suggest forcibly the idea of stray sunbeams ; and other examples of this kind of illusion might be mentioned. If we mix lampblack directly with pigments on the palette, their colour will of course be darkened, but the effects produced are not identical with those obtained by the method of rotation. Paper was painted with a strong wash composed of carmine and lampblack, which imparted to it a dark-reddish, purplish hue. From this a disk was cut and an attempt made to match its tint by mixing, according to the method of rotation, carmine and lampblack. In order to accomplish this, it was



FIG. 77.—Small central Disk composed of Cardboard washed with a Mixture of Carmine and Lampblack. This is nearly matched by disks painted with carmine, black, and white, in the proportions indicated.

found necessary to introduce into this rotation-mixture a quantity of white ; the best match being effected when the compound disk was arranged as indicated in Fig. 77. This shows that the saturation or intensity of a coloured pigment is greatly reduced by mixing lampblack with it on the palette, and is one reason why artists refuse to adopt this

method of producing dark shades of colour. The mechanical mixture of lampblack with pigments, besides reducing their saturation, also usually at the same time changes somewhat their hue. In the experiment just mentioned, after matching the two colours as well as possible, it was found that the carmine which had been mixed with lampblack on the palette was more violet in hue than that which had been mixed with black optically. Corresponding results were obtained with vermilion when mixed mechanically and optically with lampblack. In the first case the colour was more of an orange-red hue than in the last. Prussian-blue and lampblack on the palette give a much more greenish tint than when mixed by rotation, and similar changes can be observed with many other pigments.

We have seen thus far that, as we change the luminosity of a coloured surface, so do we at the same time affect its hue, all coloured surfaces when very bright tending toward a whitish-yellow tint. Changes in luminosity, however, produce still other effects which are quite remarkable. If we arrange by ordinary daylight sheets of red and blue paper, which have as far as we can judge about the same degree of luminosity, and then carry them into a darkened room, we shall be surprised to find that the blue papers appear brighter than the red. Indeed, the room may be darkened so as to cause the red paper to appear black, while the blue still plainly retains its colour. These facts seem first to have been recorded by Purkinje and Dove. By similar experiments it can be proved that red, yellow, and orange-coloured surfaces are relatively more luminous when exposed to a bright light than blue and violet surfaces; the latter, on the other hand, have the advantage when the illumination is feeble. Thus Dove noticed a long time ago that this circumstance disturbs somewhat the balance of the colours in paintings, if the observer lingers in a picture gallery as the twilight deepens. From this it follows that the chromatic composition of a painting should

be somewhat varied, according as the picture is likely generally to be seen under full daylight or in a darkened room. More attention would no doubt be paid by artists to this point if they were not obliged to contend with a still more serious obstacle in the large change which the tint of the illuminating light undergoes, according as daylight or gas-light is employed.

It follows from what has just been said that photometric comparisons of the brightness of differently coloured surfaces, if made under bright daylight, will no longer hold good in twilight, and that consequently we can not under a certain illumination establish photometric relations that shall hold good under all other illuminations. For example, we may find under ordinary daylight that a certain piece of blue paper is just half as luminous as a piece of red paper ; but it by no means follows that this statement will be true in a darkened room. Helmholtz found that even the pure colours of the spectrum act in this same manner, particularly yellow and ultramarine-blue, or greenish-yellow and violet, the changes with the other colours being smaller. This fact suggests an interesting experiment : Yellow and ultramarine-blue are complementary, that is, together make up white light ; suppose now we mingle yellow and ultramarine-blue so as to produce white, a high degree of illumination being employed ; will they still produce white if they are both correspondingly darkened ? We might very naturally suppose that the blue would not outweigh the yellow, and that instead of white we should obtain bluish-white. This was, however, found by Helmholtz, using pure spectral colours, not to be the case : the darkened mixture of yellow and blue still exactly resembled sunlight which was correspondingly darkened. The same result was also obtained when a mixture of another pair of complementary colours, greenish-yellow and violet, was used. These results apparently contradict the statement that yellow or greenish-yellow acts more power-

fully on the eye when bright than blue or violet. Helmholtz accounts for it in this way: Our standard for bright white is bright sunlight; we cause the mixture of yellow and blue to match this sunlight, and then call it white; we then darken our sunlight very much, and make it our standard for a feeble white having a small degree of luminosity; we call it darkened white or pure grey, and find that our darkened mixture of blue and yellow still matches it perfectly. But, according to Helmholtz, this pure grey is really somewhat bluish, and it is owing to this circumstance that it is able still to match the darkened yellow and blue, which is also really bluish. Pure grey has always appeared to the present writer as somewhat bluish compared with pure white, and the following experiment tends to show that this is indeed the case: A pure grey was generated on a rotating disk by mixing fifty parts of white

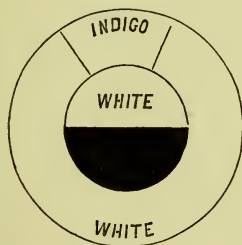


FIG. 78.—Small White-and-Black Disk arranged so as to make a Grey by rotation. This grey looks more bluish than the larger white disk; 17 per cent. of an indigo disk is then mixed with the white.

with a like proportion of black. This compound disk was placed on the same axis with a white disk, but when set in rotation the grey portion appeared slightly more bluish than the white. In order to cause the white disk to match in hue (not in luminosity) the grey disk, a disk painted with a tolerably deep wash of indigo was combined with the white disk, as indicated in Fig. 78. An assistant arranged the disks and made the measurements, while the

author simply ordered the proportion of blue to be increased or diminished till the result seemed satisfactory ; at the termination of the experiment he was informed of the result. The amounts of added blue in nine consecutive experiments were as follows, in percentages : 17, 20, 18, 16, 13, 14, 21, 19, 16 ; average, 17. According, then, to these experiments, it was necessary to add to white 17 per cent. of a strong tint of indigo, in order to cause it to match in hue a grey disk made up of equal parts of white and black. It may be remarked in this connection that the addition of the blue to the white, although slightly changing its tint, produced no particularly noticeable effect on its luminosity ; that is, it was only a little darkened.

All these phenomena can be explained by the theory of Young as modified by Helmholtz. According to this theory, the sensation of white is produced when the red, green, and violet nerves of the retina are stimulated to about the same degree of activity ; furthermore, with a feeble degree of stimulation of all three sets of nerves, the activity of the violet nerves predominates over that of the green, and that of the green again over that of the red. When the stimulation is made powerful, these conditions are reversed, the red nerves leading, the green and violet following. These relations of nerve-action are indicated by three curves in Fig. 79. The horizontal line represents increase of actual intensity of white light ; thus the portion A B stands for feeble white light, A C for white light which is twice as strong, etc. The vertical line B R measures the intensity of the red sensation produced by this feeble white light ; B G and B V give the strength of the sensations in the case of the green and violet nerves. We see that the violet sensation, as it is represented by the longest line, prevails over the others, and that the light, instead of appearing white, will be such as would be produced by mixing equal parts of the sensations red, green, and violet ; i. e., by mixing the sensation of white with a little green

and a little more violet. Now, as we have previously seen in Chapter IX., the sensations of green and violet when mixed produce that of blue, so that on the whole we have a mixture of the sensation of pure white with blue, i. e., bluish-white. If we examine in the same way the line D V G R, we shall find the conditions reversed; here we have the sensation of pure white mixed with a slight excess of that of green, and again with a little more of red; as green and

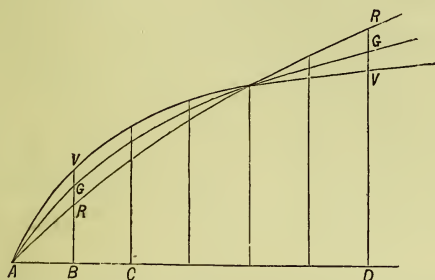


FIG. 79.—Three Curves showing the action of the Red, Green, and Violet Nerves when stimulated by White Light of different degrees of Brightness.

red when mixed furnish yellow, our result now will be white mixed with yellow, or yellowish-white. This same diagram also represents in a symbolic manner the fact that red surfaces are most luminous by bright light, and violet surfaces by feeble light. It can also be used to explain the changes which pure colour undergoes when made very bright or very pale, after the manner employed in the early part of the present chapter.

We have examined now with some detail the relative changes in luminosity which coloured surfaces undergo when exposed to bright and feeble illuminations; but, before leaving this part of our subject, it may not be amiss to mention the fact that *all* comparisons between the luminosities of differently coloured surfaces are quite valueless as the expression of objective facts. An illustration will make

this clear. Suppose we compare together by the eye two white surfaces or two red surfaces, and find that they appear to us equally luminous ; now, this will be not only a fact as far as the eye is concerned, but it will be an objective fact in nature ; it will be equally true in a mechanical sense, and on, converting our two masses of white light or red light into heat, we shall obtain equal amounts of heat. If, however, we take two differently coloured surfaces, red and blue for example, and make them equally luminous, equally powerful so far as the eye is concerned, and then convert the light they reflect into heat, a delicate thermometric apparatus will speedily inform us that we are not dealing in the two cases with equal amounts of force. In fact, the maximum heating effect was found by Melloni to be produced by the ultra-red rays which are quite invisible to the eye ; here, from an objective point of view, resides the greatest force, but the waves are too long to affect the eye at all. From this it is evident that the intensity of our visual sensations depends not only on the strength (height or amplitude) of the waves of light, but also on their length ; the maximum effects being produced by yellow light, which affects simultaneously the red and green nerves. In spite of the fact that photometric comparisons of differently coloured surfaces have no objective value, still for our purposes they may often be quite precious, or even actually indispensable, if we propose to give our work a quantitative character.

Having now considered the changes which colour undergoes when made very luminous or very feeble, we proceed to study the effects produced by mingling white with it. The general result can be expressed quite concisely : the colour becomes paler, and when the proportion of white is made large entirely disappears, leaving recognizable only a white surface. When a disk painted as in Fig. 80 is rotated, the red by mixture with the white gives a ring of pale red, like that indicated in Fig. 81. Upon reducing the

amount of the colour, it becomes very whitish and pale; and Aubert found that the red when mixed with from 120 to 180 parts of white entirely disappeared. If we set the luminosity of vermilion as one fourth of that of white paper, it follows from Aubert's experiment that mixing vermilion

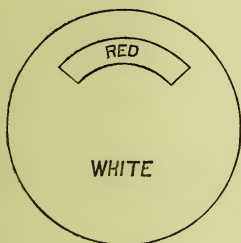


FIG. 80.—White Disk partially painted Red with Vermilion.

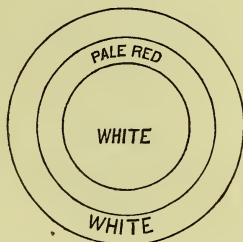


FIG. 81.—Indicates the appearance presented by the previous disk when set in rapid rotation so as to mix the red and white light.

with 720 parts of white light, having a brightness equal to its own, causes the red colour to disappear. Or we may express the fact thus: Take red light and white light of equal intensities; then, if one part of red light be presented to the eye simultaneously with 720 parts of white light, the eye will be unable to recognize the presence of the red constituent. Smaller quantities of white light produce very great changes in the appearance of the colour. If we rotate a disk like that indicated in Fig. 79, we shall be surprised to find that, though one quarter of the disk is covered with vermilion, yet the resultant red tint is quite pale. In this case twelve parts of white light are mixed with one part of equally bright red light, and when stated in this manner the result seems more natural.

When we undertake to study more carefully the mixtures of white with coloured light, certain curious anomalies present themselves. If we arrange disks of artificial ultramarine-blue and white, in the way shown in Fig. 82,

and set them in rapid rotation, we shall find that the addition of white, instead of producing merely a paler blue,

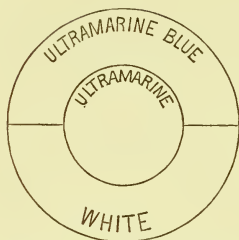


FIG. 82.—White Cardboard Disk partially painted with Ultramarine-blue (artificial).

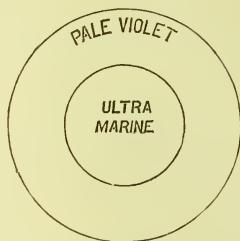


FIG. 83.—Indicates the appearance produced by mixing white with ultramarine-blue light.

actually changes the colour to a pale violet. (See Fig. 83.) If we substitute orange for the ultramarine-blue, the pale-orange hue generated by rotation shows a tendency toward red. These two facts have been known for a long time, and various explanations of them have been proposed. According to Brücke, ordinary white daylight is itself slightly reddish in tint, and, when we mix white light with coloured light, we really add at the same time a little red ; hence these changes. Aubert, on the other hand, following a suggestion of Helmholtz, supposes that the true pale shade of ultramarine-blue is actually violet, but that our judgment is perverted by experience drawn from the colour of the sky, which according to him is a greenish-blue, and retains this tint when mixed with white. This is an explanation which artists would hardly accept, and the experiments given below show that both it and the one previously cited are insufficient. In an examination of this matter it was found by the author that changes of this kind are not confined to the colours orange and artificial ultramarine-blue, but extend over all the colours except violet and its complement greenish-yellow ; the main results are given in the following table :

TABLE II.—SHOWING THE EFFECTS OF MIXING WHITE WITH COLOURED LIGHT.

Name of Colour.	Effect of adding White.
Vermilion.....	More purplish.
Orange.....	More red.
Chrome-yellow.....	More orange-yellow.
Pure yellow.....	More orange-yellow.
Greenish-yellow.....	Paler (unchanged).
Green.....	More blue-green.
Emerald-green.....	More blue-green.
Cyan-blue.....	More bluish.
Cobalt-blue.....	A little more violet.
Ultramarine (artificial).....	More violet.
Violet.....	Unchanged.
Purple.....	Less red, more violet.

It follows from these experiments that, when we mix white with coloured light, the effect produced is the same as though we at the same time mixed with our white light a small quantity of violet light. Such mixture would account for all the changes given in the table, as could be shown by reference to the colour-diagram explained in the next chapter. This, of course, is only stating the facts in different language, and is not an explanation.

In the experiments just mentioned the light from *brilliantly coloured* disks was mixed by rotation with from 5 to 50 per cent. of white light, some of the disks requiring a larger admixture of white light than others to produce the changes in hue recorded in the table. If now we first darken our colours very much, and then add a little white to them, the results will again be somewhat different from those given in the table, because here two causes are at work, which sometimes produce opposite results, as we can see by a comparison of Tables I. and II. In the next set of experiments, in every case except that of chrome-yellow, 5 parts of the coloured disk were combined with 90 parts of *pure* black and 5 parts of white; 10 parts of chrome-yel-

low were combined with 85 parts of pure black and 5 of white. The changes of hue are given below :

TABLE III.—SHOWING THE EFFECT OF MAKING COLOUR VERY DARK AND ADDING TO IT A SMALL PORTION OF WHITE. (The experiments were made by rotating disks.)

Vermilion became a.....	Dull greyish-purple.
Orange became a.....	Brown (slightly bluish).
Chrome-yellow became a.....	Greyish olive-green.
Emerald-green became a.....	Dark green (less bluish).
Cyan-blue became a.....	Dark greenish-grey.
Prussian-blue became a.....	Dark grey-blue.
Cobalt-blue became a.....	Dark grey-blue.
Ultramarine (artificial) became a....	Dark grey violet-blue.
Violet became a.....	Dark grey-violet.
Purple became a.....	Dark grey-violet (less red).

In many of these cases the results are similar in character to those given in Table II. This, however, is not the case with chrome-yellow, as in one case it was made to appear more orange, while in the other it became a whitish olive-green. It is evident that in this instance the effect of darkening the colour overbalanced that of adding white to it. With emerald-green and cyan-blue a similar result seems to have been reached, though the phenomena were less decided. The general effect, then, of first reducing greatly the luminosity of colour and then adding small amounts of white, is the production of greys which have a tendency toward blue or violet, this being the case even when the original colour is as decided as that of vermilion. The experiments given in the last two tables will account for the fact that it is almost impossible to produce a fine red with the aid of polarized light, the tint being always rather of a rose-colour, that is, showing a tendency toward a purplish hue.

It has been shown in the preceding pages that the effect of mixing white with coloured light is to cause the colour to become paler, and at the same time to change it slightly,

as though simultaneously a small amount of violet light had been added to the mixture. This fact naturally suggests an experiment like the following : Suppose we combine a purple and a green disk as indicated in Fig. 84, employing equal parts, and thus obtain a pure grey. Let

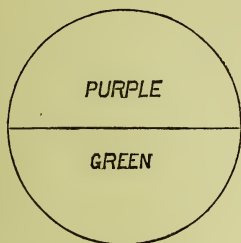


FIG. 84.—Purple and Green Disk : when rotated, it makes a Pure Grey.

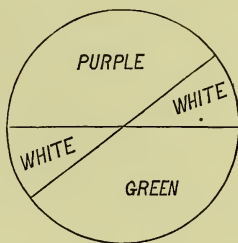


FIG. 85.—Purple, Green, and White Disk : when rotated, it makes a Pure Grey.

us now replace 10 parts of purple by white, also 10 parts of the green by white (Fig. 85) : will we then still obtain a pure grey, or will the grey be tinged with violet ? Several experiments of this kind have been accurately made by the author, but in every case the result was the production of a grey identical with that given by mixing by rotation black and white. The explanation would seem to be that the green and purple instantly combine to produce the sensation of grey, and then of course adding white to this grey can only make it paler, but can not at all alter its tint. It would seem from this that, when a colour is altered in the manner above described by admixture with white, *time* comes in as a necessary element in the process ; the mixture of white and coloured light must be allowed to act on the eye undisturbed during an interval of time which is not too short, otherwise these peculiar effects will not be produced.

One might suppose that the same result would be produced by spreading thin washes of coloured pigments on

white paper that is obtained by mixing white with coloured pigments by the method of revolving disks. The tint in these two cases, however, is usually somewhat different. A pale wash of carmine, for example, was allowed to dry on white paper, and an effort was made to imitate it by combining a deep-coloured carmine disk with one of white cardboard by the method of rotation. It was soon ascertained that the hue of the water-colour wash was considerably more saturated or intense than a tint of equal luminosity produced by the rotating disks; it was also found to be more of a purplish hue. When the luminosities in the two cases were made equal, the water-colour wash showed far more colour than did the simple mixture of the red and white light. Treated in the same way, a thin wash of vermilion was more orange in hue than a mixture of vermilion-coloured light with white light; a thin wash of gamboge looked yellow, while the mixture by rotation had more of an orange-yellow appearance. The reason of these changes is quite evident, and lies in the well-known fact that thin layers of coloured substances have in general a different absorptive action on white light from thicker layers of the same substances. A thin layer of vermilion allows, for example, more of the orange rays to pass; hence in very thin layers this pigment is sometimes used by artists to represent very pale tints of orange, or even of orange-yellow. The other fact above mentioned, viz., that thin layers are often relatively more saturated than those that are thick, is to be explained in a different way. It was shown in Chapter X. that, when a pigment is mixed with one of a different colour, not only is the hue changed, but an effect is produced as though at the same time some black had been added to the mixture. It now appears that, even when a pigment is made darker by mixing with it a larger quantity of itself, a similar change is to some extent produced, the darker wash of the pure pigment acting as though some black were mingled with it. In the experiment with the pale wash of

carmine it was actually found necessary to combine black by rotation with the water-colour wash, so as to reduce it, before it could be matched by a disk composed of white and a deep tint of carmine.

The fact now under consideration can perhaps be rendered more intelligible by a different statement. Carmine, as we know, absorbs powerfully nearly all the coloured rays of light except the red ; these latter it reflects in considerable quantity, and to this circumstance its red colour is due. But the experiments just mentioned indicate that it absorbs also to a considerable extent even the red rays, so that a deep wash of carmine sends to the eye less red light than we should expect. The author found that yellow glass presented a parallel case. Yellow glass transmits the orange-yellow, yellow, and greenish-yellow rays abundantly, and to this power mainly its yellow colour is due. But it does not transmit even these rays at all as perfectly as ordinary window-glass. In one experiment it was found that a plate of yellow glass absorbed about 25 per cent. even of these rays. Most coloured substances, pigments, and glasses probably act in a similar way.

CHAPTER XIII.

ON THE DURATION OF THE IMPRESSION ON THE RETINA.

AMONG different forms of fireworks none excite more admiration than revolving wheels of fire with their brilliant colours, ruby, emerald, or sapphire, and their wonderfully blended surfaces, which so often suggest fanciful resemblances to roses, carnations, and other flowers. It is quite possible to arrange matters so as to obtain an instantaneous view of one of these fiery objects, without at all interfering with its rapid movement ; and when this is done, it is seen that much of its beauty depends upon an illusion : the broad, variegated, shaded surface vanishes, and we have before us simply a few jets of coloured fire, in no wise particularly remarkable. The appearance of these brilliant objects depends, then, upon an illusion, and this has for its foundation the fact that the sensation of sight is always prolonged after the light producing it has ceased to act on the eye.

The most familiar illustration of this fact we find in an old experiment, which no doubt was the parent of our revolving fireworks : If a lighted coal on the end of a stick is caused to revolve rapidly, it describes a ring of fire which is plainly seen at night to be quite unbroken. The light from the moving coal falls upon the retina of the eye, and an image of it is produced, let us say at the point 1, Fig. 86 ; an instant afterward, owing to its having moved into a new position, the image will be found at 2 and then at 3,

and so on all the way around the circle. Now, if the sensation due to the first image lasts while the circle is being traversed, then it will be renewed before it has a chance to fade out, and consequently will be present continuously; the same will be true of all other points on the circle, which consequently will produce on the beholder the appearance of an unbroken ring of light. In order to produce this condition of things, it is necessary of course that the coal of fire should move with a certain velocity; according to



FIG. 86.—Appearance of a Coal of Fire in Three Positions.

the observations of D'Arcy, it is essential that it should traverse its circular path completely in thirteen hundredths of a second.

It is very easy to experiment on matters like these with the aid of revolving disks. If we take a circular disk which is painted black, and has on it a white spot like that represented in Fig. 87, and set it in rotation, as soon as the motion is quick enough we shall see a ring of white, just as in the previous case we obtained a ring of fire. Fig. 88 shows the appearance of the disk when in rapid rotation.

The duration of the sensation of light, or duration of the impression on the retina, as it is called, varies with the intensity of the light producing it, and in the case of our white paper is not by any means so great as with the coal of fire. According to an experiment of Helmholtz, the impression on the retina lasts in this case, with undiminished strength, about one forty-eighth of a second; hence it is necessary for the disk to revolve forty-eight times in a second in order to produce the appearance of a steady, uniform ring of light. While, as just stated, the impression lasts with undiminished strength for one forty-eighth of a second, its total duration with decreasing strength is much greater, being perhaps as high as one third of a second, though this interval varies somewhat with the circumstances, and is a little difficult of determination.



FIG. 87.—Disk with White Sector.



FIG. 88.—Disk of Fig. 87 in Rapid Rotation.

It is not, however, to be supposed that, in the experiment indicated in Fig. 88, the ring of white light will have the same degree of luminosity as its source, viz., the slip of white paper pasted on the black disk; on the contrary, the luminosity of the ring will be much feebler than that of the spot. The reason of this is quite evident: we have virtually spread out the light of the spot over a much larger surface, and it will be proportionately weaker; if the surface of the ring is one hundred times as great as that of the spot, then the luminosity of the ring will be exactly one hundredth of that of the spot. That this relation is always

strictly quantitative can be proved by a photometric arrangement like that used by Plateau for this purpose, or by the aid of a crystal of calc spar which divides ordinary light up into two beams of equal intensity. In this latter case we arrange a disk by making half of its surface white, the other half black, as represented in Fig. 89; alongside of it, on a black ground, we place a strip of the same white paper; the disk is then set in rotation, and assumes a grey appearance. With the aid of the calc-spar prism we then view the strip of paper, which will appear doubled, as shown in Fig. 90, each image having one half the brightness of the



FIG. 89.—Arrangement of Disk and Strip for Photometric Comparison.

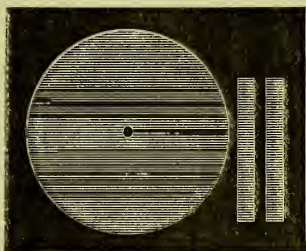


FIG. 90.—Appearance of Disk in Rotation, the Strip being viewed through a Calc-Spar Prism.

original strip; but either of these images will be as bright as the grey disk, showing that the luminosity of the grey disk is just one half of that of the white. This gives an idea of the method of proceeding, but numerous corrections must be introduced, some of which will no doubt suggest themselves to the ingenious reader; of them we will mention only one, viz.: that, according to the recent investigations of Wild, the two images furnished by calc spar do not really have exactly the same luminosity, but differ by about three per cent.* Dove has proved that the relation we have been speaking of above also holds good for coloured

* Poggendorff's "Annalen," vol. cxviii., p. 225.

light. This fact is of much importance to us, for on it is based the principle involved in Maxwell's disks, which we have already found so indispensable in quantitative investigations on colour.

The duration of the impression on the retina in the case of light of different colours has not yet been studied carefully. Some experiments were made by Plateau with papers coloured by gamboge, carmine, and Prussian-blue, and it was ascertained that in these cases the duration differed somewhat. Dr. Wolcott Gibbs suggested to the author a method which would probably solve this problem in a satisfactory manner, and which is about as follows: With the aid of a spectroscope a diffraction spectrum is to be presented to the eye in the form of a series of contiguous coloured bands, this division into bands being effected by a suitable diaphragm placed in the eyepiece of the instrument. In front of the slit of the spectroscope a revolving disk with one or more openings should allow the light to enter the instrument; and, by regulating carefully the velocity of rotation, it would be possible to seize the exact moment when one or more of the coloured bands ceased to flicker, and presented a steady, uniform appearance. This observation would give correctly the interval during which the impression remained with undiminished strength on the eye, in the case of the selected colour.

If quite bright light like that from a window is presented to the eye, the impression lasts several seconds—of course with diminishing strength. The experiment is easily made, and the observer will find, after the eyes have been closed, that there is time enough to recognize a good many details before the disappearance of the image. With intensely bright light like that of the sun, the image lasts several minutes, and finally fades out after having undergone a series of complicated changes in colour. It may perhaps be as well to mention here a fact which must be borne in mind when we undertake to study the after-sensations that follow

the action of white or coloured light on the eye. If the light be allowed to act for a short time on the eye, when it vanishes, as before stated, the sensation remains for a fraction of a second, this after-sensation being in all respects identical with the original sensation, except that it gradually becomes weaker and weaker : thus, if the original sensation is red, the after-sensation will entirely correspond to this colour. This after-image, which is the only one thus far treated of in this chapter, is called the *positive* image. After a little while, however, the positive image vanishes, and is replaced by an image of a different character, which is known as the *negative* image : thus, if the light originally acting on the eye was red, the negative image is coloured greenish-blue, or has the complementary colour. These negative images are quite important, as many matters connected with contrast depend on them, and they will be considered at length in Chapter XV.

We have seen that the positive after-images are useful in furnishing us, in the case of revolving disks, with a mode of mixing together masses of coloured light in definite proportions ; and it may be well to mention some other cases where these images play an important part. The appearances presented by water in motion depend largely on them. Thus, if we study the ocean waves under direct sunlight, we shall find that much of their character depends on elongated streaks of light, which serve to interpret not only the forms of the larger masses of water, but also the shapes of the minor wavelets with which these are sculptured. If now we examine these bright streaks, so well known to artists, with a slowly revolving disk having one open sector, we shall find that in point of fact there are no streaks at all present, but simply round images of the sun, which, owing to their motion, become thus elongated. Instantaneous photographs give the same true result, and hence appear false. An analogous action takes place even in cloudy weather, and streaks of light are produced which give the

waves a different appearance from what they would have if suddenly made solid, while yet retaining all their glassy appearance. Again, for the same reason, waves breaking on a beach appear to us different from their instantaneous photographs : when viewing the real waves we obtain an impression which is made up of the different views rapidly presented during several minute intervals of time, whereas the photograph gives us only what takes place during *one* of these small intervals. All this applies also more or less to the case of falling water, as fountains or waterfalls, and explains the transparency of rapidly revolving wheels. Owing to the same cause, the limbs of animals in swift motion are only visible in a periodic way, or at those moments when their motion is being reversed ; during the rest of the time they are practically invisible. These moments of comparative rest are seized by artists for delineation, while the less discriminating photograph is as apt to reproduce intermediate positions, and thus produce an effect which, even if quite faithful, still appears absurd.*

* For a complete list of what has been published on this whole subject, see a memoir by J. Plateau published by the Belgian Academy of Sciences in 1877.

CHAPTER XIV.

ON THE MODES OF ARRANGING COLOURS IN SYSTEMS.

As we have seen in the previous chapters, the variety of colours presented to us by nature and art is enormous, ranging from the pure brilliant colours of the spectrum down to the dull, pale tints of rocks and earth, and including whole classes which seem at first glance to have but little affinity with each other. It would be difficult, for example, to find anything in the prismatic spectrum which reminds us in the least of the colour brown; the various pale tints which wood assumes when worked seem quite unrelated to the spectral hues; and it is the same with the vast multitude of greys with which we are acquainted, and which so largely constitute the colours of natural scenery. If, instead of comparing with the colours of the spectrum the strange, wonderful, indescribable tints which nature so abundantly displays, we descend a step and think of them in connection with the hues furnished by our brightest pigments, such as vermilion, red lead, chrome-yellow, emerald-green, or ultramarine-blue, we scarcely improve the matter: even such colours as these seem to have no affinities with the modest throng of greys and browns; they appear to belong to a more princely caste, and utterly refuse to mingle on equal terms with the humbler multitude.

The colour of vermilion depends, as we learned some time ago, on three things: first, on the quantity of coloured light which it sends to the eye, or on the brightness of the

coloured light that it reflects ; second, on the wave-length of this red light ; and third, on the amount of *white* light which is mingled with the red. Its colour depends, then, on its luminosity, wave-length, and purity ; these quantities, as we have seen, are called the constants of colour.* In certain cases we can easily alter these constants considerably, and thus ascertain their significance with regard to colour. Let us take a circular disk painted with pure vermillion, and undertake to reduce its luminosity. This could be very efficiently accomplished by removing the disk to a darkened room, when it would be found that the colour was changed to dark red, or even to black. There is, however, an objection to this mode of experimenting : we have always, under such circumstances, a strong tendency not simply to receive the tint that is actually presented to us, but to make, unconsciously, an allowance for the degree of illumination under which we view it. We know that red in a darkened room presents a certain appearance ; when we see this appearance in the darkened room, we say we see dark red ; to the same appearance in a light room we would give a different name. This objection applies to all experiments of this character, whether the object be to expose a surface to a very small or to a very great illumination : we ourselves should, as it were, always be immersed in a medium illumination, so as to retain an undisturbed judgment. In the present case this difficulty is easily avoided. We take our vermillion disk to a room illuminated with ordinary daylight, and reduce its luminosity by combining it with a black disk, as indicated in Fig. 91. When the compound black and red disk is set into rapid rotation, we in effect spread out over the whole surface of the disk the small amount of red light which is reflected from the exposed red sector ; its luminosity can thus be reduced to any desirable extent. It will be found, when we combine 10 parts of

* See Chapter III.

vermilion with 90 of black in this way, that the red colour is converted into a chocolate-brown that bears no close resemblance to the original hue. It can be objected to this mode of darkening colours that there may be in the black disk something that exercises a peculiar effect on the result. If, however, we analyze the faint light which comes from



FIG. 91.—Disk with 10 Parts Vermilion and 90 Parts Black: gives by rotation a dark-reddish chocolate-brown.

the black disk with the aid of a prism, we shall find that it is essentially white, all the prismatic colours being present. Or we may expose our black disk to sunlight, analyze its light with the prism, and compare this analysis with that obtained from a piece of white paper not exposed to sunlight and shaded from the diffuse daylight. When by this proceeding the luminosities of the black and white papers have been equalized, it will be found that the colours which they furnish to the prism differ very little. The fact that the black disk darkens the red one as it would be darkened by a dark room can also be proved in another way: If we first darken a room just as much as we please, and then contrive an aperture opening into it a little larger than our red disk, and arrange matters so that not much light enters the room through this aperture, then we can virtually mix the darkness of this room with the red light of our disk. We simply place a *red sector* on the rotation machine arranged in front of the opening into the dark room, as indicated in Fig. 92, and set the coloured sector into rapid

rotation. We now have the red light of a small portion of the red disk spread out over the darkness due to the darkened room, and the result is the same : we have the same chocolate-brown (Fig. 93). The use of the black disk being thus justified, we may employ it further in our investigation ; and we shall find that by simply reducing the red

light of our vermilion disk with its aid, we produce not only a series of dark, dull reds, but a number of rich, peculiar-looking browns. When we make a corresponding set of experiments

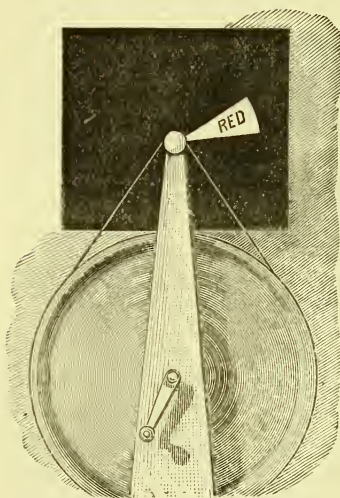


FIG. 92.—Red Sector arranged with Dark Room as a Background.



FIG. 93.—Shows the appearance presented when the sector of Fig. 92 is made to rotate rapidly.

with our red-lead disk, we obtain a series of reddish, warm-looking browns ; the chrome-yellow disk gives a set of strange-looking, dull yellows and dark olive-greens ; the green and blue disks furnish sets of dark green and blue tones. Experiments like these show what changes are produced simply by reducing the intensity of the coloured light, without in any other way tampering with it.

By a corresponding set of experiments we can study the effects of mixing white light with our coloured light : we need only combine the coloured disk with one that is white, and rapid rotation gives us the desired result. In this way

we can produce a series of pale tints that are reddish, greenish, or bluish, according to the disk employed.

Thus, either by reducing the luminosity of our coloured light or by mixing it with more or less white, a great number of tints can be produced; but we soon find that to match many natural colours it is necessary to employ both these proceedings simultaneously. By combining with our coloured disk a black and a white disk, we then become able to imitate a far greater number of the pale, indescribable tints of natural objects. To make our power more complete, we ought also to be able at will to alter the wave-length of the light reflected from the coloured disk.* There are, however, practical difficulties which prevent us from making these changes in a definite and perfect manner, and we find ourselves finally driven to abandon our very convenient and instructive disks, and to turn for help to the colours of the solar spectrum. These colours are pure in the sense of being free from any admixture of white light, their luminosity can be varied to any extent, and the lengths of the various waves which generate them have been measured with a high degree of accuracy; we also can mix white light with them at our pleasure. With the colours of the spectrum, and a purple formed by mixing the red and violet of the spectrum, we can match any colour whatsoever, provided we are allowed to increase or diminish the luminosity of our spectral hues, and to add the necessary amount of white light. This fact furnishes us with a clue toward a classification of colours. The series red, orange, yellow, green, blue, violet, and purple is one which returns on itself, and hence can be arranged in the form of a circle, as was first done by Newton. In making a colour-chart we can place the complementary colours opposite each other, and white in the middle; the pure colours of the spectrum will be situated on the circumference of the circle, and the

* For an account of the effects produced by alteration of wave-length, see Chapter III.

mixtures of these with white will lie nearer the centre, as is roughly indicated in Fig. 94. A chart of this kind will contain all colours that are possible under a given degree of illumination, arranged in an orderly manner. In the sector devoted to the reds we shall find along the circumference every kind of pure red, from purple-red to orange-red, and, as we advance inward toward the centre of the circle, a great number of tints produced by mixing these various reds with increasing quantities of white. It is the same

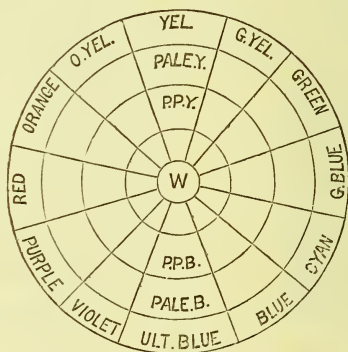


FIG. 94.—The colours of the spectrum are supposed to be on the circumference of the circle, and the mixtures of these with increasing quantities of white are in the interior. White is at the centre. (The spaces for most of the pale or greyish tints are left blank, for want of room.)

with all the other pure colours : every possible hue and tint belonging to the adopted grade of illumination will be found somewhere within the circle ; all the manifold greens and blues, also the whole range of purples, from purplish-red to purplish-violet—all will be represented. At the start, one of our conditions was that complementary colours should be opposite each other ; hence we must give to our blue not only the right hue, but a luminosity such that it is able exactly to neutralize the yellow which is opposite to it. These two colours must also have a luminosity such

that, when they are mixed, the mixture will furnish a white which is twice as bright as that at the centre of the circle. The same must be true of all the other pairs of complementary colours, whether situated on the circumference or in the interior of the circle. This mode of operating gives us a chart in which all the colours of corresponding intensity are well arranged with regard to each other, and it enables us at a glance to see some of the relations of the colours to each other.*

In the construction of this colour-chart we imagined the brilliant colours of the spectrum to be situated on the circumference of the circle, and as we advanced toward the centre a larger and larger proportion of white light was to be mixed with them. Suppose now we diminish somewhat the luminosity of our spectral colours; this will change every tint in the chart correspondingly, and also the central white; all will be darkened proportionately; we shall obtain a new colour-chart, having less luminosity, but in other respects closely resembling the first. With a further reduction of the light a corresponding result will again be reached; and, as we continue the process, we go on accumulating new colour-charts, each being darker than the last. Our two limits evidently are the brilliant colours of the spectrum on the one hand and total blackness on the other; between these we shall be able to place a series of several hundred colour-charts, differing perceptibly in luminosity, but in other respects resembling the original type as nearly as may be.

If we arrange this whole series of charts one above the other in proper order, the most luminous one, or that with which we started, being placed at the top, we shall obtain a cylinder which will contain within itself an immense series of colours. The axis of the cylinder at the top will be

* In this case we consider colours equally intense which, when mixed, neutralize each other and produce the same white. The luminosity of such colours, measured by the eye, will often be quite different.

white, and as we descend it will pass through a great series of darkening greys, finally to end in black. If we make a vertical section of the cylinder, its appearance then will be of the nature roughly indicated in Fig. 95, the axis darkening as we descend, also the charts. Now, we know it to be a fact that, as coloured surfaces are more and more feebly illuminated, so does the number of tints which we can dis-

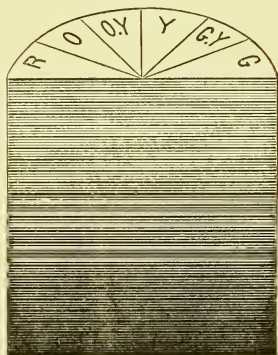


FIG. 95.—Section of a Pile of Colour-Charts, the most luminous ones being at the top.

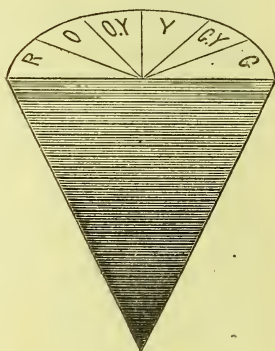


FIG. 96.—Section of a Colour-Cone.

tinguish on them constantly decrease. Hence, in the case of our cylindrical pile of charts, smaller surfaces will answer equally well for the display of the darker tints, and we may as well reduce our cylinder to a cone, as indicated in Fig. 96. This colour-cone is analogous to the colour-pyramid which was described by Lambert in 1772.

It will be remembered that we began our colour-chart with the colours of the spectrum, and these colours, along with their mixtures with white, constituted the base of our cone. The colours of the spectrum in this case were supposed to have only a moderate degree of brightness, such as would be suitable for prolonged observation. These are the brightest colours thus far contained in our cone, but

they are by no means the brightest colours that we are able to see; above them occur a great series of hues which we can more or less perfectly distinguish. As our ability to discriminate very luminous colours diminishes as their luminosity increases, the colour-charts devoted to this new set may be treated like those used for the darker colours. In this way we once more obtain a second cone, which will be placed over the one before described. At the apex of this last cone we have the brightest white which the eye is capable of perceiving; a little below and around it are situated a series of very luminous spectral colours and a purple, all being so bright as to differ, so far as the eye is concerned, not much from a brilliant white; farther down on the sides of the cone are still quite bright colours, and in its interior their mixtures with white. In this double cone, then, we are at last able to include all the colours which under any circumstances we are able to perceive; they are arranged in an orderly manner, which at once exhibits their hues and luminosities, and the amount of white light that has been mixed with them. They are arranged throughout in complementary pairs, and some of their other relations to each other are plainly exhibited.

Now, a word with regard to the possibility of executing this colour-cylinder or the double cone. In the first place, we have no pigments with which we can at all properly represent the colours of the spectrum even when their luminosity is quite moderate; our best pigments all reflect more or less white light mixed with their coloured light. If with their aid we undertook to construct a colour-chart, we should not only be obliged to descend in the cone, Fig. 96, a good distance toward its black apex, but besides this our chart would be smaller than the section of the cone at that point, owing to the presence of the foreign white light reflected by the pigments. It would be next to impossible to prepare pigments of different colours suitable even for the production of a single chart of the series; for it would be ne-

cessary that they should be right in the matter of hue, luminosity, and greater or less freedom from white light.

There are still other objections to the system as just proposed. It furnishes us with no means of giving the colours a proper or rational distribution on the circumference of the circle; we do not know whether the yellow is to be placed 90° from the red or at some other distance; the same is true with regard to the angular distribution of all the other colours; the system gives us no information on this point. It also gives us no information about the effects that are produced by mixing together colours that are not complementary.

There is another mode of attacking this problem which has been much used of late, and which offers certain advantages to the student of colour. Let us suppose that we place red of a certain luminosity at R, and green of the same luminosity at G, Fig. 97; then along the line R G we can arrange, or imagine to be arranged, all possible mixtures of these two colours. To do this we imagine that R and G have certain weights corresponding to their luminosities (or to the quantities of them which in a particular case we employ), and then proceed as if we had before us



FIG. 97.—Along the line R G we can arrange all the mixtures of red and green. The diagram represents the case where equal parts of red and green are employed. Then the point of support (mixture-point) must be in the centre of the line R G.

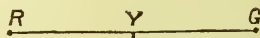


FIG. 98.—A mixture of equal parts of red and green furnishes a yellow; the position of this yellow on the line of mixtures, R G, is at Y.

a mechanical problem. An example will make this plain: Let the luminosity of the red and green both be 10; we now mix 5 parts of red with 5 of green, and obtain a yellow; the position of this yellow will be at Y, Fig. 98, half

way between R and G. We put the position of yellow at Y because, in order that 5 parts of red may balance 5 parts of green, the point of support must be half way between R and G. We have now determined accurately on the line R G the position of a yellow made by mixing equal parts of our original red and green. This yellow, made by mixing 5 parts of red and 5 of green, will also have the same luminosity as the original red or green. If we mix 7 parts of red with 3 of green, the position of the mixture will be at O, Fig. 99. If we divide up the line R G into



FIG. 99.—Seven parts of red are mixed with three parts of green; the mixture is orange in colour, and situated on the line R G at O.

10 equal parts, then O will be distant from R by 3 parts, but from G by 7 parts; for in this way alone a balance can be obtained. In general we shall always obtain a balance or equilibrium when the weight of R multiplied by its distance from O is equal to the weight of G multiplied by the distance of G from O. In this last case (Fig. 99) the mixture at O will be orange in colour, and will have a luminosity identical with the original red and green. So we can go on filling up the line R G with all possible mixtures of the original red and green. Now, this is a process which can actually be carried out in practice. We can take for our red a vermilion disk, and then select for our green a disk having a colour as nearly as possible of the same luminosity, and by the method of rotation produce all the tints above indicated. We can copy these tints, and arrange the copies along the line R G; or, if we do not wish to take this trouble, we can at least always reproduce at will, with aid of the red and green disks, any of the tints belonging on the line R G. This explanation will serve to render clear the fundamental idea on which the colour-diagram of Newton and Maxwell rests.

Thus far we have employed only two colours, red and green, and have been able by mixing them in different proportions to obtain various hues of orange, yellow, and greenish-yellow. If we wish to include the other colours, blue, violet, purple, and the mixtures of all the colours with white, we must employ at the start three instead of two colours. Maxwell selected vermilion, emerald-green, and ultramarine-blue, since according to his researches they approximately represent the three fundamental colours. These he placed at the three angles of an equilateral triangle, and ascertained in a manner afterward to be explained the position of white (or grey) in the interior of the triangle. Every colour that can be obtained by mixing red with green will lie on the line joining red and green; it is the same with green and blue, also with red and blue. Fig. 100 shows these colours disposed along the sides of the triangle; they are also so arranged that complementary colours are opposite each other; white is in the interior, and along the lines joining the sides with the centre are placed the various colours mixed with more and more white as they are situated nearer to the centre. The colours made by mixing red with green, or green with blue, being situated on the sides of the triangle, are consequently as a general thing nearer to the position of white than the three fundamental colours at the three angles of the triangle. This indicates in a geometrical manner the fact that the tints produced by the mixture of two fundamental colours are paler, or mixed with more white, than the fundamentals themselves. In general, in a chart of this kind, the farther we go from the centre or from the position of white, the more do we obtain colours which are free from admixture with white. The angular position of the colours is to some extent arbitrary, being determined partly by the process of mixture, and partly by the assumption that particular hues of red, green, and blue represent the fundamental colours. If we should assume as our fundamental colours red lead,

grass-green, and violet, the angular position of all the other colours would be disturbed. Still, in spite of this and other drawbacks, the colour-diagram is valuable for purposes of

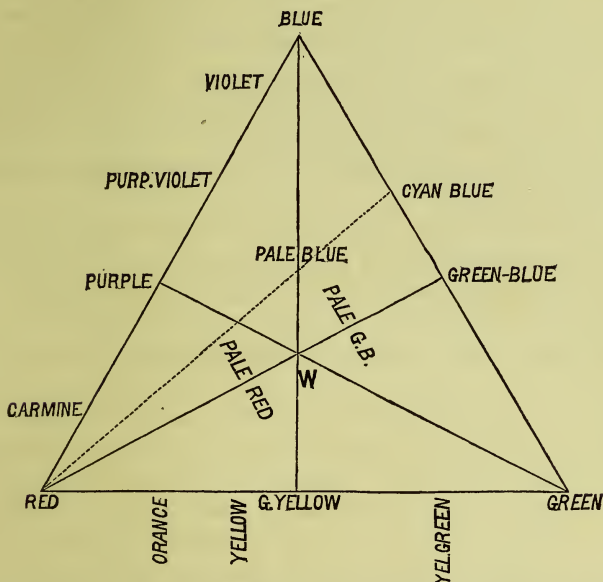


FIG. 100.—Shows the colours that are produced by mixing red with green, etc. The pale colours, or those mixed with white, are situated in the interior of triangle, and grow paler as they are nearer W, or white.

study, and enables us to express our ideas about colour in a geometrical form and with a certain degree of precision. It is easy, for example, with its aid to ascertain the result of mixing together any of the colours contained, or supposed to be contained, in it; if we mix equal parts of red with cyan-blue, it is evident by inspection that the result must be a whitish-purple; so again equal parts of yellow and cyan-blue will furnish a whitish-green. (See Fig. 100.) With the aid of this diagram we can accomplish even more: we can mix together any number of colours, and

ascertain the position and consequently the tint of the resultant hue. We select any two, join them by a line, and ascertain, as previously explained, the position of the mixture tint; we then join the third colour by a straight line with the point just ascertained, and again construct the position of the second mixture, and so on. An account of the mode of making a colour-diagram of this kind will be found in the appendix to this chapter, where the method will also be explained which Maxwell employed for the introduction of colours more or less luminous than the three fundamental ones.

The colour-charts which thus far have actually been published and laid before the world have been of a different character from those above indicated, and are calculated to display the effects, not of mixing coloured light, but coloured pigments. Among the older attempts we may mention those of Le Blond in 1735, and of Du Fay in 1737. In 1758 T. Mayer published an account of his experiments. As three fundamental colours he selected vermilion, a bright yellow, and smalt-blue. Lambert in 1772 used for the construction of his pyramid carmine, gamboge, and Prussian-blue. These colour-charts were constructed by mingling weighed portions of the fundamental pigments and of lamp-black in such a manner as to obtain as great a variety of tints as possible, which were then arranged in an orderly series. The very beautiful colour-charts of Chevreul are essentially of the same nature with those just mentioned. Chevreul employed a circle with three radii which were 120° apart, and placed on these radii red, yellow, and blue; the hues of these colours were copied from certain portions of the prismatic spectrum which were selected as standards. Between red and yellow the various hues of orange and orange-yellow were introduced; between yellow and blue the greens, the purples being situated between violet and red. This constitutes the first chromatic circle, which contains also the purest and most intense colours. In the sec-

ond circle the same colours are shown mixed with a small, definite amount of black ; the third circle is like the second, only still more darkened, and so on. There are ten of these circles, each containing seventy-two tints ; complementary colours are situated opposite each other. Besides the circles, there are charts containing colours arranged in parallel bands ; these are intended to exhibit the effects of mixing black and white with the colours contained in the first circle. They consist of twenty-two bands, the 0 band being white, the 21st black, and the 10th band the same as the corresponding colour in the first circle. Starting, for example, from the 10th band, as we move to 0 the colour grows continually paler, being mixed with more and more white ; if we advance in the other direction, the colour becomes darker, and ends finally in black. There are seventy-two sets of these bands, also one for black and white.

The ideas upon which this chart is based are not only in the main arbitrary, but also vague, and the execution of the sample examined by the author left much to be desired. We can not regard this colour-chart as a true step toward a philosophical classification of colours, but rather as a more elaborate repetition of the work of Mayer, Lambert, and Runge. In point of fact, our knowledge of colour and our means of experimenting on it are not at present sufficiently advanced to enable us even to propose a plan for a truly philosophical classification, and between the proposal and its execution there would be many weary steps. Hence, the matter contained in this chapter and its appendix is rather to be regarded as setting forth the problem than as attempting its solution.

APPENDIX TO CHAPTER XIV.

COLOUR-DIAGRAMS.

FOLLOWING a suggestion of Newton's, Maxwell constructed a diagram in which the colours of pigments and many natural objects can be laid down in accordance with certain principles and assumptions presently to be explained. Now, although some of the assumptions are arbitrary, yet if they are accepted a chart is obtained which presents many valuable features for the student of colour. The nature and scope of this colour-diagram will perhaps best be made evident by tracing the actual construction of one as made by the present writer.

Following Maxwell, vermilion, emerald-green, and artificial ultramarine-blue were assumed as the three fundamental colours, and positions at the three angles of an equilateral triangle assigned to them. The length of each side of the triangle was 200 divisions of the scale employed. The first step was to determine the position of white in the triangle. For this purpose disks of vermilion, emerald-green, and ultramarine were combined as shown in Fig. 101, smaller central disks of black and white being placed on the

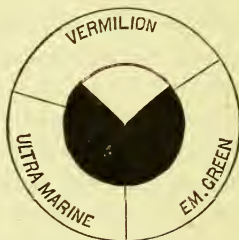


FIG. 101.—Compound Disk of Vermilion, Emerald-green, Ultramarine, White and Black, arranged for the production of Grey.

same axis. It was found, when the colours were mixed by rapid rotation, that 36·46 parts of vermilion, with 33·76 of emerald-green and 29·76 of ultramarine, gave a grey similar to that obtained by mixing 28·45 parts of white with 71·55 of black. In the experiment 24·5 parts of white were actually obtained; but this was cor-

rected by adding to it the white due to the black disk, it having been previously ascertained that, if the luminosity of the white paper composing the white disk was taken as 100, that of the black disk was 5·24. The same correction was made in all the cases that follow. The equation then reads:

$$36\cdot46 \text{ R} + 33\cdot76 \text{ G} + 29\cdot76 \text{ B} = 28\cdot45 \text{ W} \dots\dots(1).$$

The next step is to divide up the line R G, Fig. 103, in the ratio of 36·46 to 33·76:

$$(36\cdot46 + 33\cdot76) : 36\cdot46 :: 200 : 103\cdot5.$$

That is, if we mix vermilion and emerald-green in the proportion of 36·46 to 33·76, the mixture-point (*a*) lies on the line R G, and is 103·5 divisions distant from G, Fig. 103. This point is the position of the complement of the fundamental ultramarine, B. We now connect this point (*a*) with B by a straight line, find the length of the line to be 173·5 divisions, and seek the mixture-point of 36·46 R + 33·76 G and 29·76 B, which is obtained by the following proportion:

$$[(36\cdot46 + 33\cdot76) + 29\cdot76] : 29\cdot76 :: 173\cdot5 : 51\cdot64.$$

This mixture-point is the position of white; for vermilion, emerald-green, and ultramarine, when mixed in the above proportions, produce white. Hence, white (W, Fig. 103) will be on the line *a* B, 51·64 divisions from *a*. (It evidently must be somewhere on this line, for at the two extremities of the line are colours which are complementary, and there must be a mixture-point on the line which is white.) It will be noticed that in this proceeding the colours have been heated, according to Newton's suggestion, as though they were weights acting on the ends of lever-arms, and these arms have been taken of such lengths as to bring the system into equilibrium. It will also be observed that it has been assumed that the pigments, vermilion, emerald-green, and ultramarine, have the same intensity, or that equal areas of them have the same weight. Thus, 36·46 parts of vermilion and 33·76 of emerald-green, acting on a lever-arm 51·64 divisions in length, balance 29·76 parts of ultramarine acting on an arm with a length of 121·86 divisions. The lever-arms of the vermilion and emerald-green passing through W are also similarly balanced, and the whole system is in equilibrium.

The white or grey which was obtained in equation (1) was the

equivalent of 100 parts of colour; by multiplying 28·45 by 3·51 we obtain 100, and we set these 100 grey units in the place of 28·45 W in equation (1), and obtain what Maxwell calls the corrected value of the white. The factor 3·51 is called the coefficient of the white, and is used to establish a relation between equation (1) and those that follow. The coefficients of vermilion, emerald-green, and ultramarine have at the outset been assumed as 1, and hence in its corrected form equation (1) reads thus:

$$36\cdot46 R + 33\cdot76 G + 29\cdot76 B = 100 w \dots\dots(2).$$

We have now laid down upon our colour-diagram the position of our three fundamental colours and that of white, and are prepared to assign positions to all other pigments or mixtures of pigments. For example, to determine the position of pale chrome-yellow, a disk covered with this pigment is to be combined with disks of emerald-green and ultramarine, and set in rotation (Fig.

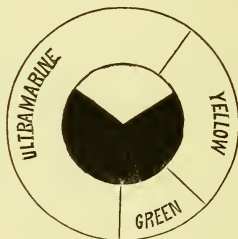


FIG. 102.—Compound Disk of Chrome-yellow, Emerald-green, Ultramarine, White, and Black, arranged so as to give a pure Grey by rotation.

102). This experiment was made, and the following equation obtained:

$$26\cdot9 Y + 12\cdot5 G + 60\cdot6 B = 32\cdot4 W + 67\cdot6 b \dots\dots(3).$$

Before using equation (3), it is necessary to bring it into relation with equation (2), and the first step is to express the value of the white in the same manner as in equation (2), viz.: we multiply it by the coefficient 3·51, and obtain in this way the value of the corrected white, or 113·87. This quantity we substitute in equation (3), which then reads:

$$26\cdot9 Y + 12\cdot5 G + 60\cdot6 B = 113\cdot87 w \dots\dots(4).$$

We must now introduce a corrected value for the chrome-yellow, so arranged that we shall have the same number of units, grey or coloured, on both sides of the sign of equality :

$$113.87 - (60.6 + 12.5) = 40.77.$$

40.77 is then the corrected value of the chrome-yellow, and equation (3) in its corrected form finally reads :

$$40.77 Y + 12.5 G + 60.6 B = 113.87 w. \dots (5).$$

To obtain the coefficient of the chrome-yellow, we divide the corrected value by the original value :

$$\frac{40.77}{26.9} = 1.51 = \text{coef. of ch.-yel.}$$

We are now prepared to determine the position of chrome-yellow in the diagram. We divide the line B G into two parts having the ratio of 12.5 to 60.6 :

$$(12.5 + 60.6) : 12.5 :: 200 : 34.2.$$

The position, then, of the complement of chrome-yellow is on the line B G, Fig. 103, at the spot marked cobalt, and is distant from B by 34.2 divisions; the distance of this point from W is found by measurement to be 94.1 divisions. We connect the point by a straight line with W, and produce the line some distance beyond; the position of chrome-yellow will be on this line, and may be found by the following proportion: Weight of chrome-yellow : weight of emerald-green and ultramarine :: distance of emerald-green and ultramarine : distance of chrome-yellow; or,

$$40.77 : (60.6 + 12.5) :: 94.1 : 168.7.$$

Chrome-yellow is consequently distant from the neutral point or white 168.7 divisions; we insert it in the diagram along with its coefficient 1.51. By a corresponding process the positions and coefficients of a number of the more ordinary colours have been laid down in the diagram. See Fig. 103. If the diagram is examined, it will be found that along any single radius the pale colours, or those mixed with much white, are located nearer W than those that are more free from such admixture; it will also be noticed that the more luminous colours have higher coefficients. By the aid of this diagram we obtain relative measures of the luminosity and saturation of colours on the same or on closely adjacent radii; the

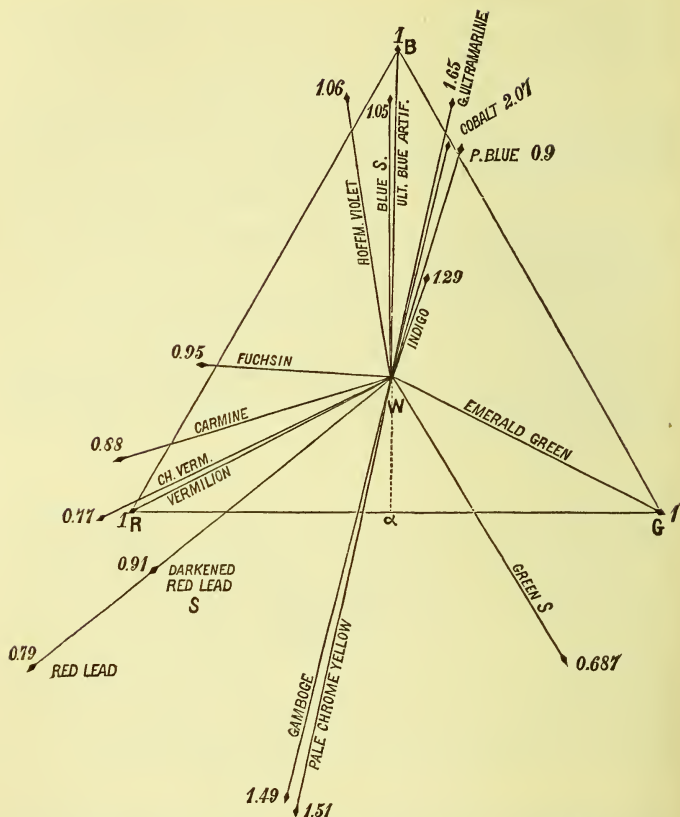


FIG. 103.—Maxwell's Colour-Diagram as constructed by O. N. R.

colours also have angular positions assigned to them, so that they are fairly defined as to angular position, intensity, and greater or less freedom from white.

It is, however, to be remarked that the construction rests upon several more or less arbitrary assumptions, as: 1. That vermilion, emerald-green, and ultramarine-blue really correspond to the three fundamental colours. If we substitute in place of them other colours, such as red lead, grass-green, and violet, we obtain different

angular positions for all the colours afterward introduced, and also different coefficients. 2. The assumption that vermilion, emerald-green, and ultramarine have the same intensity or the same coefficient is quite unwarranted, the intensity of emerald-green being evidently greater than that of ultramarine-blue. From this it follows that the coefficients and distances from the central white, W, are not comparable along different radii.

The author has reconstructed the same colour-diagram, introducing coefficients which represent the actual luminosities of the three fundamental colours. These coefficients were obtained by the method described in Chapter III. Vermilion, emerald-green, and artificial ultramarine-blue were, as before, assumed as the fundamental colours, and placed at the three angles of an equilateral triangle. Taking the luminosity of white paper as 100, the luminosities of the three pigments were as follows: Vermilion, 26·85; emerald-green, 48·58; ultramarine-blue, 7·57. Introducing these coefficients into equation (1), it becomes:

Vermilion.	Emerald-green.	Ultramarine.	White.
(26·85 × ·3646)	+ (48·58 × ·3376)	+ (7·57 × ·2976)	= 28·44.

That is:

$$9·8 \text{ verm.} + 16·4 \text{ em.-green} + 2·2 \text{ ult.} = 28·44 \text{ white.} \dots (6).$$

With the aid of equation (6), the position of white was determined in the manner previously employed, and found to be that indicated in Fig. 104, being only 13·55 divisions distant from the line V G. Making use of equation (3), the coefficient of chrome-yellow was determined as indicated below, X being this quantity:

$$(48·58 \times ·125) + (X \times ·269) + (7·57 \times 0·606) = 32·4.$$

$$X = 80·82.$$

We then have—

$$6·072 \text{ em.-green} + 21·74 \text{ ch.-yel.} + 4·587 \text{ ult.} = 32·4. \dots (7).$$

With the aid of this last equation the position of chrome-yellow can be laid down in the manner previously described. In Fig. 104 the positions of the same pigments are shown which were employed in the first colour-diagram, Fig. 103; and it will be noticed that white has been moved toward the line R G, and that the angular positions of the colours have been considerably altered. In this second colour-diagram the coefficients of pigments situated along different

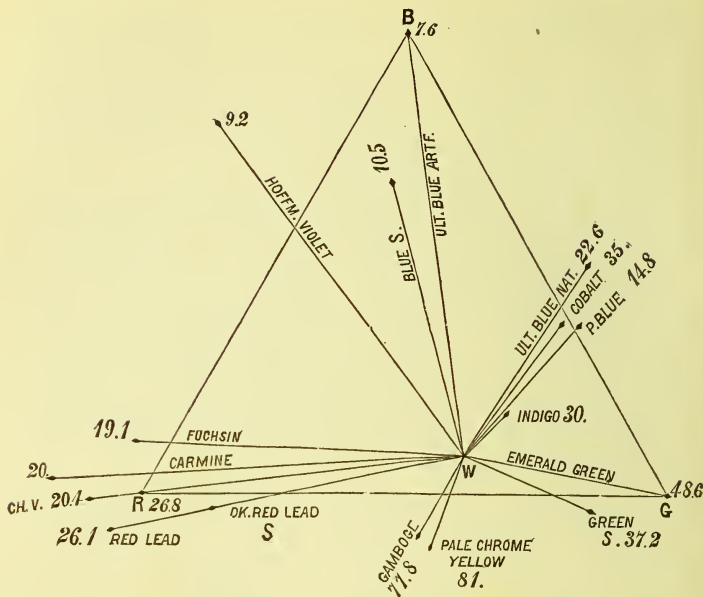


FIG. 104.—Maxwell's Diagram as reconstructed by the Author, correct Coefficients being employed.

radii are comparable with each other, since they represent the luminosities of the pigments compared with that of white paper taken as 100.

The author has constructed a new kind of colour-diagram, in which the colours are arranged in a different manner from those just described.

Idea of the New Diagram.—Let us suppose that we take a certain quantity of pure red light and locate it on the circumference of a circle at R, Fig. 105, and draw the diameter R G B, and at the point G B locate a quantity of pure green-blue light, just sufficient to neutralize the red light, or form with it a mixture which appears to the eye white. The position of white will then be at the centre of the circle, or at W. The red and green-blue light employed will be considered equal in intensity, though in actual luminosities they

may differ considerably; they will, in point of fact, relatively to each other, have equal saturating powers. We next lay down on the circumference at Y a certain amount of pure yellow light, draw the diameter Y B, Fig. 105, and at B locate an amount of blue light

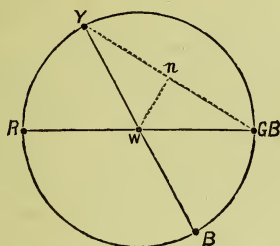


FIG. 105.

just sufficient to neutralize it, arranging matters so that the yellow and blue light when mixed shall reproduce a white identical in luminosity with that furnished by the mixture of the red and green-blue. The yellow and blue will differ greatly in luminosity, but, as they neutralize each other, will be considered to have equal intensity. *Each* of the four colours will also be considered to have equal intensity in the sense in which the word has just been employed; or, instead of using the term intensity, we may say that each of the four colours will have corresponding powers of saturation. The same will be true of any other colours belonging on the circumference. In order to realize this idea, and to obtain means of assigning to the colours proper angular positions, some other considerations must be entertained. Suppose we mix the yellow located at Y with the green-blue located at G B: we shall by varying the proportions finally obtain a mixture which, although it is not white, yet will be paler or more whitish than any other mixture; this, of course, is a well-known fact. In the practical construction of the diagram, it is assumed that this most neutral mixture will be obtained when the whole mass of the yellow at Y is mixed with the whole mass of green-blue at G B; and it is evident that, even if this assumption is not strictly true, it will approximate to the truth just in proportion as the angular distance between R and Y happens to be a small quantity. If the angular distance between R and Y is a large quantity, the assumption may or may not hold good;

at present we have no means of deciding this point. We will take it for granted till the contrary is proved, and from n , the most neutral point, we draw a perpendicular; it will pass through the centre of the circle, or through the position of white. The same will hold good when any other point not far distant from R is connected by a straight line with $G B$; here also a perpendicular drawn from the most neutral point will pass through white.

Realization of the Diagram.—In order to construct this diagram it is necessary to prepare three coloured disks having equal intensities, in the sense above employed, or equal saturating powers. These disks must also have such colours that by optical mixture they may be capable of furnishing white light. The colours selected were red lead, a grass-green, and artificial ultramarine-blue. The green disk was combined with the blue disk, and, by a rather elaborate series of experiments, it was ascertained that the most neutral mixture was obtained when equal areas were optically mixed, from which it was concluded, according to the fundamental assumption, that the saturating powers of the two disks were equal. After several trials, a similar equality was established between the green disk and one painted with slightly darkened red lead. These disks when combined gave the following equation :

$$23\cdot06 \text{ red lead} + 42\cdot16 \text{ green} + 34\cdot76 \text{ blue} = 22\cdot1 \text{ white.}$$

The coefficients of the three colours were taken as unity, since the colours had equal saturating powers. The relative areas of the colours in the above equation were then used as weights, and furnished the means of determining the positions of the three colours on the circumference of a circle in which white was placed at the centre. This was accomplished by placing the three colours at such angular distances apart as brought the whole system into equilibrium; for example, if the weights had been equal, the angular distance of the three points would have been 120° . The proper angular distances being now laid down, the positions of darkened red lead, grass-green, and ultramarine were determined; and with their aid the positions of other pigments could be ascertained by the process of mixture previously explained. (See Fig. 106.) The points laid down in this diagram indicate colour or hue by angular position, and saturation or intensity by greater or less distance from W . The relative amounts of white light reflected by the pigments situated on any particular radius can easily be determined, since distance

from the centre measures the amount of coloured light reflected, and the total amount of coloured and white light reflected can be measured by the process described in Chapter III. We have, however, at present no means of generalizing this process and applying

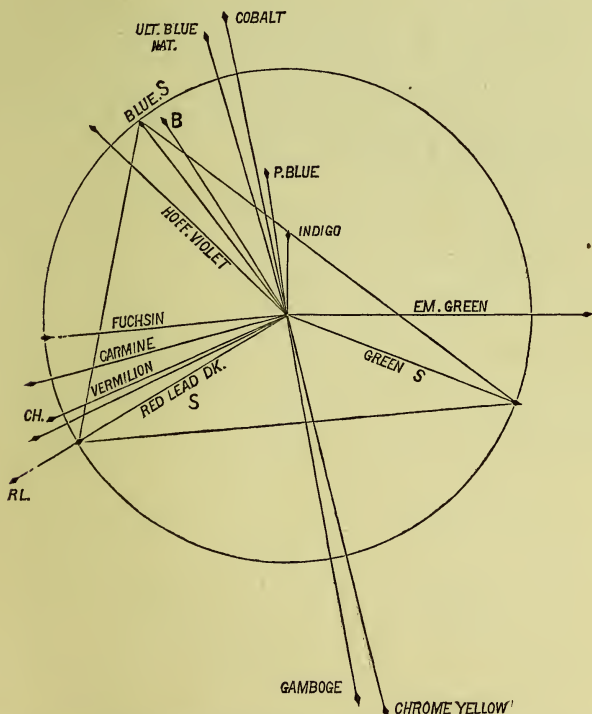


FIG. 106.—Saturation-Diagram according to Roed. The three colours used in its construction are marked S.

it to colours situated on different radii, since we have not the power of ascertaining, for example, whether our standard yellow disk at Y reflects the same amount of *white* light with the standard red disk at R, or more or less; we know that they reflect corresponding quantities of coloured light, but nothing more. Before we can

solve this problem it will be necessary for us to know the relative luminosity of all the pure colours (free from white light) which, according to the construction, fall on the circumference of the circle, and this could only be ascertained by an especial study of the spectral colours with reference to this point; but no such study has yet been made. We know that corresponding amounts of yellow and greenish-yellow have not only higher degrees of luminosity than their complements, blue and violet, but even higher than any of the other colours; but thus far no quantitative determinations have been made. Fig. 106 exhibits a diagram of the kind just described, containing the same colours or pigments previously employed: it is perhaps best called a saturation-diagram.

CHAPTER XV.

CONTRAST.

WE have now studied with some care the changes which coloured surfaces experience when viewed under various kinds of illumination, or when modified in appearance by the admixture of more or less white or coloured light. The appearance which a coloured surface presents to us can, however, be altered very materially by a method which is quite different from any of those that have thus far been mentioned: we can actually change colour to a considerable extent without at all meddling with it directly, it being for this purpose only necessary to alter the colour which

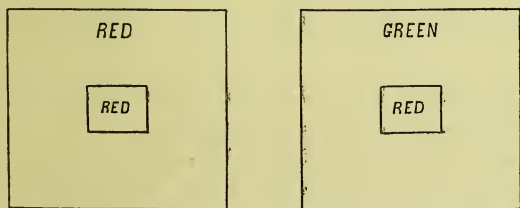


FIG. 107.—Sheets of Red and Green Paper with Red Squares.

lies adjacent to it. We can satisfy ourselves of this fact by a very simple experiment. If we cut out of a sheet of red paper two square pieces an inch or two in size, and then place one of them on a sheet of red and the other on a sheet of green paper, as indicated in Fig. 107, it will be found that the red square on the red paper will not appear nearly so

brilliant and saturated in colour as that placed on the green ground, so that the observer will be disposed to doubt whether the two red squares are really identical in hue. By a somewhat analogous proceeding we can cause a surface which properly has no colour of its own, which is really grey, to appear tinted red, blue, green, etc. These changes and others of a like character are produced by what is called contrast, and are partly due to actual effects generated in the eye itself and partly to fluctuations in the judgment of the observer. The subject of contrast is so important that it will be worth while to make a somewhat careful examination of the laws which govern it; and for

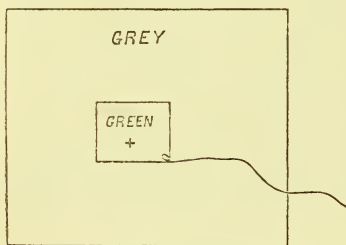


FIG. 108.—Grey Paper with Green Slip.

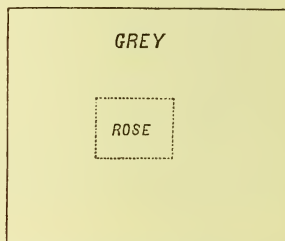


FIG. 109.—Grey Paper with Rose-coloured Image.

this purpose it will be well for the reader to repeat some of the simple experiments described below.

If we place a small piece of bright-green paper on a sheet of grey drawing-paper, in the manner indicated in Fig. 108, and then for several seconds attentively look at the small cross in the centre of the green slip, we shall find, on suddenly removing it, that in its place a faint image of a rose-red colour makes its appearance, Fig. 109. This red image presently vanishes, and the grey paper resumes its natural appearance. The rose-red ghost which is thus developed has a colour which is complementary to that which called it into existence, and this will also be the case if we

employ little squares of other colours : red will give rise to a greenish-blue image, blue to a yellow, violet to a greenish-yellow, etc., the colour of the image being always complementary to that which gave rise to it. On this account these images are called *negative*, since, as far as colour goes, they are just the reverse of the images which are first presented to the eye of the observer. They are also often spoken of in older treatises on optics as "the accidental colours." It is quite easy to explain their production with the aid of the theory of Young and Helmholtz. Let us take as an example the experiment just described. According to our theory, the green light from the little square of paper, acting on the eye, fatigues to some extent the green nerves of the retina, the red and violet nerves meanwhile not being much affected. When the green paper is suddenly jerked away by the string, grey light is presented to the fatigued retina, and this grey light may be considered to consist, as far as we are concerned, of red, green, and violet light. The red and violet nerves, not being fatigued, respond powerfully to this stimulus ; the green nerves, however, answer this new call on them more feebly, and in consequence we have presented to us mainly a mixture of the sensations red and violet, giving as a final result rose-red or purplish-red. The green nerves, of course, are not so fatigued that they do not act at all when the grey light is presented to them, but the only effect that their partial action has is to render the rose-coloured image somewhat pale or whitish in appearance. The fatigue of the optic nerve mentioned here does not differ essentially from that which it undergoes constantly, even under the conditions of ordinary use, where the waste is continually made good by the blood circulating in the retina, and by the little intervals of rest frequently occurring. In our experiment we have merely confined the fatigue to one set of nerves, instead of distributing it equally among the three sets.

The above experiments and explanation will enable us

easily to comprehend the more complicated case, where, instead of placing our little green square on grey, we lay it on a sheet of coloured paper. Instead, then, of grey, let us take yellow paper, placing the green square on it as before, Fig. 110. On suddenly withdrawing the green square, we find it replaced by an orange-coloured ghost, Fig. 111,

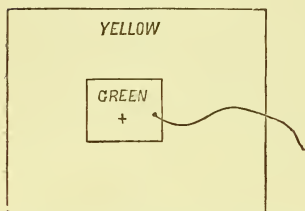


FIG. 110.—Yellow Ground with Green Slip.

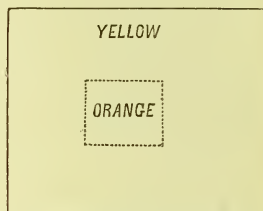


FIG. 111.—Yellow Ground with Orange-coloured Image.

which we account for thus: As before, the green nerves are fatigued, the red and violet nerves remaining fresh; when the square is removed, yellow light is presented to the retina, and this yellow light, as explained in Chapter IX., tends to act on the red and green nerves equally; but the green nerves in the present case do not respond with full activity, hence the action is more confined to the red nerves, and, as explained in Chapter X., the resultant tint is necessarily orange—that is to say, we have a strong red sensation mingled with a weak green sensation, and the result is the sensation called orange. In this experiment the violet nerves do not come into play to any great extent. If the green square is placed on a blue ground, the image becomes violet, for the reason that the blue light which is presented to the fatigued retina acts, as explained in Chapter IX., on the green and violet nerves; but the green nerves being fatigued, the action is mostly confined to the violet nerves, and hence the corresponding sensation. In this case the red nerves hardly come into play at all.

It follows from the above examples and reasoning that the final effect is, that we obtain as an after-image what amounts to a mixture of the *complementary* colour of the small square with the colour of the ground ; and, by recollecting this, we can easily retain this class of facts in the memory.

There is another similar experiment which is simpler than those just described, but which is nevertheless instructive. A small square of black paper is to be placed on a sheet of red paper, and the attention in this case is to be directed to a mark on the edge of the former. (See Fig. 112.) When the black square is suddenly removed, the ob-



FIG. 112.—Red Ground with Black Paper.

server sees in place of it a more luminous spot, which in the case before us will of course be red ; but what is remarkable is the circumstance that this red image will be more intense or saturated in colour than the rest of the ground. The rest of the sheet of red paper will look as though grey had been mixed with its colour, Fig. 113. This experiment will of course succeed with paper of any bright colour, and Helmholtz has found that the same effects can be obtained with the pure colours of the prismatic spectrum. The explanation, according to our theory, runs about thus : While we are in the act of looking at the edge of the black square, red light is passing into the eye, and is

fatiguing all those portions of the retina that are not protected by the presence of the black square ; it thus happens that the ability of the larger portion of the retina to receive the sensation of red is considerably diminished ; the ability of the protected portion of course suffers no such change.

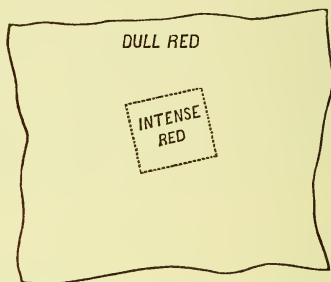


FIG. 113.—Red Ground with Intense Red Image

When the black square is suddenly removed, the unfatigued portion of the retina receives a powerful impulse from the red surface, but the effect produced on the rest of the retina is inferior in degree. This accounts for the fact that the image of the square is brighter or more luminous ; and we can easily understand why it is at the same time more intense, or saturated in colour, if we remember, as explained in Chapter IX., that red light excites into action not only the red nerves, but to a less extent the green and violet nerves. Now, as the red nerves begin to be fatigued, the action of the other two sets will be relatively more powerful than at first, so that gradually the sensations of green and violet begin to add themselves to that of red (or, what is the same thing, the sensation of white mingles itself with that of red), and the red colour of the paper looks a little greyish. The success of the experiment with the pure colours of the prismatic spectrum, which contain no white, is easily accounted for by the explanation just given.

This matter can be pushed even further if, instead of

employing a black square, we take one which has a colour complementary to that of the ground. We substitute then for the black square one coloured with emerald-green, and repeat the experiment. (See Fig. 114.) The result is much the same as before, except that the red ghost is now still more intense or saturated in colour, Fig. 115. When the

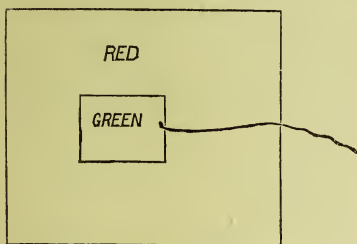


FIG. 114.—Blue-green Slip on Red Ground.

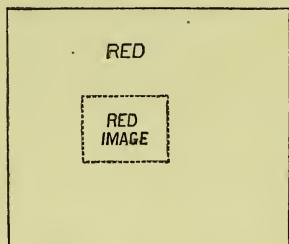


FIG. 115.—Intense Red Image on Red Ground.

experiment is made in this way we accomplish two objects : first, we protect a small portion of the retina from red light, so that it may be very sensitive to this kind of light afterward ; second, we fatigue the green and violet nerves of this portion by presenting to them bluish-green light, so that afterward the red light from the red paper will be unable to stimulate them even in a small degree ; hence the sensation that we receive is that of pure red, the action of the green and violet nerves being excluded.

All these phenomena are cases of what is called successive contrast, because we look in succession from one surface to another. When coloured surfaces are placed near each other and compared in a natural manner, successive contrast plays an important part, and the appearance of the colours is more or less modified according to its laws. If we attempt to confine our attention to only one of the coloured surfaces, this still holds good ; for the eye involuntarily wanders to the other, and to prevent this requires a

good deal of careful practice, for fixed vision is quite opposed to our natural habit. It follows from this that, in the natural use of the eye, the negative images, although present to some extent, are not sharp and distinct, and hence usually remain unobserved by persons not trained to observations of this character. Nevertheless these images modify to a considerable extent the appearances of coloured surfaces placed near each other, and the *changes* of hue are visible enough to the most uneducated eye.

One of the most common cases belonging here is represented in Fig. 116. We have a grey pattern traced on a

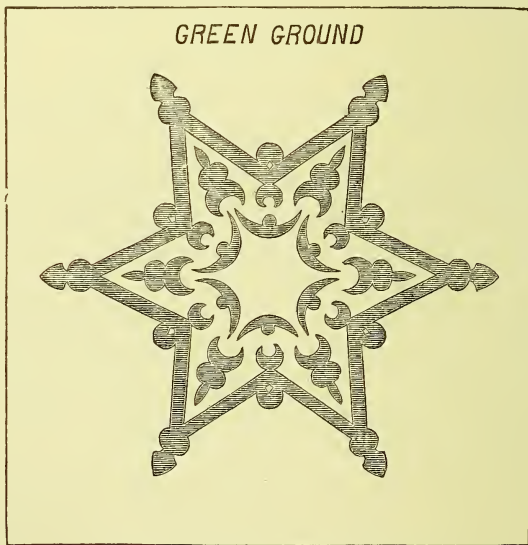


FIG. 116.—Grey Figure on a Green Ground.

green ground ; the tracery, however, will not appear pure grey, but tinged with a colour complementary to that of the ground—that is, reddish. We can, of course, substitute for the green any other bright colour, and it will al-

ways be found that the grey is more or less tinged with the complementary hue. As black is really a dark grey, we should expect to find it also assuming to some extent a colour complementary to that of the ground ; and this is indeed the case, though the effect is not quite so marked as with a grey of medium depth. Chevreul, in his great work on the simultaneous contrast of colours, relates an anecdote which illustrates the matter now under consideration. Plain red, violet-blue, and blue woven stuffs were given by certain dealers to manufacturers, with the request that they should ornament them with black patterns. When the goods were returned, the dealers complained that the patterns were not black, maintaining that those traced on the red stuffs were green, on the violet dark-greenish yellow, and on the blue copper-coloured. Chevreul covered the ground with white paper in such a way as to expose only the pattern, when it was found that its colour was truly black, and the effects which had been observed were entirely due to contrast. The remedy in such cases is not to employ pure black, but to give it a tint a little like that of the coloured ground, taking care to make it just strong enough to balance the hue generated by contrast. If we substitute a white pattern for the black, something of this same effect can often be observed, but it is less marked than with grey or black. In cases like those now under consideration the contrast is stronger when the coloured surface is bright and intense or saturated in hue. The effect is also increased by entirely surrounding the second colour with the first ; the circumscribing colour ought also to be considerably larger than its companion. When these conditions are observed, the effect of contrast is generally noticeable only on the smaller surface, the larger one being scarcely affected.

When, on the other hand, the two coloured surfaces are about equal in extent, then both suffer change. If it is desired to produce a strong effect of contrast, the coloured surfaces must be placed as near each other as possible.

This is beautifully illustrated in one of the methods employed by Chevreul in studying the laws of contrast. Two coloured strips were placed side by side in contact, as shown in Fig. 117, duplicate strips being arranged in the field of

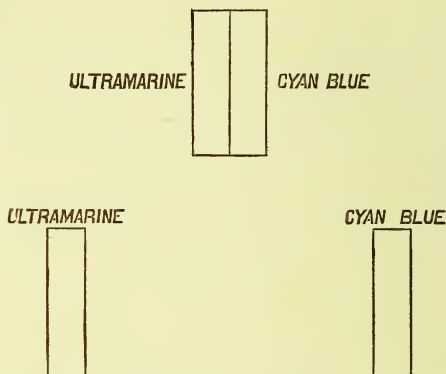


FIG. 117.—Arrangement to show the Effects of Simultaneous Contrast, half size.

view at some distance from each other. The tints of the two central strips were both altered; those placed at a greater distance apart suffered no change. In the experiment represented in Fig. 117 the central ultramarine by contrast is made to appear more violet in hue, the central cyan-blue more greenish; the colour of the outlying strips is scarcely affected. In this experiment we have an application of the rule above given for determining the changes which colours experience under the influence of contrast. The rule is quite simple; its application, however, involves a knowledge of the colours which are complementary to each other, as well as of the effects produced by mixing together masses of coloured light. According to our rule, when two coloured surfaces are placed in contiguity, each is changed as though it had been mixed to some extent with the complementary colour of the other. In the example before us the ultramarine becomes more of a violet-blue,

because it is mixed, or seems to be mixed, with the complementary colour of cyan-blue—that is, with orange. The cyan-blue appears more greenish, because it is virtually mixed with greenish-yellow, which is the complementary colour of ultramarine. As it requires a little consideration to predict the changes which colours undergo through contrast, we give below a table containing the most important cases :

Pairs of Colours.	Change due to Contrast.	
{ Red.....	Becomes more	purplish.
{ Orange.....	“	“ yellowish.
{ Red.....	“	“ purplish.
{ Yellow.....	“	“ greenish.
{ Red.....	“	“ brilliant.
{ Blue-green.....	“	“ brilliant.
{ Red.....	“	“ orange-red.
{ Blue.....	“	“ greenish.
{ Red.....	“	“ orange-red.
{ Violet.....	“	“ bluish.
{ Orange.....	“	“ red-orange.
{ Yellow.....	“	“ greenish-yellow.
{ Orange.....	“	“ red-orange.
{ Green.....	“	“ bluish-green.
{ Orange.....	“	“ brilliant.
{ Cyan-blue.....	“	“ brilliant.
{ Orange.....	“	“ yellowish.
{ Violet.....	“	“ bluish.
{ Yellow.....	“	“ orange-yellow.
{ Green.....	“	“ bluish-green.
{ Yellow.....	“	“ orange-yellow.
{ Cyan-blue.....	“	“ blue.
{ Yellow.....	“	“ brilliant.
{ Ultramarine-blue.....	“	“ brilliant.
{ Green.....	“	“ yellowish-green.
{ Blue.....	“	“ purplish.
{ Green.....	“	“ yellowish-green.
{ Violet.....	“	“ purplish.
{ Greenish-yellow.....	“	“ brilliant.
{ Violet.....	“	“ brilliant.
{ Blue.....	“	“ greenish.
{ Violet.....	“	“ purplish.

It is easy and instructive to study the changes produced by contrast with the aid of a chromatic circle, Fig. 118, and it

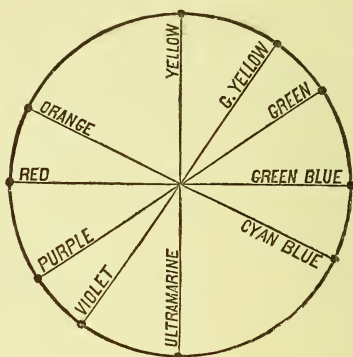


FIG. 118.—Chromatic Circle.

will be found that alterations in colour produced by contrast obey a very simple law: When any two colours of the chromatic circle are brought into competition or contrasted, the effect produced is apparently to move them both farther apart. In the case, for example, of orange and yellow, the orange is moved toward the red, and assumes the appearance of reddish-orange; the yellow moves toward the green, and appears for the time to be greenish-yellow. Colours which are complementary are already as far apart in the chromatic circle as possible; hence they are not changed in hue, but merely appear more brilliant and saturated. This is indeed the effect which a strict application of our rule leads to: the two colours are to be moved farther apart; they are already situated on the opposite extremities of a diameter of the circle, and, if they are to recede still farther from each other, they can accomplish this in no other way than by moving outside of the circumference of the circle; but this corresponds, as explained in the previous chapter, to an increase of saturation. If the

experiments indicated in the table are carefully repeated, it will be found that all the pairs of colours there enumerated are not equally affected by contrast. The *changes* of tint are greatest with the colours which are situated nearest to each other in the chromatic circle, and much less with those at a distance. Thus both red and yellow are much changed by contrast, the red becoming purplish, the yellow greenish ; while red with cyan-blue or blue is much less affected in the matter of displacement or change of hue. On the other hand, the colours which are distant from each other in the chromatic circle, while suffering but slight changes in hue, are made to appear more brilliant and saturated ; that is, they are virtually moved somewhat outside of the circle, the maximum effect taking place with colours which are complementary.

Colours which are identical are affected by contrast in exactly the opposite way from those which are complementary ; that is, they are made to appear duller and less saturated. The author finds that these and other effects of contrast can be studied with great advantage by the aid of two identical chromatic circles laid down on paper. One set of these lines should be traced on a sheet of transparent paper, which is afterward to be placed over the companion circle. The use of these circles will best be made evident with the aid of an example. Let us suppose that we wish to ascertain with their aid the effect produced by red, as far as contrast goes, on all the other colours, and also on red itself. We place the transparent circle on its companion, so that the two drawings may coincide in position, and we then move the upper circle along the diameter joining red and green-blue some little distance, so that the two circles no longer have the same common centre. We then transfer the points marked red, orange, yellow, etc., on the upper circle, by pricking with a pin, to the lower circle, and these pin-marks on the lower circle will indicate the changes produced on all the colours by competition with red. Fig.

119 gives the result. The stars on the dotted circle represent the new positions of the different colours when contrasted with red. If we examine them we find that red when contrasted with greenish-blue causes this last colour to move away from the centre of the circle in a straight line ; hence, as the new point is on the same diameter, but farther from the centre, we know that the greenish-blue is is

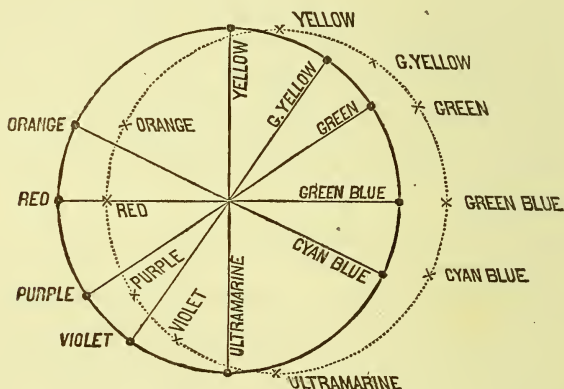


FIG. 119.—Chromatic Circle displaced by Contrast, showing the effects produced by the red on the other colours.

not made more or less blue or green, but is simply caused to appear more saturated or brilliant. The new point for the red lies also on the same diameter, but is nearer to the centre of the circle ; that is, the colour remains red, but appears duller or less saturated. Experience confirms this. If a considerable number of pieces of red cloth, for example, are examined in succession, the last one will appear duller and inferior in brilliancy to the others, but it will still appear red. Proceeding with the examination of the effects produced on the other colours, we find that orange has been moved toward yellow, and also toward the centre of the circle ; hence our diagram tells us that red, when put into competition with orange, causes the latter to appear

more yellowish and at the same time less intense. Advancing along the circumference of the circle, our diagram informs us that yellow is not much affected in the matter of saturation or intensity, but is simply made to appear more greenish. The two circles during superposition cut each other near the position of yellow ; from this point onward the effect changes as far as intensity or saturation is concerned, the greenish-yellow being moved decidedly outside of the original circle, as well as toward the green ; it is made therefore, by contrast with red, to appear more brilliant as well as more greenish. Green is made to appear somewhat bluish, and more brilliant. Greenish-blue has been considered. Cyan-blue is made to appear slightly more greenish as well as much more brilliant ; the same is true of blue, though its increase in brilliancy by contrast with red is rather less than in the case with cyan-blue. Violet has its hue considerably altered toward blue ; its saturation is diminished. Purple is made to look more violet, and is much diminished in saturation. If we wish to study the effects produced on the colours of the chromatic circle by contrasting them with yellow, we have of course merely to displace the upper circle along the line joining yellow and its complement ultramarine-blue, and then proceed as before. The proper amount of displacement will of course not be very large, and can be approximately determined by experiment ; the upper circle, namely, is to be moved, so that the colours situated on either side of the points where the circles cut each other shall, in the diagram, Fig. 118, be made to suffer changes of *saturation* corresponding to the results of actual experiment.

It is quite evident that this contrast-diagram will furnish correct results only on condition that the colours in it are properly arranged ; if the angular positions of the colours are laid down falsely, the results, in the matter of increase or diminution of brilliancy or saturation, will also be false. The author has made many experiments to settle

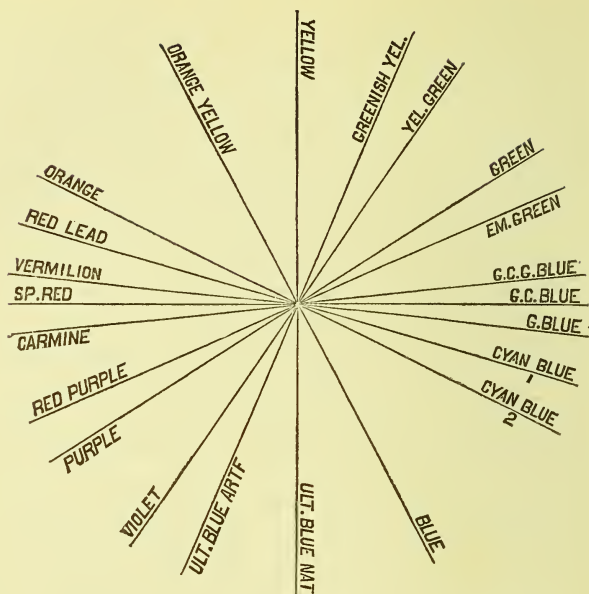


FIG. 120.—Contrast-Diagram according to O. N. Rood.

this question, and in Fig. 120 gives his result in the form of a diagram ; the same result is given below in the form of a table :

TABLE SHOWING THE DISTANCES OF THE COLOURS FROM EACH OTHER IN THE CONTRAST-CIRCLE, ACCORDING TO O. N. R.

	Angular Distances.
Pure red to vermillion.....	6°
Vermilion to red lead.....	10°
Red lead to orange.....	9°
Orange to orange-yellow.....	35°
Orange-yellow to yellow.....	28°
Yellow to greenish-yellow.....	23°
Greenish-yellow to yellowish-green.....	13°
Yellowish-green to green.....	22°

Green to emerald-green.....	10°
Emerald-green to very greenish blue, or to complement of carmine.....	18°

The hues of the papers employed in these experiments were determined with some degree of accuracy by comparing them with a normal spectrum nearly six times as long as that furnished by a single flint-glass prism, and at the same time brilliant and pure. (See Chapter III.) The following table gives the positions of these coloured papers in a normal spectrum, containing from A to H 1,000 equal parts; the corresponding wave-lengths are also given :

Coloured Papers.	Position in Normal Spectrum.	Wave-length in $\frac{1}{1000000}$ mm.
Spectral red (vermilion washed with carmine)	285	6562
Vermilion (English).....	387	6290
Red lead.....	422	6061
Orange.....	448	6000
Yellow (pale chrome).....	488	5820
Greenish-yellow.....	535	5649
Yellow-green.....	552	5587
Green.....	600	5411
Emerald-green.....	648	5236
Cyan-blue 2.....	715	4991
Ultramarine, natural.....	785	4735
Ultramarine, artificial.....	857	4472
Violet ("Hoffmann's violet B. B.").....	Rather more reddish than any violet in the spectrum.	

From the foregoing, then, it is evident in general that the effect of contrast may be helpful or harmful to colours : by it they may be made to look more beautiful and precious, or they may damage each other, and then appear dull, pale, or even dirty. When the apparent saturation is increased, we have the first effect ; the second, when it is diminished. Our diagram, Fig. 119, shows that the satura-

tion is diminished when the contrasting colours are situated near each other in the chromatic circle, and increased when the reverse is true. It might be supposed that we could easily overcome the damaging effects of harmful contrast by simply making the colours themselves from the start somewhat more brilliant ; this, however, is far from being true. The pleasure due to helpful contrast is not merely owing to the fact that the colours appear brilliant or saturated, but that they have been so disposed, and provided with such companions, that they are made to glow with *more* than their natural brilliancy. Then they strike us as precious and delicious, and this is true even when the actual tints are such as we would call poor or dull in isolation. From this it follows that paintings, made up almost entirely of tints that by themselves seem modest and far from brilliant, often strike us as being rich and gorgeous in colour ; while, on the other hand, the most gaudy colours can easily be arranged so as to produce a depressing effect on the beholder. We shall see hereafter that, in making chromatic compositions for decorative purposes or for paintings, artists of all times have necessarily been controlled to a considerable extent by the laws of contrast, which they have instinctively obeyed, just as children in walking and leaping respect the law of gravitation, though unconscious of its existence.

The phenomena of contrast, as exhibited by colours which are intense, pure, and brilliant, are to be explained to a considerable extent by the fatigue of the nerves, as set forth in the early part of the present chapter. The changes in colour and saturation become particularly conspicuous after somewhat prolonged observation, and are often attended with a peculiar soft glimmering, which seems to float over the surfaces, and, in the case of colours that are far apart in the chromatic circle, to lend them a lustrous appearance. Still, upon the whole, the effects of contrast with brilliant colours are often not strongly marked

at first glance, from the circumstance that the colours, by virtue of their actual intensity and strength, are able to resist these changes, and it often requires a practised eye to detect them with certainty. The case is quite otherwise with colours which are more or less pale or dark—that is, which are deficient in saturation or luminosity, or both. Here the original sensation produced on the eye is comparatively feeble, and it is hence more readily modified by contrast. In these cases the fatigue of the nerves of the retina plays but a very subordinate part, as we recognize the effects of contrast at the first glance. We have to deal here with what is known as simultaneous contrast, the effects taking place when the two surfaces are as far as possible regarded simultaneously. In the case of simultaneous contrast the changes are due mainly to fluctuations of the judgment of the observer, but little to the fatigue of the retinal nerves.

We carry in ourselves no standard by which we can measure the saturation of colour or its exact place in the chromatic scale; hence, if we have no undoubted *external* standard at hand with which to compare our colours, we are easily deceived. A slip of paper of a pale but very decided blue-green hue was placed on a sheet of paper of the same general tint, but somewhat darker and more intense or saturated in hue. The small slip now appeared pure grey, and by no effort of the reason or imagination could it be made to look otherwise. In this experiment no undoubted pure grey was present in the field of view for comparison, and in point of fact the small slip did actually approach a pure grey in hue more nearly than the large sheet; hence the eye instantly accepted it for pure grey. The matter did not, however, stop here. A slip of pure grey paper was now brought into the same green field, but, instead of serving as a standard to correct the illusion, it assumed at once the appearance of a *reddish*-grey. The pure grey really did approach reddish-grey more than the

green field surrounding it, and hence was accepted for this tint. The same pale blue-green slip, when placed on a pale-reddish ground, assumed a stronger blue-green hue than when on a white ground. In the first of these experiments we have an illustration of harmful and in the second of helpful simultaneous contrast. The result in both cases coincided with that which successive contrast would have produced under similar circumstances.

It has been stated above that the effects produced by simultaneous contrast are due not to retinal fatigue, but to deception of the judgment ; now, as the effects of simultaneous contrast are identical in kind with those generated by

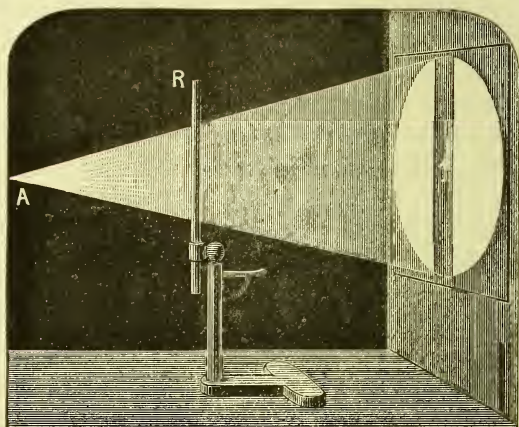


FIG. 121.—Shadow of Rod in Darkened Room.

successive contrast, it is evident that the statement needs some proof. This can be furnished with the aid of a beautiful experiment with coloured shadows. In making this experiment we allow white daylight to enter a darkened room through an aperture, A, arranged in a window, as indicated in Fig. 121. At R we set up a rod, and allow its shadow to fall on a sheet of white cardboard, or on the

white wall of the room. It is evident now that the whole of the cardboard will be illuminated with white light, except those portions occupied by the shadow 1. We then light the candle at C, Fig. 122 ; its light will also fall on

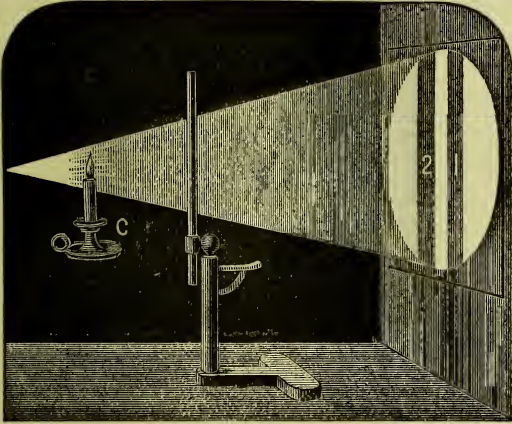


FIG. 122.—Shadows of Rod, using Daylight and Candle-light.

the cardboard screen, and will then cast the shadow 2 ; that is, the candle-light will illuminate all parts of the screen except those occupied by the shadow 2 ; this portion will be illuminated with pure white light. Instead, however, of appearing to the eye white, the shadow 2 will seem to be coloured decidedly *blue*. For the production of the most powerful effect, it is desirable that the shadows should have the same depth, which can be effected by regulating the size of the aperture admitting daylight. Now, although the shadow cast by the candle is actually pure white, yet, by contrast with the surrounding orange-yellow ground, it is made to appear decidedly blue. So strong is the illusion that, even after the causes which gave rise to it have disappeared, it still persists, as can be shown by the following experiment of Helmholtz : While the coloured shadows are

falling on the screen, they are to be viewed through a blackened tube of cardboard, held in such a way that the observer has both the shadows in his field of view; the appearance then will be like that represented in Fig. 123.

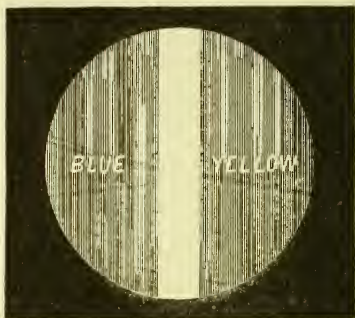


FIG. 123.—Blue and Yellow Shadows viewed through a Tube.

After the blue shadow has developed itself in full intensity, the tube is to be moved to the left, so that the blue shadow may fill the whole field. The tube being held steadily in the new position, the shadow will still continue to appear blue instead of white, even although the exciting cause, viz., the orange-yellow candle-light, is no longer acting on the eye. The candle may be blown out, but the surface will still appear blue as long as the eye is at the tube. On removing the tube, the illusion instantly vanishes, and it is perceived that the colour of the surface is identical with that of the rest of the screen, which is at once recognized as white. In a case like this the fatigue of the retinal elements can play no part, as the illusion persists during a far longer period of time than is necessary for their complete rest; we must hence attribute the result to a deception of the judgment. Expressing this in the language of Young's theory, we say that the sensation of white is produced when the three sets of nerves, red, green, and violet, are

stimulated to about the same extent ; but that nevertheless, as we have in ourselves no means of judging with certainty about this equality of stimulation, we may under certain circumstances be induced to accept an unequal for an equal stimulation, or the reverse. In the experiment with the coloured shadows we had before us in the shadow due to the candle-flame an equal stimulation, which by contrast we were in the first instance induced to accept as unequal, and the judgment afterward obstinately persisted in the error till it was corrected and took a new departure.

This experiment may be modified and extended by the use of coloured glasses instead of a candle-flame. The window is to be provided with two apertures, one of which is to be covered with a piece of stained glass, through which sunshine will be admitted to the darkened room ; the other aperture will admit white light, as before. If red glass be employed, the colour of the shadows will appear red and greenish-blue. In each case the shadows will assume complementary colours.

The effects of simultaneous contrast can also be studied with the aid of a contrivance of Ragona Scina. Two sheets of white cardboard are attached to a couple of boards fastened together at a right angle, as indicated in Fig. 124. Between the boards a plate of rather deeply coloured glass, G, is to be held in the manner shown in the figure, so that it makes, with the vertical and horizontal cardboards, an angle of about 45° . If the eye is placed at E, two masses of light will be sent to it. From the vertical cardboard white light will start, and, after being reflected on the glass plate G, will reach the eye. This light will be white, or almost entirely white, even after suffering reflection, owing to the circumstance that, with a deeply coloured plate of glass, the reflection takes place almost entirely from the upper surface, or from that turned toward the light. The second mass of light will proceed from the horizontal plate H: originally of course it was white light, but on its way

to the eye it traverses the glass plate, and becomes coloured by absorption. If the glass plate is red, this light when it reaches the eye will of course have the same colour ; consequently the first result is that we have presented to the eye

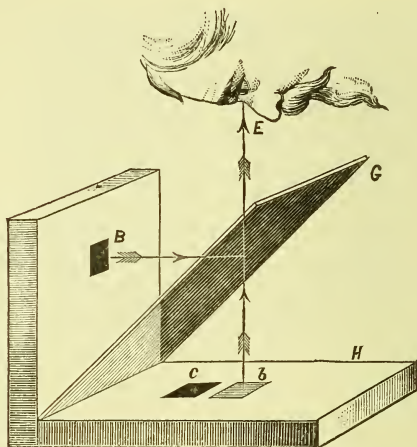


FIG. 124.—Apparatus of Ragona Scina for Contrast.

a mixture of red with white light, which will give the observer the idea that he is looking at an horizontal, square field of a somewhat pale reddish tint. If now a small black square be attached to the vertical cardboard at B, of course no white light can come to the eye from this portion of the cardboard, and the image of this spot will seem to the eye to be at *b*, on the horizontal board under the eye. Under ordinary circumstances this image would appear black ; in point of fact, however, in this case it appears deep red, owing to the red light transmitted by the plate of glass. Thus far the arrangement amounts to a device for presenting to the eye a mixture of red with white light, the white light being absent at a certain spot, which consequently appears of a deeper red. A similar black square is now to be placed on the horizontal board at *c* ; it will of

course prevent the light from the place it covers from reaching either the red glass or the eye, and under ordinary circumstances would be perceived simply as a square black spot. Owing, however, to the fact that the upper surface of the glass plate is reflecting white light to the eye, it really appears as a grey spot. The final result is, that we present to the eye at E a picture like that indicated by Fig. 125; that is, on a pale-red ground we have a spot which is pure grey, and near it one which is deep red.

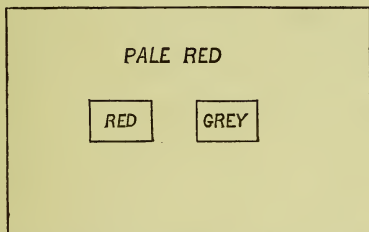


FIG. 125.—Colours that are really presented to the eye in the experiment of Ragona Scina.

Owing to contrast, however, the appearance is different: instead of a grey spot, we see one strongly coloured green-blue (Fig. 126). This effect is partly due to contrast with

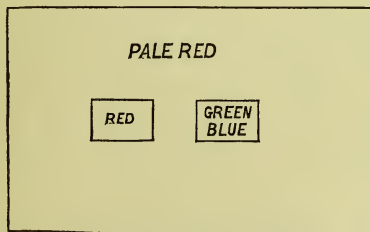


FIG. 126.—Colours that are apparently presented to the eye.

the pale red of the ground, but still more to the presence of the deep-red spot. This latter we can remove by taking away the black square B, which diminishes the effect con-

siderably. But now comes the most curious part of this experiment: If we select a square of grey paper which has the same color with the grey square seen in the apparatus arranged as in Fig. 124 (apart from effects of contrast), and place it over the glass plate and near the other two images, it will not be affected in colour, or only to a slight extent. In point of fact, we now have, side by side, on the same field, two grey squares quite identical in actual colour, but one appears by contrast blue-green, while the other is not affected, but is perceived by the eye as being simply a square of grey paper. As soon, however, as the observer recognizes the fact that these two squares really have the same grey colour, the illusion instantly vanishes, and both of them remain persistently grey. It is evident that in this case, as with the coloured shadows, the judgment is at fault rather than the retinal nerves; for, as soon as an opportunity offers, it corrects itself and takes a new departure. The illusion in this case, as well as with the coloured shadows, is produced quite independently of the knowledge of the observer, who may indeed be a trained physicist, minutely acquainted with the exact facts of the case, and with all the details employed in producing the deception, and still find himself quite unable to escape from its enthrallment.

The simple experiments of H. Mayer are less troublesome than those just described, and at the same time highly instructive. A small strip of grey paper is placed on a sheet of green paper, as indicated in Fig. 127; it will be found that the tint of the grey paper scarcely changes, unless the experimenter sits and stares at the combination for some time. A sheet of thin semi-transparent white paper is now to be placed over the whole, when it will instantly be perceived that the colour of the small slip has been converted by contrast into a pale red. Persons seeing this illusion for the first time are always much astonished. Here we have an experiment showing that the contrast

produced by strong, saturated tints is much feebler than with tints which are pale or mixed with much white light ; for, by placing tissue paper over the green sheet, the colour of the latter is extraordinarily weakened and mixed with a

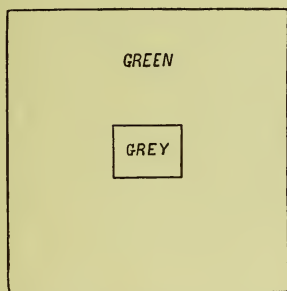


FIG. 127.—Green and Grey Papers, for Experiment on Contrast ; one-fourth size.

large quantity of white light. In this experiment it often happens that the red, which is due to contrast alone, seems actually stronger than the green ground itself. If, instead of using a slip of grey paper, we employ one of black, the contrast is less marked, and still less with one of white. It is scarcely necessary to add that, if red paper is employed, the small grey slip becomes tinted by contrast with the complementary colour, i. e., greenish-blue ; the same is true with the other colours.

By preparing with Indian ink a series of slips of grey paper, ranging from pure white to black, an interesting series of observations can be made on the conditions most favourable for the production of strong contrast-colours. The strongest contrast will be produced in the case of red, orange, and yellow, when the grey slip is a little darker than the colour on which it is placed, the reverse being true of green, blue, violet, and purple ; in every case the contrast is weaker if the grey slip is much lighter or much darker than the ground. We must expect then, in painting, to find that neutral grey will be more altered by pale

tints of red, orange, or yellow, which are slightly lighter than itself, and that the grey will be less altered by these colours when differing considerably from it in luminosity. An analogous conclusion with regard to green, blue, violet, and purple can also be drawn; these colours should be darker than the grey slip. Saturated or intense colours in a painting have less effect on white or grey than colours that are pale. This was shown in the preliminary experiment, where grey was placed on a ground of strong colour. In repeating these experiments, it will be noticed that the effect of contrast is stronger with green, blue, and violet than with red, orange, or yellow; that is to say, it is stronger with the cold than with the warm colours. If now we reverse our mode of proceeding, and place a small coloured slip on a grey ground, and cover the whole with tissue paper, it will be difficult even with a green slip to observe any effect of contrast. With a green slip, one sometimes imagines that the white sheet looks slightly pinkish or purplish for an instant, but the effect is quite uncertain. This is another illustration of the fact that, for the production of strong effects of contrast, it is necessary that the active colour should have a surface considerably larger than the one to be acted on; the former ought also, if possible, to surround the latter. There is, however, a limit beyond which this can not be carried. If the smaller field is reduced too much in size, it is liable to melt to a certain extent into the larger field of colour, in which case we obtain, not the effect due to contrast, but that produced by a mixture in the eye of the two colours; this is indeed one method employed by artists for the mixing of their colours.

Leaving now the contrast between pale colours and pure grey, we pause to consider for a moment the contrast of pale colours with each other. The laws governing this species of contrast have already been explained in detail in an earlier portion of the present chapter, and a construction

has been given by which the reader can study the differences produced in hue and saturation. To this it may now be added that, where pale tints are used in juxtaposition, the phenomena are those of simultaneous contrast, the retinal elements experiencing scarcely any fatigue ; hence the effects are due to deceptions of the judgment, and occur instantly. They are more marked than with intense or saturated colours, and the effects produced even much more surprising. These effects are heightened if the contrasted colours have about the same degree of luminosity, or differ in the same manner as in the spectrum ; that is, if the warm colours are selected so as to be rather more luminous than those that are cold. In Chapter .III. the reader will find a table showing the relative luminosity of the different colours of the spectrum, and, what is still more to our purpose, another giving the relative luminosity of the different components of white light.

We must next examine the effects that are produced by contrasting colours that differ in luminosity or in saturation. If the two colours are identical except in the matter of saturation, it will be found that the one which is more saturated will gain in intensity, while its pale rival will appear still paler. A slip of paper painted with a somewhat pale red, when placed on a vermillion ground, appears still paler, and may actually be made to look white. If a *still paler* slip be used, it may even become tinged greenish-blue, its colour being in this case actually reversed by the effect of contrast. With the aid of the two movable chromatic circles shown in Fig. 119, it is easy to trace these changes theoretically. As a pale colour, or one mixed with much white, already lies near the centre of the upper circle,* a small displacement carries it to the centre, that is, makes it appear white ; or it may even transport it beyond, and cause it to assume the complementary colour. When

* See Chapter XIV.

the colours differ in luminosity, analogous effects are observed. A dull-red slip was placed on a vermilion ground ; the effect was as though a quantity of grey had been added to the slip ; it looked more dingy and somewhat blackish. Another slip still darker and containing less red, when placed on the same ground, looked as if it were tinged with olive-green ; a still darker slip, with still less red colour, treated in the same way, looked black with a tinge of blue ; when, however, this last slip was placed on a white ground, or compared with true black, it was seen that its colour was far from black. The general result of contrasting colours which differ much in strength, then, is that the feebler one appears either more whitish or greyish, or assumes the complementary tint ; the stronger one, on the other hand, appears still more intense. If the strong and weak colours are complementary to each other, then each of them gains in intensity and appears purer, this gain seeming to be greater in the case of the pale tint. From this it follows that, while the juxtaposition of strong with feeble colours usually injures or greatly alters the latter, colours that are complementary furnish an exception, the reason of which is evident at the first glance.

When the pale or dark colours are not complementary to their more intense or brilliant rivals, they undergo the same changes indicated in the table on page 245, the changes in the case of the dull or pale colours being considerably greater. In proportion as the colours are distant from each other in the chromatic circle do they gain in saturation and beauty ; while as they approach their character is altered, and they are apt to look very pale, or, in the case of the dark colours, blackish or dirty. This is particularly so when the brilliant colour is large in surface and surrounds the darker one ; with reversed conditions the effect is not so much felt. Thus, a somewhat dull red near vermilion no longer looks red, but brown ; a dull orange tint on the same ground looks like a yellowish-brown.

It might be supposed from what has preceded that colours would enrich each other only when separated by a large interval in the chromatic circle ; and from a purely physiological point of view this is indeed true. Still, there are other influences of a more spiritual character at work, which modify and sometimes even reverse this lower law. Thus, the presence of paler colour in a painting near that which is richer often passes unperceived, simply making the impression of a higher degree of illumination. We recognize the representation of a flood of light, and delight in it, without finding fault with the pale tints, if only they are laid with decision and knowledge. Again, pale colour we delight in as representing the distance of a landscape ; the pale greenish-greys, bluish-greys, and faint tints of purple which make it up, we never think of putting into envious competition with the rich intense colours of the foreground, but enjoy each separately, and rejoice in the effect of atmosphere and distance, which neither kind of colour alone by itself could adequately render. That is to say, for the sake of light and atmosphere or distance, we gladly sacrifice a large portion of the powerful tints at our disposal, and consider ourselves gainers. The same is also true in another direction : we are ready to make the same sacrifice for the sake of avoiding monotony and gaining variety, provided only we can justify the act by a good reason. Cases of this kind often occur in large masses of foliage, which, if of the same general colour, are apt in a painting to look monotonous and dull, unless great labour is bestowed in rendering the light and shade and the small differences of tint which actually exist in nature. Under such circumstances the observer feels a certain relief at the presence of a few groups of foliage which are decidedly paler in colour than the surrounding masses, provided only there is a good excuse for their introduction. Willow-trees agitated by wind, and showing the under sides of their leaves, which are of a pale-greenish hue, offer a familiar example.

Again, the mere contrast of dark or dull tints enhances the colour and luminosity of those that are bright, and the observer receives the impression that he is gazing at a mass of gay and beautiful colouring, scarcely noticing the presence of the much larger quantity of tints that are darkened by being in deep shade. These darkened shade-tints are usually not variations of the same hue as the brighter tints, but are more bluish ; so that, technically, the combinations would often present instances of harmful contrast, were it not for the fact that the bright and dull tints do not belong even to the same chromatic circle, but to circles situated in different planes, as explained in the previous chapter. Putting this into more ordinary language, we should say simply that the strong contrast of light and shade masked such effects of harmful colour-contrast as were present. There is, however, another case where we are not so indifferent or lenient. Where two objects are placed near each other in a painting, and there is good reason why both should display the same colour with equal intensity, if one is painted with rich colour, the other with a pale or dark shade of the same colour, then the latter will look either washed out or dirty, and a bad effect will be produced. As a familiar illustration of this kind of effect, we may allude to the use in dress of two widely differing shades of ribbon, which have still the same general colour.

There is a still more general reason upon which the pleasure that we experience from contrast depends. After gazing at large surfaces filled with many varieties of warm colour, skillfully blended, we feel a peculiar delight in meeting a few mildly contrasting tints ; they prevent us from being cloyed with all the wealth of rich colouring so lavishly displayed, and their faint contradiction makes us doubly enjoy the richer portions of the painting. So also when the picture is mainly made up of cool, bluish tints : it is then extraordinarily strengthened and brightened by a few touches of warm colour. Precisely the same idea

holds good in drawings destitute of colour, and made up merely of lines : if the drawing is composed mainly of soft flowing curves, a few slanting straight lines across them seem delicious ; or, to take a parallel case from another department of art, in a discourse which is mainly grave in tone the introduction of a few slight touches of humour brightens and warms the audience most pleasantly. If there is about an equal quantity of gay and sombre tints, the effect is less good, becoming particularly bad when the composition is divided up into many alternate groups of gay and pale or sombre colours, impartially distributed.

Before concluding this chapter, it is necessary to add a few words with regard to the simple contrast of light and shade, that is, where all the elements are comprised by white, black, and intermediate shades of grey. As might be expected from what has preceded, when a light grey is



FIG. 128.—Black and White Disk for Experiment on Contrast.



FIG. 129.—Showing the result when disk, Fig. 128, is set into rapid rotation.

placed near a darker grey, the light shade appears still lighter, the dark shade still darker. This can be beautifully shown with the aid of our very convenient revolving disks. We take a black and white disk painted as represented in Fig. 128. When this disk is set in rotation, it will, on account of the mixture of the black and white, produce a series of grey rings, growing darker as we proceed from

the circumference toward the centre. Each ring, from the circumstances of the case, will as a matter of fact have an absolutely uniform shade of grey, but nevertheless it will not appear so to the observer. The rings will appear to him not uniform, but shaded, the lightest shade being always turned inward toward the centre, as roughly represented in Fig. 129. Where a ring comes in contact with one that is lighter than itself, it is made to look darker; with one darker than itself, to look lighter. The same effect can be observed by painting a series of pieces of paper with different flat tints of grey, and then arranging them to correspond with the disk experiment; they will present an appearance like that indicated by Fig. 130. It is hardly

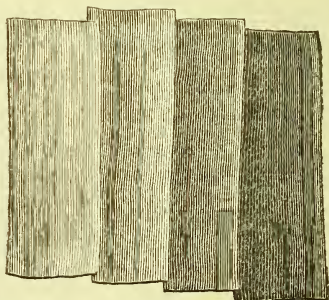


FIG. 130.—Slips of grey paper made to appear shaded by contrast.

necessary to add that in light-and-shade drawings, as well as in nature, appearances of this kind, more or less modified, are of constant occurrence. One of the most common cases is where range after range of mountains rise behind one another, the lower portions of the distant ranges appearing lighter than the upper outlines. During rain, ranges of hills often exhibit this phenomenon with astonishing distinctness. Even when the light and dark tints are at quite a distance from each other, the phenomena of contrast present themselves if there is much difference in the depth of

the two sets of shades. It is a very common experience that the sky of a landscape in a drawing turns out too pale after the rest of the drawing is completed. Contrasted with the white paper of the unfinished sketch, it may look quite right ; but, after the deeper tones of the distance and foreground are added, may become quite insignificant. Again, a few decidedly black touches in a drawing will often by contrast lighten up portions that had previously seemed considerably too dark ; or a few touches of pure white will apparently darken spaces that had seemed pale and weak. In each case the observer is furnished by external means with a standard for measuring the depth of the shade, and induced to use it rather than his memory. By the skillful employment of contrast, drawings in light and shade can be made to appear luminous and brilliant, or rich and deep ; neglect of this element produces tameness and feebleness. The contrast of light with dark shades is not inferior in power to that of warm with cool tints ; and, in point of fact, the contrast of white with black is the strongest case of contrast possible. We have on the one hand the presence of all the colours, on the other their total absence. Hence, as has been noticed before, the contrast that takes place between light and shade will sometimes mask or even reverse that which occurs with different colours. We can perhaps better tolerate a shortcoming in the matter of colour-contrast than in that of light and shade ; if the latter is right and powerful, we forgive a limited amount of inferiority in the former, merely remarking that the work is rather slight or pale in colour, but not on that account pronouncing a verdict of total condemnation. On the other hand, if the colour as such is right, but the depth of the different tints mostly defective, then the whole is spoiled, and we contemplate the tints, lovely enough in isolation, with no satisfaction. We forgive, then, a partial denial of the truths of colour more easily than those of light and shade, which probably is a result of the nature of the opti-

cal education of the race. For the human race, thus far, light and shade has been the all-important element in the recognition of external objects ; colour has played only a subordinate part, and has been rather a source of pleasure than of positive utility.

All that has been said with regard to the contrasts of white, black, and grey, with slight modification, applies to any single colour taken by itself ; for instance, to drawings executed in one colour only, such as blue or brown. From this it results that every colour is capable of exhibiting two kinds of contrast, viz., that involved by competition with other colours and that of mere light and shade.

The contrast of white, black, and grey with the series of positive colours remains to be noticed. Taking up these in order, we find that red when placed on a white ground appears darker and rather more intense in hue ; on a black ground it becomes tinted somewhat orange-red, and looks of course more luminous. Both these effects are probably due ultimately to mere contrast of light and shade ; the white ground makes the red by contrast look darker. But we are accustomed to see red when it is darkened recede from orange and approach pure red, or even perhaps to become somewhat purplish ; hence it appears so in this case ; it is an instance of expectant attention. When red is placed on a black ground, it is made by contrast to look more luminous ; but we are accustomed to see luminous red become tinted with an orange hue ; hence the result. Red on grey grounds of various depths undergoes modifications corresponding to those just mentioned. Pale red, i. e., red mixed with much white, on a white ground, gains in intensity of colour ; on a black or dark-grey ground it loses intensity, and approximates to pure white in appearance. Here the contrast of light and shade is so strong as to cause the colour to pass almost unperceived ; or we may say pale red really does approach much nearer to pure white than black, and hence is at last accepted for it. Dark, dull red

on a white ground may be mistaken for brown ; on a black ground it appears more luminous and more red. Orange on a white ground looks darker and more reddish, on a black ground more luminous and yellow. The other effects correspond with those described in the case of red. Yellow on a white ground appears darker and more greenish than on a black ground ; in the latter case it is particularly brilliant, and the black also looks well, taking on a bluish tint. Dark yellow on a white ground looks brown or greenish-brown ; on a black ground its colour is displayed to more advantage. Pale yellow on a white ground is apt to look greenish, on a black ground to appear whitish. Yellow and grey or black constitute a pleasant combination, of which extensive use has been made in nature and art. Green on a white ground looks deeper and richer, on a black ground somewhat paler ; by contrast the black is made to look somewhat reddish or rusty. Green causes grey to appear reddish ; the effect is particularly marked when the grey has about the same luminosity with the green, also when both are in the shade. Cyan-blue on white appears darker and perhaps more greenish than on black. Blue on white appears dark and rich, but shows no tendency to green ; on black, by contrast, it becomes more luminous. The same is true with blue on grey ; the latter acquires a somewhat yellowish or rusty hue. The action with violet is similar to that of blue.

From the foregoing it is evident that the contrast of black, white, and grey with the colours depends mainly on an apparent increase or diminution of their luminosity, whereby in most cases their apparent hue is affected owing to association. In the case of the colder colours, the tint of the grey or black ground is affected, and shows a tendency toward a hue complementary to the colour employed. We associate grey with blueness, and where the effect is such as contradicts this habitual association it is disagreeable ; on the other hand, grey with yellow forms

an agreeable contrast, as the yellow tends to make the grey look more bluish, and thus corrects any yellowish or rusty appearance connected with it. It is claimed in some works on colour that the complementary tints furnished by the pure grey react on and strengthen the colours which call them forth. An eye which is tired by gazing at green is indeed rested by looking at its complement, i. e., at a mixture of red and violet, and afterward will see the green with more vividness ; but it is difficult to understand how the presentation of red, violet, and green, or, what is the same thing, grey light, can materially refresh the eye, or restore its temporarily exhausted power. In the case of pale tints, an effect of this character does indeed seem to take place, but we must attribute it rather to an act of judgment than to a physiological cause.

CHAPTER XVI.

ON THE SMALL INTERVAL AND ON GRADATION.

IN the preceding chapter we have seen that, when two colours which are nearly identical are contrasted, each is made to appear less intense or saturated : red with orange-red, yellow with orange-yellow, cyan-blue with blue, are examples of such combinations. From this it might be supposed that, in chromatic compositions, it would not be allowable to place colours thus nearly related in close juxtaposition. It is, however, found in practice that colours which are distant from each other in the chromatic circle by a *small interval* can be associated without detriment under certain conditions. If the two colours express a variation in the luminosity of one and the same coloured surface, they do not come into hurtful competition, and we receive the impression of a single coloured surface, more highly illuminated in certain portions. The scarlet coat of a soldier when shaded appears red ; the sunlit portion is orange-red. Grass in the sunshine acquires a yellowish-green hue ; in the shade its colour is more bluish. But neither of these cases produces on us a disagreeable effect, for we regard them as the natural consequences of the kind of illumination to which these objects are exposed. The effect is not disagreeable even in mere ornamental painting, if it is seen that the two tints are intended to express different degrees of luminosity of the same constituent of the design, even though this be only arabesque tracery. From this explanation it follows that the two contiguous tints should

have their luminosities arranged so as to correspond to nature ; otherwise a contradictory effect would be produced. The following table gives a series of small intervals, arranged properly as to luminosity; and it will be seen to correspond to the relative luminosities of the colours of the spectrum, or of the colours which taken together make up white light (see Chapter III.) :

TABLE OF SMALL INTERVALS.

Darker.	Lighter.
Red	Orange-red.
Orange-red	Orange.
Orange	Orange-yellow.
Orange-yellow	Yellow.
Yellowish-green	Greenish-yellow.
Green	Yellowish-green.
Cyan-blue	Green.
Blue	Cyan-blue.
Ultramarine-blue	Blue.
Violet	Purple.
Purple	Red.

It will be noticed that the colours under the heading “ Darker ” are really the shade-tints of the series opposite them, and the difference may often be greater than that indicated in the table. One of the commonest of these intervals is that of yellow deepening into orange-yellow. In sunsets yellow scarcely occurs without undergoing a change of this kind ; it is almost the rule with yellow flowers ; and even the pale, broken, subdued yellowish-browns of many natural objects manifest the same tendency. The relations of greenish-yellow, etc., to green are shown beautifully by foliage under sunlight, while the interval of cyan-blue to blue or to ultramarine-blue is displayed on the grandest scale by the sky. In brilliant sunsets the first and last pair of intervals are of constant occurrence ; in fact, we can scarcely think of a sunset without calling up in imagination

red and purple. The interval greenish-yellow and yellow is not included in the list ; it is perhaps less easy to tolerate than any of the others ; we like to see yellow luminous or rich, that is, passing into orange ; but, when it begins to become decidedly greenish, we hesitate, unless there is some good reason for accepting it. When the small interval is used, and the two tints are put more or less into competition by belonging to different surfaces, the effect is less good, unless it is accounted for by the nature of the illumination, or in some other equally satisfactory way.

Much of the above applies to the case where the colours pass into each other by gentle and insensible gradations, so that the observer is quite at a loss to say where one ends and the other begins. Here, as before, colours which are nearly related, or separated only by a small interval, blend harmoniously into each other and produce a good effect. The reason of this is again found mainly in our preconceived ideas of the changes which coloured surfaces undergo when more or less strongly illuminated. If the colours are quite distant from each other in the chromatic circle, a rapid transition from one to the other, by blending, produces always a strange and often a disagreeable effect. A yellow surface distinctly opposed or contrasted to a blue surface often gives a good effect ; but, if it passes by a series of quick gradations into blue, the effect is bad ; it is as though it tried to assert at the same time that it was warm and luminous as well as cold and dark. In the case of the sky, it is true that we have, toward sunset, the yellow portions blending below into orange and red, and above, by a long and slow series of gradations, into blue ; but the distance between the blue and yellow is large, and they are separated by a series of neutral tints, and we think of the whole as an effect produced by apparent nearness or distance from the sun. Even in a case like this, many artists prefer not to include in their paintings too much of the upper blue, and thus are able to give more decided expres-

sion to the warmth and brightness of the sky. When we see in nature a field of grass gradually growing decidedly red, we think of clover as the excuse, without, nevertheless, being particularly edified by its presence. In some mountain lakes, such as the Königssee, we find the blue-green water actually passing in some places by rather quick gradations into a purplish-red. The rapid transition into this almost complementary hue produces an effect which seems strange and almost incredible to those who for the first time behold it. When the cause is recognized, we learn to look upon the purple patches as marking the shallower water, and, having accepted the effect as reasonable, we soon find ourselves enchanted by it, and always remember it for its strange beauty.

When two colours differing considerably, not only in hue but in saturation, or simply in the latter respect, blend rapidly into each other on the same surface, we always require a reason for the change of tint ; and, if none is furnished, the effect is apt to appear absurd, and resemble somewhat the case of a man who at one moment is calm and cool, and the next, without obvious reason, tender and pathetic. When we find the cool grey or greyish-brown tones on the surface of a cliff suddenly becoming rose-tinted, we require an explanation of the change, and are quite satisfied if told that the top of the cliff is still illuminated by the sinking sun ; if, however, it is midday, we are forced to think of red veins of some foreign substance disseminated through the sober rock, and wonder what it can possibly be, and wish it were away. All this forms one of the minor reasons why painters like to keep their tints together in large masses, the bright warm colours in one place, the cool pale tints in another.

One of the most important characteristics of colour in nature is the endless, almost infinite gradations which always accompany it. It is impossible to escape from the delicate changes which the colour of all natural objects un-

dergoes, owing to the way the light strikes them, without taking all the precautions necessary for an experiment in a physical laboratory. Even if the surface employed be white and flat, still some portions of it are sure to be more highly illuminated than others, and hence to appear a little more yellowish or less greyish ; and, besides this source of change, it is receiving coloured light from all coloured objects near it, and reflecting it variously from its different portions. If a painter represents a sheet of paper in a picture by a uniform white or grey patch, it will seem quite wrong, and can not be made to look right till it is covered by delicate gradations of light and shade and colour. We are in the habit of thinking of a sheet of paper as being quite uniform in tint, and yet instantly reject as insufficient such a representation of it. In this matter our unconscious education is enormously in advance of our conscious ; our memory of sensations is immense, our recollections of the causes that produce them utterly insignificant ; and we do not remember the causes mainly because we never knew them. It is one of the tasks of the artist to ascertain the causes that give rise to the highly complex sensations which he experiences, even in so simple a case as that just considered. From this it follows that his knowledge of the elements that go to make up chromatic sensations is very vast compared with that of ordinary persons ; on the other hand, his recollection of mere chromatic sensations may or may not be more extensive than theirs. Hence it follows that it requires long training to acquire the power of consciously tracing fainter gradations of colour, though much of the pleasure experienced by their passive reception can be enjoyed without previous labour.

These ever-present gentle changes of colour in all natural objects give to the mind a sense of the richness and vastness of the resources of Nature ; there is always something more to see, some new evanescent series of delicate tints to trace ; and, even where there is no conscious study-

of colour, it still produces its effect on the mind of the beholder, giving him a sense of the fullness of Nature, and a dim perception of the infinite series of gentle changes by which she constantly varies the aspects of the commonest objects. This orderly succession of tints, gently blending into one another, is one of the greatest sources of beauty that we are acquainted with, and the best artists constantly strive to introduce more and more of this element into their works, relying for their triumphs far more on gradation than on contrast. The greatest effects in oratory are also produced by corresponding means ; it is the modulation of the tone and thought, far more than sharp contrasts, that is effective in deeply moving audiences. We are very sensitive to the matter of modulation even in ordinary speech, and instantly form a general judgment with regard to the degree of cultivation and refinement of a stranger from the mode in which a few words are pronounced. All this has its parallel in the use of colour, not only in painting, but also in decoration. Ruskin, speaking of gradation of colour, says : “ You will find in practice that brilliancy of hue and vigor of light, and even the aspect of transparency in shade, are essentially dependent on this character alone ; hardness, coldness, and opacity resulting far more from *equality* of colour than from nature of colour.” In another place the same author, in giving advice to a beginner, says : “ And it does not matter how small the touch of colour may be, though not larger than the smallest pin’s head, if one part of it is not darker than the rest, it is a bad touch ; for it is not merely because the natural fact is so that your colour should be gradated ; the preciousness and pleasantness of colour depends more on this than on any other of its qualities, for gradation is to colours just what curvature is to lines, both being felt to be beautiful by the pure instinct of every human mind, and both, considered as types, expressing the law of gradual change and progress in the human soul itself. What the difference is in mere beauty

between a gradated and ungradated colour may be seen easily by laying an even tint of rose-colour on paper and putting a rose-leaf beside it. The victorious beauty of the rose as compared with other flowers depends wholly on the delicacy and quantity of its colour-gradations, all other flowers being either less rich in gradation, not having so many folds of leaf, or less tender, being patched and veined instead of flushed."*

All the great colourists have been deeply permeated by a sentiment of this kind, and their works, when viewed from the intended distance, are tremulous with changing tints—with tints that literally seem to change under the eye, so that it is often impossible for the copyist to say exactly what they are, his mixtures never seeming to be quite right, alter them as he will. Among modern landscape paintings, those of Turner are famous for their endless quantity of gradation, and the same is true even of his water-colour drawings. The perfect blending of colours, for example, in the sky, or in our best representations of it, produces an effect of wonderful softness and beauty, the tints melting into each other with a liquid smoothness for which we can find no other parallel. The absolutely perfect gradation and softness of the sky well expresses its qualities as a gas, impalpable, evanescent, boundless.

There is, however, another lower degree of gradation which has a peculiar charm of its own, and is very precious in art and nature. The effect referred to takes place when different colours are placed side by side in lines or dots, and then viewed at such a distance that the blending is more or less accomplished by the eye of the beholder. Under these circumstances the tints mix on the retina, and produce new colours, which are identical with those that

* "Elements of Drawing," by J. Ruskin. The distinguished artist Samuel Colman once remarked to the writer, that this book not only contained more that was useful to the student of art than any previous work, but that it contained more than all of them put together.

are obtained by the method of revolving disks. (See Chapter X.) If the coloured lines or dots are quite distant from the eye, the mixture is of course perfect, and presents nothing remarkable in its appearance; but before this distance is reached there is a stage in which the colours are blended, though somewhat imperfectly, so that the surface seems to flicker or glimmer—an effect that no doubt arises from a faint perception from time to time of its constituents. This communicates a soft and peculiar brilliancy to the surface, and gives it a certain appearance of transparency; we seem to see into it and below it. Dove's theory of lustre has perhaps some bearing on this well-known phenomenon. According to Dove, when two masses of light simultaneously act on the eyes, lustre is perceived, provided we are in any way made conscious that there are actually *two* masses of light. On a polished varnished table we see the surface by means of its imperfections, scratches, dust, etc., and then besides have presented to us another mass of light which is regularly reflected from the surface; the table looks to us lustrous. The author, and afterward Dove in a different way, succeeded in producing this lustrous appearance when only a single eye was employed, that is, without the aid of binocular vision.* In the case before us, the images of the colour-dots are more or less superimposed on the retina, and consequently seen one through the other; and at the right distance there is some perception of a lack of uniformity, the degree of blending varying from time to time. According to Dove's theory, we have here the conditions necessary for the production of more or less soft brilliancy. With bright complementary colours the maximum degree of lustre is obtained; when the colours are near each other in the chromatic circle, or dull or pale, the effect is not marked, but exists to the extent of making the surface appear somewhat transparent. When the two colours are replaced simply by black and white,

* "American Journal of Science and Arts," May, 1861.

the same lustrous appearance is still produced. Sir David Brewster has described an experiment which has some bearing on these matters. If a wall-paper is selected with a pattern which repeats itself at intervals of a few inches, it is possible, after some practice, so to arrange the eyes as to cause the adjacent and corresponding portions to seem to coalesce and form a new picture, which will in most respects be identical with that obtained by ordinary vision. This new picture will not seem to be at the same distance from the eye as the real objects, and will move with each slight motion of the head ; but what concerns us more is, that it has a certain appearance of transparency and beauty not found in the original. In this experiment two slightly dissimilar masses of light are presented to the two eyes, and the result is an appearance of transparency, using this word in its artistic sense.

But to return : the result of this imperfect blending of colours or of black and white by the eye is to communicate to the surface an appearance of clearness, and to remove any idea of hardness or chalkiness ; it is so familiar to us that we accept it as quite natural, and only become conscious of its charm when it is withdrawn. As an example in nature, we have the somewhat distant sea under a bright-blue sky : the waves will be mainly green, the spaces between them blue ; these colours then blend into a sparkling greenish-blue, which can not be imitated with a simple mixed pigment. Also in grasses viewed at some distance, the yellowish-green, bluish-green, reddish, purplish, and brown tints, and the glancing lights, blend more or less together, and produce an effect which can not be reproduced by a single sweep of the brush. The more distant foliage of trees on hillsides shows something of this kind ; and it does not appear to be entirely absent even from the dust on a traveled road, the minute sparkling grains of sand still producing some action on the eye after they can no longer be distinguished individually.

In fresco-painting, and in scene-painting for the theatre, most extensive use is made of this principle : at the right distance adjacent tints blend, and what near at hand seemed a mass of purposeless daubs becomes an effective picture. This same method of mixing colours on the retina of the observer is also used more or less in oil painting with excellent effect ; it lends to them a magical charm, the tints seeming purer and more varying ; the very fact that the appearance of the painting changes somewhat according as the observer advances or retires from it being an advantage, communicating to it, as we might say, a certain kind of life. Oil paintings in which this principle is not employed labour under one quite demonstrable disadvantage : as the observer retires adjacent tints blend, whether it was the intention of the artist or not ; and if this has not been calculated for, a new and inferior effect is pretty sure to be produced. In water-colour drawings the same mode of working is constantly employed under the form of stippling, more or less formal ; and with its aid certain results of transparency and richness can be attained, which otherwise would be out of the reach of the artist. If the stippling is formal and quite evident, it is apt to give a mechanical look to a drawing, which is not particularly pleasant ; but properly used, it has great value, and readily lends itself to the expression of form. To descend several steps lower, we find the designers of wall-papers and carpets employing this mode of mixing colours and producing their gradations. In cashmere shawls the same principle is developed and pushed to a great extent, and much of their beauty is dependent on it. Finally, in etchings, engravings, and pen-and-ink drawings, we have other examples of its application ; their clearness, transparency, and sparkling effect being mainly due to the somewhat imperfect blending of the black and white lines. This effect can best be perceived by comparing them with lithographs, or, better still, with Indian ink or sepia drawings. The sky-like softness of the last two is very lovely, and, in

some respects, very true to nature ; but if in them the line manner is entirely avoided, they are a little apt to show a lack of transparency in the deeper masses of shade, and to look heavy or dull. This result is avoided by purposely introducing a certain amount of line-drawing, either with the pen or a small brush. We have in nature a great variety of appearances, and the various methods of art are calculated to represent one or the other of them more or less perfectly ; but there is no single kind of art manipulation which will deal equally well with all.

Finally, it is to be remarked that when colour is used simply for ornamental purposes, blending or gradation becomes of subordinate importance. This is the case, for example, where the design is worked out solely in flat tints. Work of this kind, where the fancy is not allowed to interfere much with the general correctness of the drawing or colour, forms one of the first steps by which painting gradually passes over into pure ornamental design. We have here colours arranged in harmonious masses, bounded by sharp outlines, often definitely traced in black, and are pleased with them, and with the beautiful, correct outlines. All gradation and blending of colours is abolished, and this fact alone announces to us, in an emphatic way, that the design makes no pretension to realistic representation ; we are pleased with the colours and outlines, and are rather surprised to find how much can be accomplished by them ; and if gold is introduced in the background or draperies, its presence only adds to the general effect. By insensible changes the figures of men and animals, etc., become more conventional or grotesque, as in heraldry, until finally there is no attempt made to portray any particular natural object. *Suggestions* are taken from objects in nature, which are used in much the same way as by musical composers. The intention, however, is the production of a beautiful design which shall serve to ornament something else, as a woven stuff, a vase, or the wall of a building. As gradation is

one of our most efficient modes of giving work in colour a thoroughly realistic appearance, it evidently can not be much employed in ornament, where it is an object to avoid any imputation of intentional realism.

In closing this chapter it may be well to allude to a singular effect often produced by insensible gradation on natural objects, or on their representations in paintings. We have seen that a coloured surface having a well-defined shape, when placed on a grey ground, is capable through contrast of causing the ground to appear of the complementary colour. For example, a grey square or a green ground will appear as though tinted with rose-colour. If, however, the green passes into the grey by insensible gradations, the matter may be so arranged that a small amount of green causes the whole surface to appear green, when most of it really is grey. This effect is often seen on rocks partially covered with green moss: a few small patches on the side exposed to the light will have a bright-green hue; some of the surface in the shade will be tinted dark green, this colour passing gently into brown or grey, with here and there a few quite small touches of olive-green. Three fourths of the surface of the shaded side of the rock will then be really grey or brown, but nevertheless the whole will appear to be dark green. Another very common example is furnished by the foliage of trees standing so that the sun appears to be over them. Under these circumstances their tops and sides catch the sunbeams and appear of a bright yellowish-green; the rest of the tree is in the shade, and appears at first sight of a darker green, and is always so painted by beginners. If, however, the colour is examined through an aperture about the size of a pea, cut in a piece of white cardboard, it will be found that the real colour is a somewhat greenish grey. On retiring farther from the tree, this colour of its shady side will often change to a pure grey, yet to a casual observer it will still appear green. Quite wonderful effects have been obtained by

some artists from the recognition of the principle here involved ; their calm resignation of every trace of local colouring, and acceptance in its place of some kind of grey, imparting to their pictures a high degree of aërial perspective and of apparent luminosity.

CHAPTER XVII.

ON THE COMBINATION OF COLOURS IN PAIRS AND TRIADS.

IN the previous portions of this work we have dealt with facts that are capable of more or less rigorous demonstration ; but we now encounter a great series of problems that can not be solved by the methods of the laboratory, or by the aid of a strictly logical process. Why a certain combination of colours pleases us, or why we are left cold or even somewhat shocked by another arrangement, are questions for which we can not always frame answers that are satisfactory even to ourselves. There is no doubt that helpful and harmful contrast have a very great influence on our decision, as will hereafter be pointed out ; but besides this, we are sometimes influenced by obscure and even unknown considerations. Among these may perhaps be found inherited tendencies to like or dislike certain combinations or even colours ; influence of the general colour-atmosphere by which we are surrounded ; training ; and also a more or less delicate nervous susceptibility.

The author gives below, in the form of tables, some of the results furnished by experience, and takes pleasure in acknowledging his indebtedness to Brücke and to Chevreul for much of the information contained in them.

Spectral red * with blue gives its best combination.

Spectral red with green gives a strong but rather hard combination.

* A red between carmine and vermilion.

Spectral red with yellow gives an inferior combination.

Spectral red with red lead gives a bad combination.

Spectral red with violet gives a bad combination.

If gold be substituted for the yellow pigment, the combination becomes excellent. Red and yellow also make a better combination when the red inclines to purple and the yellow to greenish-yellow. The combination red and yellow is also improved by darkening the yellow or both colours; this causes the yellow to appear like a soft olive-green (R.). The combination red and green is also improved by darkening both colours, or the green alone (R.).

Vermilion with blue gives an excellent combination.

Vermilion with cyan-blue gives an excellent combination.

Vermilion with green gives an inferior combination.

Vermilion with yellow gives an inferior combination.

Vermilion with violet gives a bad combination.

Vermilion and gold furnish an excellent combination. The combination vermilion and yellow is improved somewhat by darkening the yellow; if it is considerably darkened, it tells as a soft olive-green (R.). Vermilion and green are better when the green or both colours are much darkened (R.).

Red lead with blue gives an excellent combination.

Red lead with cyan-blue gives an excellent combination.

Red lead with blue-green gives a strong but disagreeable combination.

Red lead with yellowish-green gives a tolerably good combination.

Red lead with yellow gives quite a good combination.

Red lead with orange gives quite a good combination.

The combination red lead and bluish-green is improved by darkening the green or both the colours (R.). Red lead gives a better combination with a yellow having a corresponding intensity or saturation; if the yellow is too bright, the effect is inferior (R.). The combination red lead and yellow is much better than red and orange. The last two

combinations given in the table are of course cases where the small interval is employed. (See Chapter XVI.)

Orange with cyan-blue gives a good and strong combination.
 Orange with ultramarine gives a good and strong combination.
 Orange with green gives a good combination.
 Orange with violet gives a moderately good combination.

Orange-yellow with ultramarine gives its best combination.
 Orange-yellow with cyan-blue gives not quite so good a combination.
 Orange-yellow with violet gives a good combination.
 Orange-yellow with purple gives a good combination.
 Orange-yellow with purple-red gives an inferior combination.
 Orange-yellow with spectral red gives an inferior combination.
 Orange-yellow with sea-green gives a bad combination.

Yellow with violet gives its best combinations.
 Yellow with purple-red gives good combinations.
 Yellow with purple gives good combinations.
 Yellow with spectral red gives inferior combinations.
 Yellow with blue, inferior to orange-yellow and blue.
 Yellow with blue-green gives one of the worst possible combinations.
 Yellow with green gives bad combinations.

The combination yellow and spectral red is improved by darkening the yellow (R.). Blue-green and yellow, both much darkened, give a better combination (R.). According to Chevreul, yellow gives with green a good and lively combination; to this the author can not agree, although it is true that the effect is improved by darkening the yellow considerably. Chrome-yellow and emerald-green give combinations that are not bad when both the colours are very much darkened (R.).

Greenish-yellow with violet gives its best combinations.
 Greenish-yellow with purple gives good combinations.
 Greenish-yellow with purplish-red gives good combinations.
 Greenish-yellow with vermilion gives strong but hard combinations.
 Greenish-yellow with spectral red gives strong but hard combinations.
 Greenish-yellow with red lead gives tolerably good combinations.

Greenish-yellow with orange-yellow gives bad combinations.

Greenish-yellow with cyan-blue gives bad combinations.

Greenish-yellow with ultramarine gives a somewhat better combination.

The combination greenish-yellow and orange-yellow is improved by darkening the latter colour, which then appears brownish (R.). Greenish-yellow and cyan-blue make a better combination when the blue is darkened (R.).

Grass-green with violet gives good but difficult combinations.

Grass-green with purple-violet gives good but difficult combinations.

Grass-green with rose gives combinations of doubtful value.

Grass-green with carmine gives combinations of doubtful value.

Grass-green with pink gives combinations of doubtful value.

Grass-green with blue gives combinations of doubtful value.

The value of the last four combinations is a disputed matter. The combination green and carmine is improved by darkening both colours considerably (R.). The combination green and blue becomes better as the green inclines to yellow and the blue to violet (R.). The combination green and violet, according to Chevreul, is better when the paler hues of these colours are employed.

Emerald-green with violet gives strong but hard combinations.

Emerald-green with purple gives strong but hard combinations.

Emerald-green with red gives strong but hard combinations.

Emerald-green with orange gives strong but hard combinations.

Emerald-green with yellow gives bad combinations.

All these combinations are very difficult to handle. Emerald-green and yellow, when both are much darkened, furnish somewhat better combinations (R.).

Sea-green with vermilion gives good combinations.

Sea-green with red lead gives good combinations.

Sea-green with violet gives good combinations.

Sea-green with purple-violet gives tolerably good combinations.

Sea-green with purple-red gives, simply as pairs, poor combinations.

Sea-green with carmine gives, simply as pairs, poor combinations.

Sea-green with blue gives bad combinations.

Sea-green with yellow gives bad combinations.

The surface of the green should be much larger than that of the vermilion or red lead.

Cyan-blue with chrome-yellow gives moderate combinations.

Cyan-blue with Naples-yellow gives good combinations.

Cyan-blue with straw-yellow gives good combinations.

Cyan-blue with carmine (light tones) gives good combinations.

Cyan-blue with violet gives poor combinations.

Cyan-blue with purple-violet gives poor combinations.

Cyan-blue with ultramarine gives good combinations (small interval).

The combinations of cyan-blue with violet and purple-violet are not good, except in fine materials and light tones.

Ultramarine with carmine gives poorer combinations than cyan-blue.

Ultramarine with purple-red gives poorer combinations than cyan-blue.

Ultramarine with violet gives, simply as pairs, poor combinations.

Violet with purple gives poor combinations if extended beyond the small interval.

Violet with carmine gives poor combinations.

In studying the effects produced by colours in combination, it is of course important to exclude as far as possible all extraneous causes that might influence or confuse the judgment. Hence the colours under examination should be disposed in very simple patterns, as the employment of beautiful form or good composition might easily become a means of leading the student to accept, as good, combinations that owed their beauty to something besides mere colour. For the same reason, gradation and good light-and-shade effect should in such examinations be avoided; for these, as well as good composition, are means of concealing to some extent the poverty of a colour-combination. For a similar reason the materials employed in such experi-

ments should not be too fine. Almost any colour-combination worked out in stained glass appears pretty good, owing to the brilliancy of the coloured light. This is one reason why the patterns in a kaleidoscope have been of so little value in decorative art ; for, when the colours are most carefully imitated in coarser materials, they are apt not only to lose their brilliancy, but even sometimes to appear dull or dirty from the effects of harmful contrast, which did not make itself felt before. To a less degree this applies also to silk ; many colour-combinations worked out in this material are tolerable on account of its high reflecting power, while the same colours, if transferred to wool or cotton, appear poor enough.

In forming a judgment as to the value of combinations of colour, we should also be cautious in basing our conclusions even on observations made directly from nature itself ; for here our judgment is liable to be warped by the presence of beautiful form, good composition, exquisite gradation, and high luminosity. Green and blue, for example, make a poor combination, and yet it is one constantly occurring in nature, as in the case where the blue sky is seen through green foliage. This effect is often very good, but a careful examination will show that, in most cases, blue and green do not really come in contact ; for if the sunlight penetrates the leaves in contact with the sky, they no longer look green, but greenish-yellow, and this colour makes a tolerable combination, particularly with ultramarine-blue. Generally, however, the leaves actually in contact with the sky are in the shade, or at least do not send bright light to the eye, and we have really greenish-grey or brownish-green combined with the blue of the sky. When green actually does fairly touch the blue of the sky, as with a forest of young trees growing thickly, the green is usually far darker than the blue sky, as may be seen by closing the eyes partially. Here the combination is helped somewhat by light-and-shade contrast ; but when, owing to

any cause, the blue of the sky is darkened till it approximates in luminosity to the green of the foliage, then the colour-combination is felt by an artist to be bad. The forms of trees are so beautiful, the variety, the gradation they exhibit so endless, the associations called up by them so agreeable, that we are apt to deceive ourselves about this colour-combination ; but when an attempt is made to transfer it to canvas, we become painfully sensible of the fact that Nature sometimes delights in working out beautiful effects with colours that are of very doubtful value, cunningly hiding their poverty with devices that often are not easy to discover or to imitate.

There are several causes that may render a combination of two colours bad. Prominent among them we find the matter of contrast: the colours may look dull and poor on account of harmful contrast, or may on the other hand appear hard and harsh from an excess of helpful contrast. The author has placed in the form of a diagram the results of his observations on the effects of contrast in diminishing or increasing the saturation or brilliancy of colours. This diagram (Fig. 131) and its use are explained in Chapter XV., and at present we merely remind the reader that colours less than 80° or 90° apart suffer from harmful contrast, while those more distant help each other. In the case of colours that are about 80° apart, the matter remains a little doubtful ; the two colours may help each other somewhat, or the reverse may be true. On comparing this diagram with the results furnished by experience and given in the preceding tables, it will be found that in good combinations the two colours are always more than 90° apart, so that the effect of contrast is mutually helpful. Thus, red furnishes good combinations with blue and cyan-blue, which are considerably more than 90° distant from it ; while the combination with artificial ultramarine, which is nearer, is inferior, and that with violet bad. It does not follow, however, that the colours in the diagram which are

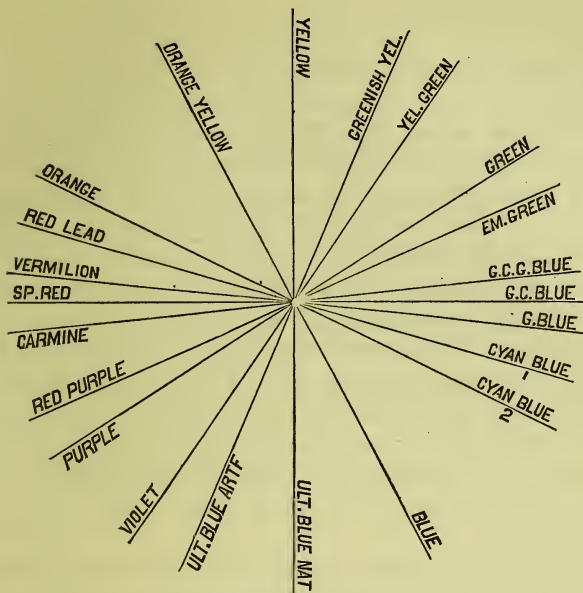


FIG. 131.—Contrast Diagram.

situated farthest apart always make the best combinations ; for, if this were the case, the best combinations would be simply the complementary pairs, which in the diagram are placed at the greatest distance from each other, viz., opposite. But some of the complementary colours are quite harsh from excessive contrast ; for example, red and its complement green-blue, also purple and its complement green. Of all the complementary pairs, according to Brücke, these are least employed in art, as the harshness with them is at a maximum. Now we can divide the colour-diagram, Fig. 131, into two halves by a line drawn from yellowish-green to violet, and the left-hand half will contain the warm colours, the right-hand the cold. After doing this, we find that red and green-blue, or purple and green, are not only complementary, but also situated at or

near the positions, if we may so express it, of the greatest warmth and coldness; hence, owing to a double reason, the contrast becomes excessive, and the combination harsh. According to the same authority, the complementary colours most in use are ultramarine and yellow, blue and orange-yellow, or cyan-blue and orange; then follow violet and greenish-yellow. In these cases, the complementary pairs are situated at some distance from the centres of warmth and coldness, being in fact either on or not far from the dividing line, which prevents excessive contrast and the consequent hardness complained of in the examples first cited. It may here be remarked that colours which are truly complementary often appear better than those which only approximate to this condition; vermilion and red lead, with their complements green-blue and greenish-blue, do not furnish such offensive combinations as are obtained when green is substituted for the true complementary hue.

The complementary colours are very valuable when the artist is obliged to work with dark, dull, or pale colours, and still is desirous of obtaining a strong or brilliant effect. The fact that the colours are dull or pale or greyish prevents much possibility of harshness; and the use of complementary hues excludes all risk of the brilliancy of the tints being damaged by harmful contrast. In general, the lower we go in the scale, and the more our colours approximate to black, brown, or grey, the more freely can we employ complementary hues without producing harshness; and even those objectionable pairs, red and green-blue, purple and green, if sufficiently darkened, become agreeable.

It has been stated above that in good combinations the colours are always a considerable distance apart in the chromatic circle. This, however, does not exclude the class of combinations mentioned in Chapter XVI., where it was shown that any two colours differing but slightly produce

a more or less pleasant effect ; this is the case of the *small* interval, which at present we are not considering.

Now, although in good combinations the colours are rather far apart in the chromatic circle, it does not follow that all colours that are far apart make good combinations. When green, emerald-green, or bluish-green enters into a combination, it is apt to produce a harsh effect if the green is at all decided or covers much space. The enormous difficulty of managing full greens or bluish-greens is perfectly well understood by artists, and many of them avoid their use as far as possible. The presence in a picture of a very moderate amount of a colour approaching bluish-green or emerald-green excites in most persons a feeling of disgust, and causes a work otherwise good to appear cold and hard—very cold and hard. Corresponding to this, most artists seem to be of the opinion that the pigment known as emerald-green is more intense and saturated than any of the other colours used by them. From a purely optical point of view this would seem hardly to be the case : emerald-green reflects more white light mixed with its coloured rays than vermilion, and its luminosity is not out of proportion to those of vermilion or ultramarine-blue, if we adopt as our standard the luminosities of the corresponding colours in the spectrum. Hence we must seek elsewhere for the reason of its unusually intense action. The author is disposed to attribute this well-known intolerance of all full greens to the fact that green light exhausts the nervous power of the eye sooner than light of any other colour. This exhaustion is proved by the observation that the after-pictures, or accidental colours, are more vivid with green than with the other colours. (See Chapter VIII.) Now, as a general thing, very strong sensations are offensive when freely interspersed among those that are weaker ; thus Helmholtz has shown that discord in music is due to the presence of “beats,” which are merely rapid alternations of sound and silence following each other at such

intervals as to allow the sensitiveness of the ear to remain at a maximum, and hence producing disagreeably intense sensations which offend. Quite analogous to this is the action of a flickering light, which is both disagreeable and hurtful to the eye. This general principle, as it seems to the author, applies also to the matter now in hand : a green which optically may be the equivalent of a red, yellow, blue, or violet, nevertheless produces on the nerves of the eye a more powerful and exhausting sensation than these colours, and hence is out of harmony with them, or discordant. Besides this, and apart from these considerations, green is not a colour suggestive of light or warmth, but is what artists call cold ; the peculiar action above alluded to renders it intense as well as cold, and consequently painters are only able to employ it with a most cautious hand. Yellow conveys the idea of light, red that of warmth : if too much of either is present in a painting, the general effect is of course impaired ; but by a small over-dose of green, the picture is killed.

The colour which next to green acts most powerfully on the nerves of the eye is violet ; after that follows blue-violet (artificial ultramarine-blue). It so happens that, among the pigments at the disposal of the painter or decorator, violet has only a set of dull representatives ; hence it is not quite so easy to transgress in this direction as with green, for to obtain a violet which is at all the optical equivalent of vermilion or emerald-green, it is necessary to use some of the aniline colours. Blue-violet or artificial ultramarine-blue easily gives rise to cold and hard combinations, and large surfaces of it are apt to appear disagreeable if the hue is at all intense. Skies painted with blues that are too intense are easily ruined, and misjudgments in this direction are not entirely confined to the work of beginners or amateurs.

When the colours are arranged according to the order in which they exhaust the nervous power of the eye, it is

found that green heads the list; violet, blue-violet, and blue follow; then come red and orange, and last of all yellow. This is also about the order in which we are able to enjoy (or tolerate) positive colour in a painting; large masses of yellowish hues being often recognized only as communicating luminosity, while hues of orange or red-orange, darkened, are called brown, and considered as scarcely more positive than warm greys. From this it by no means follows that the introduction of large masses of positive green into paintings is always to be avoided; it is not advisable, unless it can be accomplished *successfully*, and without injury to the work as a chromatic composition. The ability to solve this problem in a brilliant manner is one of the signs which indicate an accomplished colourist; and, when the green is combined with blue, the task becomes still more difficult and success more praiseworthy. On the other hand, the handling of combinations of dull yellow, brown, grey, or bluish-grey is much easier, and, in fact, constitutes the first step by which beginners should approach more positive colour.

As stated above, hurtful contrast is one of the commonest reasons that render combinations of colour bad: as examples, we have orange and carmine, yellow and yellowish-green, green and cyan-blue. All the colours in the contrast-diagram, Fig. 131, that are less than 80° or 90° apart are more or less under the dominion of harmful contrast. These effects become still more pronounced when the colours have luminosities decidedly differing from those found in the spectrum, where yellow is the brightest and violet the darkest. (See Chapter III.) There are various modes of mitigating to a considerable extent the effects of hurtful contrast: a common one is to make one of the contending colours darker than its rival, or to assign to it a much smaller field; a third colour situated at a considerable distance in the chromatic circle is also sometimes added. Thus, for example, yellow and yellowish-green are im-

proved by adding to the combination a small quantity of violet or purplish-violet ; green and cyan-blue in the same way are helped by the addition of purple or orange. Harmful contrast in the matter of colour may also sometimes be concealed by strong light-and-shade effect, or by a large amount of gradation, which tends to enable all colours to maintain themselves against its influences ; beauty and variety of form also to some extent mask its effects. It may be added that apparent truth to nature sometimes causes harmful contrast to be overlooked or pardoned ; on the other hand, soiled or impure-looking tints, contradiction of nature either in colour or form, and indecision of handling, all are causes that intensify its action.

A combination may also be poor because the actual intensities of the two colours differ too much, although their position in the chromatic circle is advantageous ; thus, for example, the introduction of a quantity of chrome-yellow into a design produces harsh effects, which would be avoided by the use of the more modest yellow ochre. When this trouble exists in a high degree, the offending colour usually catches the eye of the observer at first glance, and before any of the other colours are fairly seen. A delicate colour-emphasis is by no means easy of attainment, and its lack produces on a chromatic composition effects quite analogous to the want of the corresponding quality in speaking or reading.

A combination may also be poor because it contains no decided representative of the warm colours, including under this term yellow and purple and the colours situated between them. There is reason to believe that the warm colours actually preponderate in the most attractive and brilliant chromatic compositions ; however this may be, it is certain that compositions founded almost exclusively on the colder colours, such as yellowish-green, green, blue, and violet, appear poor, and are apt to arouse in the mind of the beholder a feeling of more or less dissatisfaction. The

general preference for warm colour is somewhat analogous to that displayed for articles of food that have a tendency rather to sweetness than the reverse ; but, however interesting an inquiry as to the causes which during past ages have brought about this result might be, it evidently would not help us much in our present studies ; we are obliged to accept the fact, and make as good use of it as our skill and feeling for colour permit.

Thus far we have considered the effects that are produced when the colours are used in pairs ; they may, however, also be employed in triads. The studies that we have made with the contrast-diagram, Fig. 130, render it easy for us to select a series of triads that are free from the defect of hurtful contrast ; for this will be the case with all colours that are equally distant from each other in the diagram, or are separated by an angle of 120° ; and, when we examine the triads that have been most employed by artists and decorators, we find that this principle has actually been more or less closely observed. The triads that have been most extensively used are :

Spectral red, yellow, blue ;
 Purple-red, yellow, cyan-blue ;
 Orange, green, violet ;
 Orange, green, purple-violet.

In the second triad the colours are almost exactly 120° apart ; in the first the yellow is a little less than 90° from the red, and in fact forms with it a doubtful combination, which is only rendered good by the presence of the blue. In the third triad the orange and violet are about 90° apart, but are nearly equally distant from the green, and form, both of them, a good combination with it.

In the selection of colours for these triads a second principle also seems to have guided the choice of artists : there is an evident wish in each case that two out of the three should be *warm* colours, and in two of the triads the matter

of contrast has been somewhat sacrificed for the furtherance of this end. The desire to satisfy both these conditions of course greatly limits the number of triads, as an examination of the contrast-diagram shows ; and, in point of fact, in certain inferior triads which have been employed, one or both of these principles have necessarily to a considerable extent been neglected.

Carmine, yellow, and green

was, according to Brücke, a triad much used during the middle ages, though to us the combination is apt to appear somewhat hard and unrefined. Here we have two warm colours, but the matter of contrast is also twice sacrificed ; that is, slightly in the case of the carmine and yellow, and more with the yellow and green.

Orange-yellow, violet, and bluish-green

is an example of a combination which is poor not from defect of contrast, but because it contains two cold colours, one of them being the coldest in the chromatic circle.

Vermilion, green, and violet-blue

is a triad which has been extensively used in some of the Italian schools. At first sight we have here apparently two cold colours ; but, as the green was olive-green, the combination really amounts to

Vermilion, dark greenish-yellow, and violet-blue,

and corresponds in principle with those above given.

In the employment of any of these triads in painting or in ornament, the artist can, of course, vary the hue of the three colours through the small interval without destroying the definite character of the chromatic composition ; and even small quantities of foreign colours can also be added. When, however, they begin to assume importance in the combination, they destroy its peculiar character. White or grey can be introduced, and is often used with a happy effect, particularly in the triads

Orange, green, violet ;
 Purple-red, yellow, cyan-blue.

It is perhaps hardly necessary to dwell on the advantages of studying the relations of colours to each other by the use of pairs and triads, before more complicated arrangements are attempted. Many of the pairs furnish opportunities for the construction of beautiful chromatic compositions, and the practical study of colour in pairs and triads can not be too strongly urged. In constructing a chromatic composition, it is also of the first importance to determine at the outset what the leading elements are to be ; after this has been done, it will be comparatively easy to see what variations are allowable, and what are excluded. The most impressive and beautiful compositions are by no means those that contain the most colours ; far more can be attained by the use of a very few colours, properly selected, varied, and repeated in different shades, from the most luminous to the darkest.

We have now examined to some extent the good and the poor combinations of colour, and it may be as well to add a word with regard to the balance of colour ; for it is desirable that we should be able not only to select our colours properly, but also to provide them in quantities suitable for the production of the best effect. It has been a common opinion among English writers on colour, that the best result is attained by arranging the relative areas of the colours in a chromatic composition in such a way that a neutral grey would result if they all were mixed together. It is quite true that, if the colours were portioned out in this manner, there would be a balance of colour in an optical sense, though how far balance in an æsthetic sense would be attained is quite another question. Field in his "Chromatics" has given certain rules for obtaining an optical balance, and assumes that optical and æsthetic balance are one and the same thing. For example, he states that if

we take red, yellow, and blue, of corresponding intensities, then 5 parts of red, 3 parts of yellow, and 8 of blue will neutralize each other in a mixture, and produce grey ; also, 8 parts of orange with 11 of green and 13 of purple will produce the same result ; likewise 19 parts of citrine ("compound of orange and green"), 21 parts of russet ("orange and purple"), and 24 parts of a mixture of olive-green and purple. These rules are based on the supposition that red, yellow, and blue are fundamental colour-sensations, and when mixed produce white, though, as we have seen in Chapter IX., this is quite the reverse of being true. In a mixture of red, yellow, and blue, the yellow neutralizes the blue, since these colours are complementary, and the superfluous red strongly tinges this grey or white light, which then appears decidedly reddish. Field's actual experiments on mixing colours were made by transmitting white light through hollow glass wedges filled with coloured liquids ; but it is, as we have seen in Chapter X., impossible in this way to mix masses of coloured light. For example, the light which passes through a yellow and a blue wedge placed in contact is merely that which is not absorbed by either wedge, or which both the wedges allow to pass. Both wedges allow green light to pass, and stop almost all the other rays ; but from this it is not allowable to draw, as Field did, the inference that yellow light and blue light make green light when mixed, since we know with the utmost certainty that these two kinds of coloured light make grey or white light. Field's method gave entirely false results, and his conclusions based on them, including his so-called "chromatic equivalents," have therefore for us neither value nor meaning.

We return now to the proposition that the best effect is produced when the colours in a design are present in such proportions that a complete mixture of them would produce a neutral grey. It is very easy with our present knowledge to ascertain what areas we must assign to two

or more coloured surfaces in order to realize this effect. It is only necessary to combine, according to Maxwell's method, rotating disks which are painted with the pigments that are to be used in the chromatic composition. Let us examine this matter with the aid of a few actual examples. Taking the first of the triads, spectral red, yellow, and blue, we find that it is not possible to mix the colours in such proportions as to obtain a neutral grey; the yellow and blue neutralize each other, and the red then colours the mixture reddish. The same is true of the triad carmine, green, yellow: the mixture will be orange, yellowish, or greenish-yellow, according to the proportions. In the case of the two triads, purple-red, yellow, cyan-blue; and orange, green, violet, neutralization can be produced by mixture; and, when the colours are thus arranged, the result is more pleasing in the first than in the second case. If we take triads not much used in art, we meet with similar results; for example, vermilion, green, ultramarine-blue, when combined in such proportions as to furnish a grey, give a very unpleasing result, the cold colours being greatly in excess. But it is needless to multiply examples, as the reader can easily make these experiments for himself. If we examine the areas and intensities of the colours in the works of good colourists, we shall find that they are generally not such as to produce neutrality when the colours are mixed; that, on the contrary, as in most of the above experiments, there is always an excess of some positive colour. The presence of this excess gives a particular character to the composition, which will vary with the hue which is thus emphasized. Hence we see that this problem of the proper balance of colour is one which can not be solved exactly by any set of rules, but must be left to the feeling and judgment of the artist.

Attempts have been made from time to time to build up theories of colour based on analogies drawn from sound. The sensation of sound, however, is more particularly connected with time, that of sight with space; and these facts

necessitate a fundamental difference in the organs devoted to the reception of sound-waves and of light-waves ; and, on account of this difference between the eye and the ear, all such musical theories are quite worthless. Thus, our perception for colour does not even extend over one octave, while in music seven octaves are employed. When two musical sounds are mingled, we have accord or discord, and the ear of a practised musician can recognize the separate notes that are struck ; but, when two masses of coloured light are mingled, a new colour is produced, in which the original constituents can not be recognized even by the eye of a painter. Thus, red and green light when mixed furnish yellow light ; and this yellow is in no way to be distinguished from the yellow light of the spectrum, except that it is somewhat paler and looks as though it had been mixed with a certain amount of white light. Again, in music the *intervals* are definite and easily recognized relations, as, for example, that of the fundamental with its fifth or octave ; we can calculate the corresponding intervals for coloured light, but they can not be accurately recognized even by the most skillful painter. In painting we are constantly obliged to advance from one colour to another by insensible steps, but a proceeding like this in music gives rise to sounds that are ludicrous. These facts, which are susceptible of the most rigid proof, may suffice to show that a fundamental difference exists between the sensations of vision and hearing, and that any theory of colour based on our musical experience must rest on fancy rather than fact.

CHAPTER XVIII.

ON THE USE OF COLOUR IN PAINTING AND DECORATION.

THE power to perceive colour is not one of the most indispensable endowments of our race ; deprived of its possession, we should be able not only to exist, but even to attain a high state of intellectual and æsthetic cultivation. Eyes gifted merely with a sense for light and shade would answer quite well for most practical purposes, and they would still reveal to us in the material universe an amount of beauty far transcending our capacity for reception. "But over and above this we have received yet one more gift, something not quite necessary, a benediction as it were, in our sense for and enjoyment of colour."* It is hardly fair to say that without this gift nature would have appeared to us cold and bare ; still, we should have lost the enjoyment of the vast variety of pleasant and refined sensations produced by colour as such and by colour-combinations ; the magical drapery which is thus cast over the visible world would have given place merely to the simpler and more logical gradations of light and shade. The love of colour is a part of our constitution as much as the love of music ; it develops itself early in childhood, and we see it exhibited by savage as well as cultivated races. We find the love of colour manifesting and making itself felt in the strangest places ; even the most profound mathematicians

* From an address by Professor Stephen Alexander.

are never weary of studying the colours of polarized light, and there can be no doubt that the attractive power of colour has contributed largely to swell the mathematical literature of this subject. The solar spectrum with its gorgeous tints was for many years before the discoveries of Kirchhoff and Bunsen a favourite, almost a beloved, subject of study with physicists; the great reward of this devotion was withheld for nearly half a century; divested of its colour-charm, attracting less study, the spectrum might still have remained an enigma for another hundred years.

Colour is less important than form, but casts over it a peculiar charm. If form is wrongly seen or falsely represented, we feel as though "the foundations were shaken"; if the colour is bad, we are simply disgusted. Colour does not assist in developing form; it ornaments and at the same time slightly disguises it: we are content to miss some of the modeling of a beautiful face for the sake of the colour-gradations which adorn and enliven it.

The aims of painting and decorative art are quite divergent, and as a logical consequence it results that the use made by them of colour is essentially different. The object of painting is the production, by the use of colour, of more or less perfect representations of natural objects. These attempts are always made in a serious spirit; that is, they are always accompanied by some earnest effort at realization. If the work is done directly from nature, and is at the same time elaborate, it will consist of an attempt to represent, not all the facts presented by the scene, but only certain classes of facts, namely, such as are considered by the artist most important or most pictorial, or to harmonize best with each other. If it is a mere sketch, it will include not nearly so many facts; and finally, if it is merely a rough colour-note, it will contain perhaps only a few suggestions belonging to a single class. But in all this apparently careless and rough work the painter really deals with form, light and shade, and colour, in a serious spirit, the conven-

tionalisms that are introduced being necessitated by lack of time or by choice of certain classes of facts to the exclusion of others. The same is true of imaginative painting: the form, light and shade, and colour are such as might exist or might be imagined to exist ; our fundamental notions about these matters are not flatly contradicted. From this it follows that the painter is to a considerable extent restricted in the choice of his tints ; he must mainly use the pale unsaturated colours of nature, and must often employ colour-combinations that would be rejected by the decorator. Unlike the latter, he makes enormous use of gradation in light and shade and in colour ; labours to express distance, and strives to carry the eye beneath the surface of his pigments ; is delighted to hide as it were his very colour, and to leave the observer in doubt as to its nature.

In decorative art, on the other hand, the main object is to beautify a surface by the use of colour rather than to give a representation of the facts of nature. Rich and intense colours are often selected, and their effect is heightened by the free use of gold and silver or white and black ; combinations are chosen for their beauty and effectiveness, and no serious effort is made to lead the eye under the surface. Accurate representations of natural objects are avoided ; conventional substitutes are used ; they serve to give variety and furnish an excuse for the introduction of colour, which should be beautiful in itself apart from any reference to the object represented. Accurate, realistic representations of natural objects mark the decline and decay of decorative art. A painting is a representation of something which is not present ; an ornamented surface is essentially not a representation of a beautiful absent object, but is the beautiful object itself ; and we dislike to see it forsaking its childlike independence and attempting at the same time both to be and to represent something beautiful. Again, ornamental colour is used for the production of a result which is delightful, while in painting the aim of the

artist may be to represent sorrow, or even a tragic effect. From all this it follows that the ornamenteer enjoys an amount of freedom in the original construction of his chromatic composition which is denied to the painter, who is compelled by profession to treat nature with at least a fair degree of seeming respect. The general structure of the colour-composition, however, being once determined, the fancy and poetic feeling even of the decorator are compelled to play within limits more narrow than would be supposed by the casual observer. It is not artistic or scientific rules that hedge up the path, but his own taste and feeling for colour, and the desire to obtain the best result possible under the given conditions. In point of fact, colour can only be used successfully by those who love it for its own sake apart from form, and who have a distinctly developed colour-talent or -faculty ; training or the observance of rules will not supply or conceal the absence of this capacity in any individual case, however much they may do for the gradual colour-education of the race.

From the foregoing it is evident that the positions occupied by colour in decoration and in painting are essentially different, colour being used in the latter primarily as the means of accomplishing an end, while in decoration it constitutes to a much greater degree the end itself. The links which connect decoration with painting are very numerous, and the mode of employing colour varies considerably according as we deal with pure decoration, or with one of the stages where it begins to merge into painting.

The simplest form of colour-decoration is found in those cases where surfaces are enlivened with a uniform layer of colour for the purpose of rendering their appearance more attractive : thus woven stuffs are dyed with uniform hues, more or less bright ; buildings are painted with various sober tints ; articles of furniture and their coverings are treated in a similar manner.

The use of several colours upon the same surface gives rise to a more complicated species of ornamentation. In its very simplest form we have merely bands of colour, or geometrical patterns made of squares, triangles, or hexagons. Here the artist has the maximum amount of freedom in the choice of colour, the surfaces over which it is spread being of the same form and size, and hence of the same degree of importance. In such cases the chromatic composition depends entirely on the taste and fancy of the decorator, who is much less restricted in his selection than with surfaces which from the start are unequal in size, and hence vary in importance. After these simplest of all patterns follow those that are more complicated, such as arabesques, fanciful arrangements of straight and curved lines, or mere suggestions taken from leaves, flowers, feathers, and other objects. Even in these, the choice of the colours is not necessarily influenced by the actual colours of the objects represented, but is regulated by artistic motives, so that the true colours of objects are often replaced even by silver or gold. Advancing a step, we have natural objects, leaves, flowers, figures of men or animals, used as ornaments, but treated in a conventional manner, some attention, however, being paid to their natural or local colours, as well as to their actual forms. In such compositions the use of gold or silver as background or as tracery, also the constant employment of contours more or less decided, the absence of shadows, and the frank disregard of local colour where it does not suit the artist, all emphasize the fact that nothing beyond decoration is intended. Up to this point the artist is still guided in his choice of hues by the wish of making a chromatic composition that shall be beautiful in its soft subdued tints, or brilliant and gorgeous with its rich display of colours; hence intense and saturated hues are often arranged in such a way as to appear by contrast still more brilliant; gold and silver, black and white, add to the effect; but no attempt is made to imitate nature

in a realistic sense. When, however, we go some steps further, and undertake to reproduce natural objects in a serious spirit, the whole matter is entirely changed ; when we see groups of flowers accurately drawn in their natural colours, correct representations of animals or of the human form, complete landscapes or views of cities, we can be certain that we have left the region of true ornamentation and entered another which is quite different. A great part of our modern European decoration is really painting—misapplied.

We return now to a brief consideration of monochromy, or decoration in a single colour. In order to avoid the monotony attendant on the use of a uniform surface of colour, lighter and darker shades of the same hue are very often employed. These not only give more variety, but serve also as a means of introducing various ornamental forms, such as borders, centre-pieces, etc. Monochromy is advantageously employed when it is desired, on the one hand, to avoid the brilliancy attendant on the introduction of several distinct colours, and on the other the dullness consequent on the exclusive use of a single tone. It is much used in wall-painting, also in woven stuffs intended for articles of dress or for covering furniture, and for many other purposes.

In monochromatic designs the small interval is very frequently employed : for example, in using red, the artist will employ for the lighter shades a red that is slightly more orange than the general ground ; for the darker, one that is rather more purplish. In this use of the small interval, regard is to be had to the hues which colour assumes under different degrees of illumination ; this matter is fully explained in Chapter XVII. Monochromatic designs can furthermore be enlivened by ornamenting them with gold, either alone or in connection with a small amount of positive colour. The use of black and white is, however, best avoided, as it furnishes occasion for the production of

contrast-colours which interfere with the general effect. (See chapter on Contrast.)

In polychromy a number of distinct colours are employed simultaneously, with or without gold and silver, white and black. The laws which guide the selection of colours in this kind of ornamentation have already been considered in Chapter XVII. Saturated and intense colours are often used to cover only the smaller surfaces ; they are then balanced or contrasted with colours of less intensity spread over proportionately larger surfaces. In purely decorative polychromy we deal mainly with rich and beautiful arrangements of colour disposed in fanciful forms ; natural objects, if introduced at all, being treated conventionally. In the composition of such designs, however, the artist is controlled to a considerable extent by the shape and size of the spaces which the colours are destined to occupy ; the large masses of the composition in the best polychromy being worked out in colours of proper intensity, which make by themselves a broad design, over which again smaller designs are wrought out in the same and in different colours. As remarked by Owen Jones,* "The secret of success is the production of a broad general effect by the repetition of a few simple elements, variety being sought rather in the arrangement of the several portions of the design than in the multiplication of varied forms."

In the best polychromy great use is made of outlines or contours ; they are employed to separate ornaments from the ground on which they are placed, particularly when the two do not differ greatly in colour. Colours that differ considerably are prevented by contours, on the other hand, from melting into each other and thus giving rise to mixture tints ; in other words, each colour is made by the separating outline to retain its proper position. Contours when used for this purpose may be light or dark coloured,

* "Grammar of Ornament," London, 1856.

or even black. If the ornament is lighter than the ground, the contour is made still lighter; if darker, the contour will be still darker. In the best decoration the figures of men and animals, when introduced, are surrounded with decided contours which emphasize the fact that realistic representation is not intended. Contours are also made white or golden; they then become an independent part of the ornamentation. Contours consisting of several lines of gold and silver, white and black, are often used to separate colours that do not harmonize particularly well together, though, considered in a large way, they may still belong in the compositions. These pronounced contours are never intended to disappear when viewed at a distance, but form a new ornamental element; hence their shapes will often vary more or less from the form of the spaces which they enclose.

In the richest polychromy the designs are mainly worked out in intense or saturated colours, along with gold and silver, white and black. Dark and pale tints are not much employed as such, but are produced by black or white tracery on the coloured grounds. Corresponding to this, variations of the dominant colours are effected, not by the introduction of new tints, but by placing small quantities of pure colour on a differently coloured ground; the two colours then blend on the retina of the observer and give rise to the desired hue. For example, in a richly ornamented table-cover from Cairo, the writer noticed that the use of a fine tracery of white on a blue ground gave rise to the appearance of a lighter blue, which persisted at a distance; in the border a pure red was made to appear orange-red by a tracery of yellow; in other portions, small red and white ornaments on a blue ground produced at a distance the effect of a light violet tint.

In the superb decoration of the Alhambra, the colours employed on the stucco work are red, blue, and gold; purple, orange, and green are found only in the mosaic dados.

The colours are either directly separated by narrow white lines, or indirectly by the shadows due to the projecting portions of the ornamentation. Masses of colour are never allowed to come into contact. The blue and gold are often, however, interwoven purposely, so as to produce at a distance a soft violet hue ; on this ground designs are traced in gold and red, the gold figures being much larger than the red ; or, on the same ground sometimes, will be found figures in white with small touches of red. The principle for the production of new colours above mentioned is constantly employed : blue and white blend to a light blue ; blue, white, and red furnish a light violet or purple hue ; while red and gold mingle to a rich, subdued orange. Sometimes in these designs the gold greatly predominates, as in the "Hall of the Ambassadors" or in the "Court of the Lions"; here we find a mass of wonderful gold tracery, with only small portions of red and blue imbedded in it. On the dados the mosaic designs are often worked out in red-purple, green, orange-yellow, and a dark blue of but slight intensity, the ground being grey. Narrow contours of white separate the colours from the ground. To this series light blue is sometimes added, or we find combinations of orange-yellow, dark blue, and green or purple ; dark blue and orange-yellow ; or simply orange-yellow and small spaces of dark blue, the grounds in all these cases being of a medium grey. The general effect of the colour of the mosaics is cool and somewhat thin ; it rests the eye which has gazed on the magnificent displays placed above, or prepares it by the contrast for new enjoyment.

True polychromy has not been very successfully cultivated in Europe since the time of the Renaissance, painting having to a great extent usurped its place. Hence in modern times we find not only our porcelain, carpets, window-shades, but the walls themselves and whatever else it may be possible to decorate, covered with groups of flowers, figures, or landscapes, architectural views, copies of cele-

brated paintings—all executed with as much pretended truth to nature as the purchaser is able or willing to reward. It is hardly necessary to add that the taste which produces or demands such false decoration, while it may have much to excuse, has but little to recommend it; and it is not to be expected that any general improvement can be effected till the public at large learns better to distinguish between genuine decoration and genuine painting.

In decorative art the element of colour is more important than that of form: it is essential that the lines should be graceful and show fancy or even poetic feeling; but we do not demand, or even desire, that they should be expressive of form in a realistic sense. Just the reverse is true in painting: here, colour is subordinate to form. Nevertheless, its importance still remains very great, and it is trifling to attempt to adorn with colour that which is really only a light-and-shade drawing. The chromatic compositions of a painting should from the start receive the most careful and loving attention; otherwise it is better to work in simple black and white.

The links which connect designs in mere light and shade with works in colour run about as follows: We have, as the first step, pictures executed essentially in one tint, but with endless small modifications. In this way a peculiar luminous glow is introduced which is never exhibited by designs executed solely in black and white, or indeed in any one tint. As examples of this kind of work we may mention drawings in sepia or bistre, in which the tint is varied by the introduction here and there of different quantities of some other brown having a reddish, yellowish, or orange hue. In the next stage the design is worked out essentially in bluish and brownish tints. If a landscape, the distance and much of the sky will be greyish-blue; the foreground, on the other hand, a rich warm brown, with here and there a few touches of more positive color. The blue of the dis-

tance will be variously modified, having often a greenish hue, and being replaced in the more highly illuminated portions by a yellowish tint. No real attempt will be made to render correctly the natural colours of the objects depicted, except as they happen to fall in with the system adopted. By this mode of working, distance and luminosity can be represented far more effectively than by the mere use of black and white. Designs of this kind merge by insensible degrees into others, where the strong browns of the foreground vanish, and are replaced by a set of tints which, though not very positive, yet represent the actual colours of the scene somewhat more truly. The rather uniform bluish-grey of the distance, also, is exchanged for a greater variety of cool bluish tints, and faint violet and purple hues begin to mingle with the other colours. The yellows and orange-yellows become more pronounced, but decided greens are not admitted except in small touches, and as the local colour requires it; large masses also of any other strong colours that happen to be present in the scene will be suggested rather than represented. In designs of this kind there is a good deal of room for the interchange and play of different hues, and they make at first sight the impression of being veritable works in colour. Many of Turner's earlier drawings were executed in accordance with these methods, which allow the student gradually to encounter and overcome the difficulties of colour. The substitution of paler tints for the real colours of the scene, and particularly the exclusion of green, a colour always difficult to manage, diminish the possibilities of entanglement in harsh or bad combinations of colour, and render more easy the attainment of harmony. This mode of using colour is of course conventional, and pictures of this kind are not to be regarded as executed in colour, in the full sense of the word. Among genuine works in colour, the simplest are those painted essentially with a single pair of colours, variously modified or combined with grey; colours widely separated in the chro-

matic circle from the selected pair being admitted only in small masses or subdued tones. After these follow chromatic compositions in which three colours with their modifications are systematically employed in the same manner, to the exclusion as far as possible of all others. The character of these compositions will again vary according as the light illuminating the scene in nature is supposed to be white or coloured. If yellowish, the blue and violet hues will be more or less suppressed, the greens more yellowish, while the red, orange, and yellow tints will gain in intensity. Just the reverse will occur under a bluish illumination. The practice of employing an illumination of one dominant colour, which spreads itself over the whole picture, modifying all the tints, is very common among artists, and has often been successfully used for the production of impressive effects.

Good colour depends greatly on what may be called the chromatic composition of the picture. The plan for this should be most carefully considered and worked out beforehand, even with reference to minor details; the colours should be selected and arranged so that they all help each other either by sympathy or by contrast—so that no one could be altered or spared without sensibly impairing the general effect. No rules will enable a painter coldly to construct chromatic compositions of this character; the constant study of colour in nature and in the works of great colourists will do much, but even more important still is the possession of a natural feeling for what may be called the poetry of colour, which leads the artist almost instinctively to seize on colour-melodies as they occur in nature, and afterward to reproduce them on canvas, with such additions or modifications as his feeling for colour impels him to make. Thus it is often advisable to deepen nature's colours somewhat, as in the case of the pale-tinted greys of a distance, or in the mere suggestions of colour often presented by flesh. In this process the proportions of the coloured and

white light of nature are somewhat altered, and the coloured element made more prominent. On the other hand, all the colours may be made paler and more greyish than those of nature ; yet if they retain their proper relations, if all are correspondingly affected, the harmony will not be disturbed, and a design of this character will still be, from a chromatic point of view, logical. If the cold hues, the greens and blues, are allowed to stand in full strength, while the warm colours, red, orange, and yellow, are weakened, a particularly bad effect is produced.

Good colour, then, depends primarily on the chromatic compositions ; next in importance on the drawing, including under this term outline and light and shade. The want of good, decided, and approximately accurate drawing is one of the most common causes that ruin the colour of paintings. Powerful drawing adds enormously to the value of the tints in a coloured work when they are at all delicate, or when the combination contains doubtful or poor colour-contrasts, which in point of fact is a case common enough in nature. Here the artist is obliged either to reject the material furnished by nature, or to treat it in nature's own way ; that is, the drawing must be excellent and the gradation endless. Poor or bad combinations of colour are almost converted into good combinations by sufficient gradation. When all the tints are pale, as in distances, it is almost impossible to cause them to appear luminous or brilliant without the aid of delicate and accurate drawing. There is still another way in which the drawing influences the colour : perfectly clear, clean tints can be used, and will look well, where the same colours in a slightly soiled or dirty condition would be quite inadmissible. This results from the circumstance that helpful contrast is favoured by clean, even tints, while harmful contrast is strengthened by a dirty or spotty condition of the pigments. This is peculiarly true when the colours are not very positive, or are low in the scale ; the tints, if not clear and decided, instantly lose all

value and become a blemish. To insure this desirable appearance, called by artists purity, the colours must be laid on rapidly and with decision, and not afterward gradually corrected ; but to do this requires the hand of an accomplished draughtsman.

The advance from drawing to painting should be gradual, and no serious attempts in colour should be made till the student has attained undoubted proficiency in outline and in light and shade. Amateurs almost universally abandon black and white for colour at a very early stage, and this circumstance alone precludes all chance of progress. The stage of advancement can, however, be very easily ascertained. Thus, for example, if the student can not execute a perfectly satisfactory study of any class of subjects in outline with slight shade, then there is no use in trying full light and shade ; if it is impossible for him to draw the objects in full light and shade in a rather masterly way, then there is no use in attempting colour. The method employed by Turner of gradually effecting the transition from black and white to colour has been just described, and is worthy of the most careful study. In making the first essays at colour, it is advantageous to execute careful studies of the scene in full light and shade, but to note down the colours only in writing and in the memory. Afterward, from these notes and the black and white drawing, a colour-sketch may be attempted, *away* from the scene. By this means fluctuations of judgment about the colours and their relations are avoided, and, though the painting may be all wrong, it has at least a chance of being executed on one plan, and its frank errors can afterward be ascertained. Beginners when working in the presence of nature are apt to keep constantly altering the plan of the chromatic composition, in the hope that it will at last come right, and thus waste much time. Artists under similar circumstances deliberately make up their minds beforehand what colour-facts they will take, what

view of the problem they will adopt, and adhere to this decision unflinchingly.

After some progress has been made, the colour-sketches that are attempted directly from nature should be simple and executed with reference to *colour*, the element of form being kept quite subordinate. The very natural desire to make something that will afterward look like a picture is to be suppressed, and the work performed rather with an eye to the remote future. Beginners always neglect the large relations of light and shade and colour, dwelling on those that are small ; whereas the aim of the true artist is the production of a broad general effect by the use of a few masses of colour, properly interchanged and contrasted, variety being gained not so much by the introduction of new colours as by the repetition of the main chords. Various modes of contending with this evil have been suggested. One of the simplest is making the colour-sketches so small that there is hardly room for anything but the main masses of colour, the use of small brushes meanwhile being avoided. Corresponding to this, it is frequently found that if a picture by a beginner is actually cut up into two or more parts, the fragments thus produced are better in the matter of chromatic composition than the original.

There are several other stumbling-blocks that are encountered with much regularity by those who make their first essays in colour. One of the most important is the tendency to employ in the painting colours that are vastly more intense than those displayed by nature. The colours of nature are usually pale and low in intensity, even when they make upon the beholder just the reverse impression ; and a practical knowledge of this fact is not to be immediately attained. Distant fields, for instance, often appear to be of a rather intense green hue, when the colour *actually* presented to the eye may be scarcely more than a grey having in it a faint tinge of green. The actual colours

exhibited by different parts of a landscape may be advantageously studied by isolating them; according to a suggestion of Ruskin, with the aid of a small aperture, half an inch square, in a piece of white cardboard, held at arm's length. By this simple proceeding the student can convince himself of the true nature of the tints composing a scene, for when thus isolated they are not heightened by contrast. With such square patches of colour, the judgment is not so much affected by the *memory* of the hues which the objects exhibit at short distances, or by what artists call their local colour. The local colour of grass is green, but if placed at a distance it may display a great variety of pale tints, scarcely even greenish; yet owing to the action of the memory the distant grass still suggests, not the idea of a variety of pale delicate greys, but of its local colour, green. The illustration is very old, but the principle applies not only to the greens, but to all colours: all will be altered by distance, by the brightness of the illumination or by its colour. The hues of all objects are also greatly affected by their surroundings, as explained in the chapter on contrast; and this is another source of perplexity and confusion to the beginner, who is constantly led astray by appearances due to this cause. The extent of the difficulty can be appreciated when we remember that contrast affects not only the intensity of the colour, but its position in the chromatic circle, and also its apparent luminosity, and is particularly lively in the case of the pale colours of nature. It is as well to meet this difficulty fairly face to face, and, instead of spending all the disposable time in endeavoring to solve the riddles of contrast presented by nature, to reverse the process, and occasionally to construct in the studio simple chromatic compositions founded on the known laws of contrast, and thus study its effects by experiment as well as by observation.

The appearance of colour, as has been explained in another chapter, depends also greatly on gradation; colour

which is uniform appearing hard and disagreeable, while the same tint when gently varied becomes pleasing as well as truer to nature. Gradation of colour is almost universal in nature, and a considerable part of the education of the student consists in its study and practice. The uneducated eye feels the effect of gradation in nature and in a painting, but is quite unable to trace the delicate play of colour and light and shade on which it depends. Skill in the use of gradation gives the artist great power to manage large masses of nearly uniform colour, and an astonishing mastery over colour-combinations which inherently are of doubtful value.

The enormous influence of good, decided drawing has already been alluded to, but we return again to the matter for a moment, to insist on the added lustre which all the tints of a painting acquire when connected with good, well wrought-out light-and-shade effect. The beginner can most easily convince himself of the great influence which the light-and-shade effect exercises on the colour, by copying the engraving of some simple subject by a master in such colours as may seem most appropriate, and then comparing the coloring thus obtained with that of his own original designs. The selection of pigments in both cases is by the same hand, but it will be found that the masterly light and shade has given a value even to the colours, which without this little plagiarism they would not have possessed.

In painting, the selection of subjects on account of their chromatic qualities is a very important element of success. It is only by experience that artists gradually learn better and better how to select their subjects, and the mistakes of beginners in this respect are often a source of prolonged discouragement. Subjects which contain much green are invariably difficult to manage, and should as far as possible be avoided in the earlier stages ; green fields, green trees, green mountains, all need great skill if the colour is rendered with any approach to fullness. This is the reason

that the older landscapists lowered the colour of their trees to a dull olive-green, and even to brown. Combinations of green, blue, and grey or white are very common in nature, but difficult to handle, and necessitate the use of an unusual amount of gradation. From a chromatic point of view the combination is poor ; as seen in nature, we do not value it less on that account, perhaps more. It is delightful to see how much can be accomplished with elements of such doubtful value. Again, effects which are much dependent for beauty on very high degrees of luminosity are difficult, for their pale colours, when transferred to canvas and robbed of their natural luminosity, are apt to appear tame enough. In the same category we must place distances, with their excessively pale, delicate tints. The colouring in nature seems very brilliant, but in point of fact the effect is produced partly by mere luminosity, and partly by the aid of tints differing so slightly from each other and from grey that the problem of imitation, either literal or free, is not at all easy.

We might go on in this way adding to the catalogue of art difficulties, but perhaps it will be asked, What subjects are easy ? The truthful answer is simply, that all are difficult if even a moderate degree of excellence is demanded. The painter who wishes to excel in colour devotes his life to this object, and is constantly accumulating studies and sketches from nature of all kinds of subjects, some quite elaborate, others with less detail, many mere colour-notes. Quite often beautiful effects of colour in nature last only a few minutes ; these will be treasured in the memory and transferred to paper or canvas the next day, the sketch being completed only far enough to fix the facts in the memory of the artist. Many experimental sketches will be made, not directly from nature, but with a view, as it were, of guessing at the elements on which certain difficult or evanescent chromatic effects depend, and also for the purpose of ascertaining their relations to mere light and shade.

This varied work in colour will be accompanied by constant practice in black and white for light and shade, and in outline for form, since bad drawing is ruinous to colour. All the while there will be more or less anxious study of the works of good colourists, ancient and modern ; and this work will be pushed on month after month with patient energy, till, after a score of years or so, the student finally, if gifted, blossoms out into a colourist.

NOTE ON TWO RECENT THEORIES OF COLOUR.

HERING has lately proposed a theory of colour which is quite different from that of Young. According to the new theory, the retina is provided with three visual substances, and the fundamental sensations are not three but six:

Black and White.
Red and Green.
Blue and Yellow.

Each of these three pairs corresponds to an assimilation or diassimilation process in one of the visual substances; thus red light acts on the red-green substance in exactly the opposite way from green light, and when both kinds of light are present in suitable proportions a balance is effected, and both sensations, red and green, vanish.

Furthermore, according to this theory, all the colours of the spectrum also affect the black and white substance in the same way that white light does; for example, red light affects the red-green substance and produces the sensation of red, but it also acts on the white-black substance, and the sensation of red is mingled with that of white—to a large degree. Consequently, according to this theory, the white which is produced by mixtures of red and green light ought to have a less intensity than the sum of the separate components; but according to the experiments of the author this is not the case.* For further details the reader is referred to the original paper, "*Lehre vom Lichtsinne*," Vienna, 1878.

In 1876 F. Boll discovered that the retina contained a red or purple substance that quickly disappeared on exposure to light. Boll and Kühne have both studied the effect of monochromatic light on this coloured substance, and it was found that red light intensified the hue at first and afterward caused it to fade slowly. The action of yellow light was slow; green, blue, and violet light acted more quickly. On observations of this charac-

* "*American Journal of Science and Arts*," October, 1877.

ter Kühne has constructed a theory of vision. He supposes that the waves of light give rise in the retina to different compounds according to their length, and thus produce the different colour-sensations. If three such compounds are thus produced, giving rise to the sensations red, green, and violet, then this new theory is identical with that of Young; if there are five such compounds, furnishing the sensations red, yellow, green, blue, violet, then the apparatus for yellow and blue has been duplicated in the retina, since it can be shown that a mixture of the sensations red and green gives that of yellow, a mixture of green and violet that of blue. Good reasons can also be adduced to render probable the idea that yellow and blue are not fundamental sensations, but mixtures (compare the observations of Bezold in Chapter XII.). For additional information the reader is referred to the papers of Kühne published in the "Verhandlungen des Naturhistorische-medicinischen Vereins zu Heidelberg, 1877-'79."



INDEX.

A

Abnormal perception of colour, 92.
 Absorption, production of colour by, 65.
 Absorption and true mixture of light compared, 143.
 Absorption of light by stained glass, 65.
 Agassiz, A., observations of on colour of flounders, 101.
 Airy opposed to Brewster's theory, 109.
 Albert on colour-photography, 87.
 Alhambra, decoration of, 312.
 All pigments reflect some white light, 76.
 Antique glass, colours of, 52.
 Aubert on mixtures of blue and white, 196;
 relative luminosity of white and black paper, 183; sensitiveness of eye to mixtures of white and coloured light, 89.

B

Bert, observations of on chameleon, 101;
 on crustaceans, 10.
 Bezold, prismatic colours change with their brightness, 181.
 Bierstadt, experiments of in colour-photography, 87.
 Blake, Eli, his mode of recomposing white light, 29.
 Blue, complement of, 177.
 Bokowa, Maria, artificial colour-blindness of, 97.
 Brewster, Sir David, colour theory of, 108;
 discoverer of cross and rings, 47.
 Brücke, his apparatus for complementary colours, 161; observations on mixtures of blue and white, 196.
 Brücke's solution, imitates sky tints, 154.
 Bunsen's experiment on colour of water, 81.

C

Calculation of number of visible tints, 40.
 Campbell, J., experiments on photographing colours by, 86.
 Chameleon, its power of imitating colours, 101.
 Charts, colour, 213, 220.
 Chevreul, colour-chart of, 222.
 Chrome-yellow, spectrum of, 76.

Colour, abnormal perception of, 92; apparent spreading of, 284; balance of, 301, 303; by moonlight, 187; change of, with wavelength, 17, 27; changed by illumination, 181; effect of lamp-light on, 154; gradation of, 276; has more than one complement, 172; how affected by mingling it with white, 194; is subjective, 17; less important than form, 306; musical theories of, 303; of vegetation, 82; of water, 81; produced by absorption, 65; produced by dispersion, 17; produced by electric current, 9; produced by opalescent media, 53; production of by interference, 50; relative luminosity of dependent on degree of illumination, 189; reproduction of by photography, 86; sensation of, produced by white light, 92; value of, from practical point of view, 305.

Colour and wave-length do not change equally, 27.

Colour-blindness, 95, 96; of artists, 100; means of helping, 98; to green, 98; to red, 96.

Colour-chart, Chevreul's, 222; of Du Fay, 222; of Le Blond, 222.

Colour-charts, 213, 220.

Colour-combinations, bad, 292; bad owing to absence of warm colours, 298; bad owing to intensity, 298; pairs, 286-299.

Colour-cone, 216; and cylinder, impossible to execute, 217.

Colour-contrast, 235-273.

Colour-cylinders, 215.

Colour-diagram, Maxwell's, 224; Rood's, 233.

Colour-equations, 184.

Colour-sensations that are not fundamental, 115.

Colour-theory of Brewster, 108; of Young, 113; of Young and Helmholtz, 113.

Colour-triangle, 221.

Coloured light when bright becomes more yellowish, 181-183.

Coloured photographs, indirect process, 87.

Coloured silk and wool compared, 79.

Colours can be too pure and intense, 80; combined in triads, 299-301; in combination, mode of studying, 290; fundamental, defined, 120; in mixture represented by

- weights, 218; mixture of by binocular vision, 158; mixture of by Lambert's apparatus, 139; mixture of on retina of observer, 279; of metals, 84; of ordinary objects due to absorption, 65; of pigments due to absorption, 65; of prismatic spectrum, 18; of woven fabrics due to absorption, 78; photometric, comparisons of not absolute, 190; prismatic, change due to brightness, 181.
- Colours, complementary, 161; explained by Young's theory, 176; by gas-light, 173; in combination, 294; of polarized light rather pale, 177.
- Complementary colours, by gas-light, 173; explained by Young's theory, 176; method of studying with Maxwell's disks, 167; luminosity of, 164; no fixed relation between their wave-lengths, 175; of polarized light are rather pale, 177; table of, 163.
- Constants of colour, 30-210.
- Contours, 311.
- Contrast, 235-273; experiment with shadows, 254; hurtful, 297; intensity of colours being different, 263; of black, white, and grey, 267; of black, white, and grey with colours, 270; of pale and dark colours, 253-263; simultaneous, 241-245; strength with different colours, 261; successive, 235-242; table of effects of, 245.
- Contrast-circles, 248.
- Contrast-diagram, 250.
- Cross and rings produced by polarized light, 47.
- Cross, C., experiments of in colour-photography, 87.
- Curves for action of red, green, and violet on the eye, 198.
- D**
- Dalton, colour-blindness of, 97.
- Dalton's eye-piece, 36.
- D'Arcy on duration of impression on retina, 203.
- Dark lines of spectrum, 20.
- Decoration, different kinds of, 309; false aim in, 307, 313; use of one colour in, 308, 310; use of several colours, 309, 311.
- Decoration and painting divergent in aim, 306.
- De Haldat on binocular perception of colour, 159.
- Dichroöscope, Dove's, 137.
- Diffraction grating, 23; Rutherford's, *ib.*
- Diffraction spectrum, 23.
- Disks, complementary, 170 Maxwell's, 109; rotating, used in the study of Young's theory, 185.
- Dispersion, production of colour by, 17.
- Dove on binocular perception of colour, 159; his comparison of effects of absorption and true mixture of light, 143; dichroöscope of, 137; his method of studying complementary colours, 165; observations on relative luminosity of red and blue, 189; photometric experiments on revolving disks, 205; theory of lustre, 280.
- Draper, H., opposed to Brewster's theory, 109.
- Drawing, importance of, 317, 321.
- Du Fay, colour-chart of, 222.
- Duration of impression on retina, 202; in case of animals in motion, 208; in case of ocean waves, 207.
- E**
- Electricity, production of colour by, 95.
- Emerald-green, spectrum of, 75.
- Erythroscope, 83.
- Etchings, blending of white and black on retina of observer, 232.
- Eye, colour of, 58; more sensitive to change of wave-length in certain regions of the spectrum, 27.
- F**
- Favre, examination of colour-blind persons by, 99.
- Feathers, colour of, 50.
- Fechner on colours of after-images, 93.
- Field, chromatic equivalents of, 301; experiments on pigments by, 88, 89.
- Fixed lines of solar spectrum, 20.
- Fluorescence, production of colour by, 62.
- Foucault on binocular perception of colour, 159.
- Fraunhofer, discovery of fixed lines by, 20.
- Fundamental colours defined, 120; intensity of, in prismatic spectrum, 123; Wunsch on, 122.
- Fundamental colour-sensations, how determined, 115.
- G**
- Gas-light, effects of, on colours, 154.
- Gibbs, Wolcott, on duration of impression of prismatic colours, 206.
- Glass, opalescent, 55.
- Glass under strain, colour of by polarized light, 48.
- Gold used in painting, 85.
- Gradation of colour, 276; rapid, often unpleasant, 275; subordinate in decoration, 283.
- Green in colour-combinations, 295.
- Grunow, William, spectrometer of, 21.
- H**
- Harris, colour-blindness of, 99.
- Helmholtz on colour-blindness, 97; colour-blind zone of normal eye, 97; colours of after-images, 93; experiment of with blue and yellow glass, 183; on fundamental colours, 120: mixtures of blue and yellow, 190; mixture of prismatic colours, 111, 126; no fixed relation exists between wave-lengths of complementary colours, 175; prismatic colours change with their brightness, 181.
- Helmholtz and Young, colour theory of, 113.
- Helmholtz's spiral disk for after-images, 93.
- Hering's theory of colour, 324.
- Holmgren, examination of colour-blind persons by, 99.

Huddart, remarkable case of colour-blindness, 99.
Hue, 36.

I

Illumination, monochromatic, 102.
Indigo, complement of, 178; its real colour, 21; term improperly used by Newton, *ib.*; unfit designation of spectral hue, *ib.*
Insects, colour of, 51.
Interval, small, 278.

K

Kühne's theory of colour, 324.

L

Lambert, apparatus of for mixing coloured light, 110; his apparatus used for mixing colours, 189; colour-chart of, 222.
Lamp-light, effects of on colours, 154.
Le Blond, colour-chart of, 222.
Listing's experiments on spectrum, 26.
Luminosity of colour, 38.
Lustre, Dove's theory of, 280.

M

Magnus, Hugo, on development of sense for colour, 101.
Maxwell on colour-blindness, 103; fundamental colours, 120; intensity of fundamental colours in prismatic spectrum, 123; mixture of prismatic colours, 126.
Maxwell's colour-diagram, 224; reconstructed, 228.
Maxwell's disks, 109, 180.
Mayer, A. M., his history of Young's theory, 122.
Mayer, H., his arrangements for contrast, 260.
Mayer, T., colour-chart of, 222.
Medium with which pigments are mixed, 77.
Melloni opposed to Brewster's theory, 109.
Metals used in painting, 85.
Mlle, his mode of mixing colours, 139.
Milk, colours produced by, 58.
Mixture of blue and yellow light makes white, 112; of colours by binocular vision, 158; of coloured rays of prismatic spectrum, 126; of different-coloured light, 124; of pigments, theory and effects, 141; of prismatic colours, 111; of white and coloured light, 31, 82.
Monochromatic illumination, 102.
Monochromy, 308, 310.
Moonlight, colour of, 187.
Morton, H., thallene described by, 63.
Mountains, distant, colours of, 59.
Müller, J. J., on fundamental green, 121; green light in mixture produces a whitish tint, 119; mixture of prismatic colours, 126.

N

Newton's diagram for the colour-blind, 105; for lamp-light, 105.
Newton's experiment, 18.

Niece de Saint-Victor's experiments on photographing colours, 86.
Nitrate of potash, colours of, in polarized light, 47.
Nobert, diffraction grating of, 23.
Normal spectrum, 24, 25; appearance of, 122.

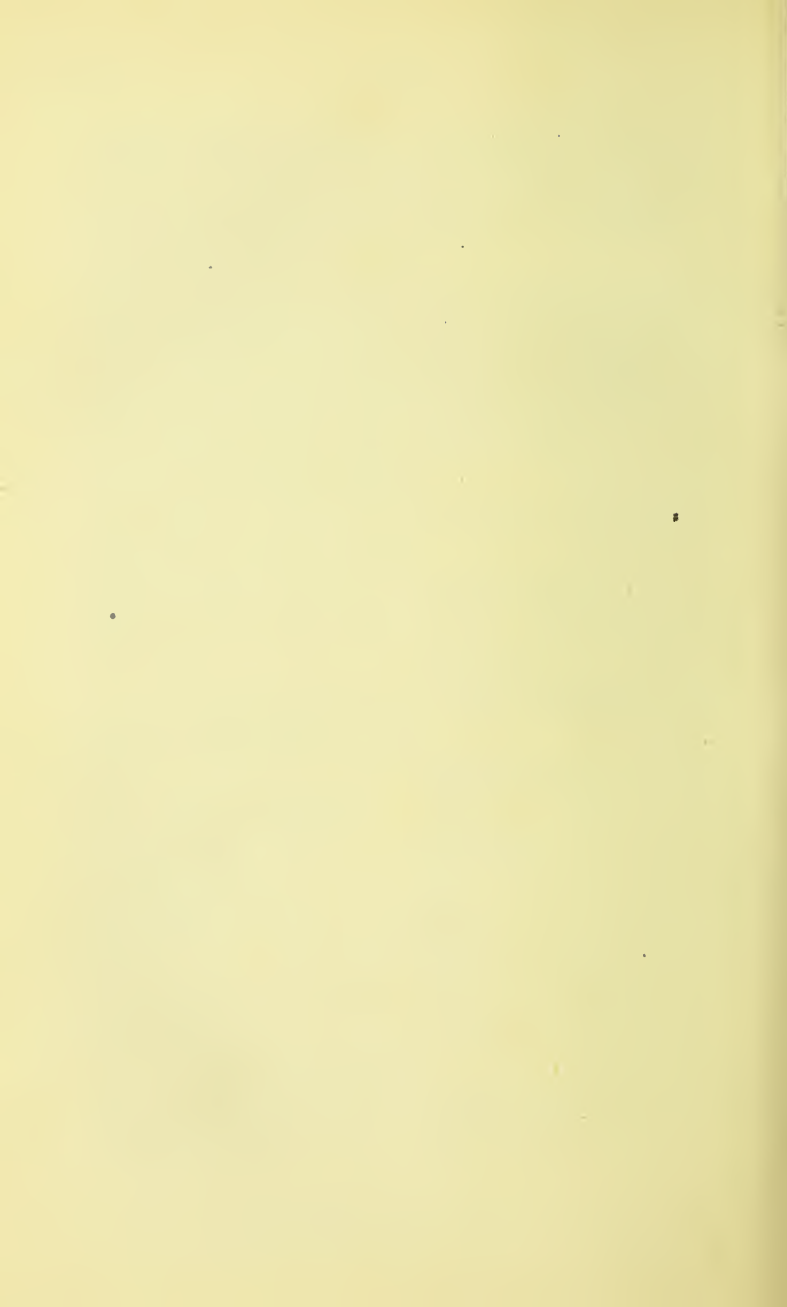
P

Painting, first practice, 318.
Painting and decoration divergent in aim, 306.
Painting and drawing, connecting links, 314.
Pettenger's process, 58.
Pfaff, experiment of on optic nerve with electricity, 9.
Phosphorescence, colours of, 64.
Photographs, instantaneous, peculiarity of, 207.
Photography, coloured, thus far a failure, 86.
Pierce, Charles, darkened red becomes more purplish, 185; fundamental green, 120; observation on colour-blindness, 96; photometric researches of, 41.
Pigments, action of light on, 88; appearance of affected by medium, 77; comparative luminosity of, 75; only three absolutely essential, 108; peculiar properties of influence their mixtures, 124; used for set of complementary disks, 179.
Pigments and stained glass compared, 73.
Pisko, F. J., on fluorescence, 63.
Plateau on duration of impression of coloured light on retina, 206; photometric experiment of, 205.
Platino-cyanide of barium used for fluorescence, 63.
Polarization, production of colour by, 43.
Polarizing apparatus, simple, 44.
Polychromy, 311.
Pouchet, observations of on colour of flounders, 101.
Preyer on colour-blindness, 97, 98.
Prismatic colours, mode of isolating, 19.
Prismatic spectrum, 18.
Purity of colour, 82.
Purkinje, relative luminosity of warm and cold colours dependent on the degree of illumination, 189.
Purple, how produced, 28.

R

Ragona Scina, apparatus of for contrast, 257.
Recomposition of white light, 28.
Red, sensation of, more intense when green and violet nerves are fatigued, 118.
Red light, action of on green nerves, 117.
Reflection, by polished surfaces, 11; by rough surfaces, 13; by water, 12; of coloured light by rough surfaces, 13; of light, 11.
Regnault on binocular perception of colour, 159.
Retina, 10.
Rood on binocular perception of colour, 159; colour-blindness produced by a shock to nervous system, 95; coloured spaces in spectrum, 22, 24; colours corresponding

- to certain wave-lengths, 26; comparison of effects of absorption and true mixture of light, 146; complementary colours by lamp-light, 173; complementary disks, 171; complement of red, 164; contrast-circles, 248; contrast-diagram, 250; estimation of the coloured spaces in the prismatic spectrum, 22; effects of gas-light on colour, 155; experiments on darkened pigments, 185, 188; experiments on pigments, 90; experiments on subjective colours, 94; grey has a tendency to blue, 191; luminosity of pigments, 35; method of comparing the luminosity of white and coloured surfaces, 84; mixtures of white and coloured light, 197; peculiarity of thin layers of pigments, 199; position of pigments in normal spectrum, 38; quantitative analysis of white light, 41; reflecting power of black disks, 184; reflection of coloured light from coloured surfaces, 149; size of coloured spaces in normal spectrum, 24; saturation-diagram, 233; time necessary for perception of colour, 102; wave-length corresponding to different colours, 26.
- Rutherford, observations of on blue of the spectrum, 121; prismatic colours change with their brightness, 181.
- Rutherford's automatic spectroscope, 37; diffraction grating, 23, 26; diffraction plates, 38.
- Ruskin on mixing colours, 140; on colour-gradation, 278.
- S
- Santonin, colour-blindness produced by, 95.
- Saturation-diagram, Rood's, 233.
- Schelske on colour-blind zone of normal eye, 97.
- Seebeck's observations on colour-blindness, 96.
- Seguin on colours of after-images, 93.
- Selenite, colours of in polarized light, 44.
- Shadow confused with reflection, 15.
- Shells, colours of, 51.
- Simler's erythroscopie, 83.
- Sky, colours of, 53.
- Small intervals, table of, 274.
- Smoke, opalescent colours of, 55.
- Solar spectrum, 18.
- Soap-bubbles, colours of, 49; falsely painted, *ib.*
- Spectra due to chloride of chromium, 72.
- Spectrometer, 21.
- Spectroscope, 20.
- Spectrum, diffraction, 23.
- Spectrum due to blue glass, 70; to green glass, *ib.*; to green leaves, 82; to red glass, 66; to small paper, 75; to stained glass varies with thickness of glass, 71.
- Spectrum, normal, 23; appearance of, 122; normal and prismatic compared, 23; of orange glass, 69; prismatic, 18.
- Stained glass, colour transmitted by, 16; and pigments compared, 73.
- Stokes, researches on fluorescence, 62.
- Successive contrast, 285-242.
- Sugar, colours of in polarized light, 46.
- Sulphide of barium, phosphorescence of, 64; of calcium, *ib.*; of strontium, *ib.*
- Sunset colours, normal series, 61.
- T
- Table of fixed lines in solar spectrum calculated to 1,000 parts, 22.
- Tables of colours in pairs, 286-291.
- Tait, colour-blindness produced by fever, 95.
- Tartaric acid, colours of in polarized light, 46.
- Thallene, fluorescence of, 63.
- Theories of colour, recent, 324.
- Thin films, colours of, 49.
- Translucency, 15.
- Transmission of light, 15.
- U
- Uranium glass, for production of fluorescence, 62.
- V
- Vegetation reflects red light, 83.
- Veins, colours of, 58.
- Velvet, colours of, 79.
- Vermilion, spectrum of, 75.
- Vierordt's photometric researches on the spectrum, 33.
- Vision, theory of, 11.
- Von Bezold, observations of on darkened prismatic spectrum, 183.
- W
- Warm and cold colours, proportion of in white light, 42.
- Wave-length made greater in fluorescence, 62.
- Wave-length and colour do not change equally, 27.
- Waves of light produce sensation of colour, 17.
- White lead on dark ground appears bluish, 56.
- White light reflected from surfaces of pigments, 76.
- Window-glass, old, colours of, 52.
- Woinow on colour-blind zone in normal eye, 99.
- Wollaston noticed fixed lines, 20.
- Wünsch on fundamental colours, 122.
- Y
- Yellow, complement of, 177; from a mixture of red and green light, not very brilliant, 116.
- Young, colour theory of, 113.



A LIST OF
C. KEGAN PAUL AND CO.'S
PUBLICATIONS.

I, Paternoster Square, London.

A LIST OF C. KEGAN PAUL AND CO.'S PUBLICATIONS.

ADAMS (F. O.), F.R.G.S.

The History of Japan. From the Earliest Period to the Present Time. New Edition, revised. 2 volumes. With Maps and Plans. Demy 8vo. Cloth, price 21s. each.

ADAMS (W. D.).

Lyrics of Love, from Shakespeare to Tennyson. Selected and arranged by. Fcap. 8vo. Cloth extra, gilt edges, price 3s. 6d.

Also, a Cheap Edition. Fcap. 8vo. Cloth, price 2s. 6d.

ADAMSON H. T.), B.D.

The Truth as it is in Jesus. Crown 8vo. Cloth, price 8s. 6d.

A. K. H. B.

From a Quiet Place. A New Volume of Sermons. Crown 8vo. Cloth, price 5s.

ALBERT (Mary).

Holland and her Heroes to the year 1585. An Adaptation from Motley's "Rise of the Dutch Republic." Small crown 8vo. Cloth, price, 4s. 6d.

ALLEN (Rev. R.), M.A.

Abraham; his Life, Times, and Travels, 3,800 years ago. Second Edition. With Map. Post 8vo. Cloth, price 6s.

ALLEN (Grant), B.A.

Physiological Æsthetics. Large post 8vo. 9s.

ALLIES (T. W.), M.A.

Per Crucem ad Lucem. The Result of a Life. 2 vols. Demy 8vo. Cloth, price 25s.

A Life's Decision. Crown 8vo. Cloth, price 7s. 6d.

AMATEUR.

A Few Lyrics. Small crown 8vo. Cloth, price 2s.

AMOS (Prof. Sheldon).

Science of Law. Fourth Edition. Crown 8vo. Cloth, price 5s.

Volume X. of The International Scientific Series.

ANDERSON (Col. R. P.).

Victories and Defeats. An Attempt to explain the Causes which have led to them. An Officer's Manual. Demy 8vo. Cloth, price 14s.

ANDERSON (R. C.), C.E.

Tables for Facilitating the Calculation of every Detail in connection with Earthen and Masonry Dams. Royal 8vo. Cloth, price £2 2s.

Antiope. A Tragedy. Large crown 8vo. Cloth, price 6s.

ARCHER (Thomas).

About my Father's Business. Work amidst the Sick, the Sad, and the Sorrowing. Crown 8vo. Cloth, price 2s. 6d.

Army of the North German Confederation.

A Brief Description of its Organization, of the Different Branches of the Service and their rôle in War, of its Mode of Fighting, &c. &c. Translated from the Corrected Edition, by permission of the Author, by Colonel Edward Newdigate. Demy 8vo. Cloth, price 5s.

ARNOLD (Arthur).

Social Politics. Demy 8vo. Cloth, price 14s.

Free Land. Crown 8vo. Cloth, price 6s.

AUBERTIN (J. J.).

Camoens' Lusiads. Portuguese Text, with Translation by. With Map and Portraits. 2 vols. Demy 8vo. Price 30s.

Aunt Mary's Bran Pie.

By the author of "St. Olave's." Illustrated. Cloth, price 3s. 6d.

AVIA.

The Odyssey of Homer Done into English Verse. Fcap. 4to. Cloth, price 15s.

BAGEHOT (Walter).

Physics and Politics; or, Thoughts on the Application of the Principles of "Natural Selection" and "Inheritance" to Political Society. Fifth Edition. Crown 8vo. Cloth, price 4s.

Volume II. of The International Scientific Series.

Some Articles on the Depreciation of Silver, and Topics connected with it. Demy 8vo. Price 5s.

The English Constitution. A New Edition, Revised and Corrected, with an Introductory Dissertation on Recent Changes and Events. Crown 8vo. Cloth, price 7s. 6d.

Lombard Street. A Description of the Money Market. Seventh Edition. Crown 8vo. Cloth, price 7s. 6d.

BAGOT (Alan).

Accidents in Mines: their Causes and Prevention. Crown 8vo. Cloth, price 6s.

BAIN (Alexander), LL.D.

Mind and Body: the Theories of their relation. Seventh Edition. Crown 8vo. Cloth, price 4s.

Volume IV. of The International Scientific Series.

Education as a Science. Crown 8vo. Third Edition. Cloth, price 5s.

Volume XXV. of The International Scientific Series.

BAKER (Sir Sherston, Bart.).

Halleck's International Law; or Rules Regulating the Intercourse of States in Peace and War. A New Edition, Revised, with Notes and Cases. 2 vols. Demy 8vo. Cloth, price 38s.

The Laws relating to Quarantine. Crown 8vo. Cloth, price 12s. 6d.

BALDWIN (Capt. J. H.), F.Z.S.

The Large and Small Game of Bengal and the North-Western Provinces of India. 4to. With numerous Illustrations. Second Edition. Cloth, price 21s.

BANKS (Mrs. G. L.).

God's Providence House. New Edition. Crown 8vo. Cloth, price 3s. 6d.

Ripples and Breakers. Poems. Square 8vo. Cloth, price 5s.

BARLEE (Ellen).

Locked Out: a Tale of the Strike. With a Frontispiece. Royal 16mo. Cloth, price 1s. 6d.

BARNES (William).

An Outline of English Speechcraft. Crown 8vo. Cloth, price 4s.

Poems of Rural Life, in the Dorset Dialect. New Edition, complete in 1 vol. Crown 8vo. Cloth, price 8s. 6d.

Outlines of Redecraft (Logic). With English Wording. Crown 8vo. Cloth, price 3s.

BARTLEY (George C. T.).

Domestic Economy: Thrift in Every Day Life. Taught in Dialogues suitable for Children of all ages. Small crown 8vo. Cloth, limp, 2s.

BASTIAN (H. Charlton), M.D.

The Brain as an Organ of Mind. With numerous Illustrations. Second Edition. Crown 8vo. Cloth, price 5s.

Volume XXIX. of the International Scientific Series.

BAUR (Ferdinand), Dr. Ph.

A Philological Introduction to Greek and Latin for Students. Translated and adapted from the German of. By C. KEGAN PAUL, M.A. Oxon., and the Rev. E. D. STONE, M.A., late Fellow of King's College, Cambridge, and Assistant Master at Eton. Second and revised edition. Crown 8vo. Cloth, price 6s.

BAYNES (Rev. Canon R. H.)

At the Communion Time. A Manual for Holy Communion. With a preface by the Right Rev. the Lord Bishop of Derry and Raphoe. Cloth, price 1s. 6d.

** Can also be had bound in French morocco, price 2s. 6d.; Persian morocco, price 3s.; Calf, or Turkey morocco, price 3s. 6d.

Home Songs for Quiet Hours. Fourth and cheaper Edition. Fcap. 8vo. Cloth, price 2s. 6d.

This may also be had handsomely bound in morocco with gilt edges.

BELLINGHAM (Henry), Barrister-at-Law.

Social Aspects of Catholicism and Protestantism in their Civil Bearing upon Nations. Translated and adapted from the French of M. le Baron de Haullerville. With a Preface by His Eminence Cardinal Manning. Crown 8vo. Cloth, price 6s.

BENNETT (Dr. W. C.).

Narrative Poems & Ballads. Fcap. 8vo. Sewed in Coloured Wrapper, price 1s.

Songs for Sailors. Dedicated by Special Request to H. R. H. the Duke of Edinburgh. With Steel Portrait and Illustrations. Crown 8vo. Cloth, price 3s. 6d.

An Edition in Illustrated Paper Covers, price 1s.

Songs of a Song Writer. Crown 8vo. Cloth, price 6s.

BERNSTEIN (Prof.).

The Five Senses of Man. With 91 Illustrations. Second Edition. Crown 8vo. Cloth, price 5s.

Volume XXI. of The International Scientific Series.

BETHAM - EDWARDS (Miss M.).

Kitty. With a Frontispiece. Crown 8vo. Cloth, price 6s.

BEVINGTON (L. S.).

Key Notes. Small crown 8vo. Cloth, price 5s.

BLASERNA (Prof. Pietro).

The Theory of Sound in its Relation to Music. With numerous Illustrations. Second Edition. Crown 8vo. Cloth, price 5s.

Volume XXII. of The International Scientific Series.

Blue Roses ; or, Helen Malinowska's Marriage. By the Author of "Véra." 2 vols. Fifth Edition. Cloth, gilt tops, 12s.

** Also a Cheaper Edition in 1 vol. With Frontispiece. Crown 8vo. Cloth, price 6s.

BLUME (Major W.).

The Operations of the German Armies in France, from Sedan to the end of the war of 1870-71. With Map. From the Journals of the Head-quarters Staff. Translated by the late E. M. Jones, Maj. 20th Foot, Prof. of Mil. Hist., Sandhurst. Demy 8vo. Cloth, price 9s.

BOGUSLAWSKI (Capt. A. von).

Tactical Deductions from the War of 1870-71. Translated by Colonel Sir Lumley Graham, Bart., late 18th (Royal Irish) Regiment. Third Edition, Revised and Corrected. Demy 8vo. Cloth, price 7s.

BONWICK (J.), F.R.G.S.

Egyptian Belief and Modern Thought. Large post 8vo. Cloth, price 10s. 6d.

Pyramid Facts and Fancies. Crown 8vo. Cloth, price 5s.

The Tasmanian Lily. With Frontispiece. Crown 8vo. Cloth, price 5s.

Mike Howe, the Bushranger of Van Diemen's Land. With Frontispiece. Crown 8vo. Cloth, price 5s.

BOWEN (H. C.), M. A.

English Grammar for Beginners. Fcap. 8vo. Cloth, price 1s.

Studies in English, for the use of Modern Schools. Small crown 8vo. Cloth, price 1s. 6d.

Simple English Poems. English Literature for Junior Classes. In Four Parts. Parts I. and II., price 6d. each, now ready.

BOWRING (Sir John).

Autobiographical Recollections. With Memoir by Lewin B. Bowring. Demy 8vo. Price 14s.

Brave Men's Footsteps.

By the Editor of "Men who have Risen." A Book of Example and Anecdote for Young People. With Four Illustrations by C. Doyle. Sixth Edition. Crown 8vo. Cloth, price 3s. 6d.

BRIALMONT (Col. A.).

Hasty Intrenchments. Translated by Lieut. Charles A. Empson, R. A. With Nine Plates. Demy 8vo. Cloth, price 6s.

BRODRICK (The Hon. G. C.).

Political Studies. Demy 8vo. Cloth, price 14s.

BROOKE (Rev. S. A.), M. A.

The Late Rev. F. W. Robertson, M.A., Life and Letters of. Edited by.

I. Uniform with the Sermons. 2 vols. With Steel Portrait. Price 7s. 6d.

II. Library Edition. 8vo. With Two Steel Portraits. Price 12s.

III. A Popular Edition, in 1 vol. 8vo. Price 6s.

Theology in the English Poets. — COWPER, COLERIDGE, WORDSWORTH, and BURNS. New and Cheaper Edition. Post 8vo. Cloth, price 5s.

Christ in Modern Life. Fourteenth and Cheaper Edition. Crown 8vo. Cloth, price 5s.

Sermons. First Series. Eleventh Edition. Crown 8vo. Cloth, price 6s.

BROOKE (Rev. S. A.), M.A.—
continued.

Sermons. Second Series. Third Edition. Crown 8vo. Cloth, price 7s.

The Fight of Faith. Sermons preached on various occasions. Third Edition. Crown 8vo. Cloth, price 7s. 6d.

Frederick Denison Maurice: The Life and Work of. A Memorial Sermon. Crown 8vo. Sewed, price 1s.

BROOKE (W. G.), M. A.

The Public Worship Regulation Act. With a Classified Statement of its Provisions, Notes, and Index. Third Edition, Revised and Corrected. Crown 8vo. Cloth, price 3s. 6d.

Six Privy Council Judgments—1850-1872. Annotated by. Third Edition. Crown 8vo. Cloth, price 9s.

BROUN (J. A.).

Magnetic Observations at Trevandrum and Augustia Malley. Vol. I. 4to. Cloth, price 63s.

The Report from above, separately sewed, price 21s.

BROWN (Rev. J. Baldwin).

The Higher Life. Its Reality, Experience, and Destiny. Fifth and Cheaper Edition. Crown 8vo. Cloth, price 5s.

Doctrine of Annihilation in the Light of the Gospel of Love. Five Discourses. Third Edition. Crown 8vo. Cloth, price 2s. 6d.

The Christian Policy of Life. A Book for Young Men of Business. New and Cheaper Edition. Crown 8vo. Cloth, price 3s. 6d.

BROWN (J. Croumbie), LL.D.

Reboisement in France; or, Records of the Replanting of the Alps, the Cevennes, and the Pyrenees with Trees, Herbage, and Bush. Demy 8vo. Cloth, price 12s. 6d.

The Hydrology of Southern Africa. Demy 8vo. Cloth, price 10s. 6d.

BRYANT (W. C.)

Poems. Red-line Edition. With 24 Illustrations and Portrait of the Author. Crown 8vo. Cloth extra, price 7s. 6d.

A Cheaper Edition, with Frontispiece. Small crown 8vo. Cloth, price 3s. 6d.

BURCKHARDT (Jacob).

The Civilization of the Period of the Renaissance in Italy. Authorized translation, by S. G. C. Middlemore. 2 vols. Demy 8vo. Cloth, price 24s.

BURTON (Mrs. Richard).

The Inner Life of Syria, Palestine, and the Holy Land. With Maps, Photographs, and Coloured Plates. 2 vols. Second Edition. Demy 8vo. Cloth, price 24s.

** Also a Cheaper Edition in one volume. Large post 8vo. Cloth, price 10s. 6d.

BURTON (Capt. Richard F.).

The Gold Mines of Midian and the Ruined Midianite Cities. A Fortnight's Tour in North Western Arabia. With numerous Illustrations. Second Edition. Demy 8vo. Cloth, price 18s.

The Land of Midian Revisited. With numerous illustrations on wood and by Chromolithography. 2 vols. Demy 8vo. Cloth, price 32s.

CALDERON.

Calderon's Dramas: The Wonder-Working Magician—Life is a Dream—The Purgatory of St. Patrick. Translated by Denis Florence MacCarthy. Post 8vo. Cloth, price 10s.

CANDLER (H.).

The Groundwork of Belief. Crown 8vo. Cloth, price 7s.

CARPENTER (W. B.), M.D.

The Principles of Mental Physiology. With their Applications to the Training and Discipline of the Mind, and the Study of its Morbid Conditions. Illustrated. Fifth Edition. 8vo. Cloth, price 12s.

CAVALRY OFFICER.

Notes on Cavalry Tactics, Organization, &c. With Diagrams. Demy 8vo. Cloth, price 12s.

CHAPMAN (Hon. Mrs. E. W.).

A Constant Heart. A Story. 2 vols. Cloth, gilt tops, price 12s.

CHEYNE (Rev. T. K.).

The Prophecies of Isaiah. Translated, with Critical Notes and Dissertations by. Two vols., demy 8vo. Cloth. Vol. I., price 12s. 6d.

Children's Toys, and some Elementary Lessons in General Knowledge which they teach. Illustrated. Crown 8vo. Cloth, price 5s.

CHRISTOPHERSON (The late Rev. Henry), M.A.

Sermons. With an Introduction by John Rae, LL.D., F.S.A. Second Series. Crown 8vo. Cloth, price 6s.

CLAYDEN (P. W.).

England under Lord Beaconsfield. The Political History of the Last Six Years, from the end of 1873 to the beginning of 1880. Second Edition. With Index, and Continuation to March, 1880. Demy 8vo. Cloth, price 16s.

CLERY (C.), Major.

Minor Tactics. With 26 Maps and Plans. Fourth and Revised Edition. Demy 8vo. Cloth, price 16s.

CLODD (Edward), F.R.A.S.

The Childhood of the World: a Simple Account of Man in Early Times. Sixth Edition. Crown 8vo. Cloth, price 3s.

A Special Edition for Schools. Price 1s.

The Childhood of Religions. Including a Simple Account of the Birth and Growth of Myths and Legends. Third Thousand. Crown 8vo. Cloth, price 5s.

A Special Edition for Schools. Price 1s. 6d.

Jesus of Nazareth. With a brief Sketch of Jewish History to the Time of His Birth. Small crown 8vo. Cloth, price 6s.

COLERIDGE (Sara).

Pretty Lessons in Verse for Good Children, with some Lessons in Latin, in Easy Rhyme. A New Edition. Illustrated. Fcap. 8vo. Cloth, price 3s. 6d.

Phantasmion. A Fairy Tale. With an Introductory Preface by the Right Hon. Lord Coleridge, of Ottery St. Mary. A New Edition. Illustrated. Crown 8vo. Cloth, price 7s. 6d.

Memoir and Letters of Sara Coleridge. Edited by her Daughter. Cheap Edition. With one Portrait. Cloth, price 7s. 6d.

COLLINS (Mortimer).

The Secret of Long Life. Small crown 8vo. Cloth, price 3s. 6d.

Inn of Strange Meetings, and other Poems. Crown 8vo. Cloth, price 5s.

CONWAY (Hugh).

A Life's Idylls. Small crown 8vo. Cloth, price 3s. 6d.

COOKE (M. C.), M.A., LL.D.

Fungi; their Nature, Influences, Uses, &c. Edited by the Rev. M. J. Berkeley, M.A., F.L.S. With Illustrations. Second Edition. Crown 8vo. Cloth, price 5s.

Volume XIV. of The International Scientific Series.

COOKE (Prof. J. P.)

The New Chemistry. With 31 Illustrations. Fifth Edition. Crown 8vo. Cloth, price 5s.

Volume IX. of The International Scientific Series.

Scientific Culture. Crown 8vo. Cloth, price 1s.

COOPER (H. J.).

The Art of Furnishing on Rational and Æsthetic Principles. New and Cheaper Edition. Fcap. 8vo. Cloth, price 1s. 6d.

COPPÉE (François).

L'Exilée. Done into English Verse with the sanction of the Author by I. O. L. Crown 8vo. Vellum, price 5s.

CORFIELD (Prof.), M.D.

Health. Crown 8vo. Cloth, price 6s.

CORY (William).

A Guide to Modern English History. Part I. MDCCCXV. —MDCCCXXX. Demy 8vo. Cloth, price 9s.

COURTNEY (W. L.).

The Metaphysics of John Stuart Mill. Crown 8vo. Cloth, price 5s. 6d.

COWAN (Rev. William).

Poems: Chiefly Sacred, including Translations from some Ancient Latin Hymns. Fcap. 8vo. Cloth, price 5s.

COX (Rev. Sir G. W.), Bart.

A History of Greece from the Earliest Period to the end of the Persian War. New Edition. 2 vols. Demy 8vo. Cloth, price 36s.

The Mythology of the Aryan Nations. New Edition. 2 vols. Demy 8vo. Cloth, price 28s.

A General History of Greece from the Earliest Period to the Death of Alexander the Great, with a sketch of the subsequent History to the present time. New Edition. Crown 8vo. Cloth, price 7s. 6d.

Tales of Ancient Greece. New Edition. Small crown 8vo. Cloth, price 6s.

School History of Greece. With Maps. New Edition. Fcap. 8vo. Cloth, price 3s. 6d.

The Great Persian War from the Histories of Herodotus. New Edition. Fcap. 8vo. Cloth, price 3s. 6d.

A Manual of Mythology in the form of Question and Answer. New Edition. Fcap. 8vo. Cloth, price 3s.

COX (Rev. Sir G. W.), Bart., M.A., and EUSTACE HINTON JONES.

Popular Romances of the Middle Ages. Second Edition in one volume. Crown 8vo. Cloth, price 6s.

COX (Rev. Samuel).

Salvator Mundi ; or, Is Christ the Saviour of all Men? Sixth Edition. Crown 8vo. Cloth, price 5s.

The Genesis of Evil, and other Sermons, mainly Expository. Second Edition. Crown 8vo. Cloth, price 6s.

CRAUFURD (A. H.).

Seeking for Light : Sermons. Crown 8vo. Cloth, price 5s.

CRAWFURD (Oswald).

Portugal, Old and New. With Illustrations and Maps. Demy 8vo. Cloth, price 16s.

CRESSWELL (Mrs. G.).

The King's Banner. Drama in Four Acts. Five Illustrations. 4to. Cloth, price 10s. 6d.

CROMPTON (Henry).

Industrial Conciliation. Fcap. 8vo. Cloth, price 2s. 6d.

CROZIER (John Beattie), M.B.

The Religion of the Future. Crown 8vo. Cloth, price 6s.

D'ANVERS (N. R.).

Parted. A Tale of Clouds and Sunshine. With 4 Illustrations. Extra Fcap. 8vo. Cloth, price 3s. 6d.

Little Minnie's Troubles.

An Every-day Chronicle. With Four Illustrations by W. H. Hughes. Fcap. Cloth, price 3s. 6d.

Pixie's Adventures ; or, the Tale of a Terrier. With 21 Illustrations. 16mo. Cloth, price 4s. 6d.

Nanny's Adventures ; or, the Tale of a Goat. With 12 Illustrations. 16mo. Cloth, price 4s. 6d.

DAVIDSON (Rev. Samuel), D.D., LL.D.

The New Testament, translated from the Latest Greek Text of Tischendorf. A New and thoroughly Revised Edition. Post 8vo. Cloth, price 10s. 6d.

DAVIDSON (Rev. Samuel), D.D., LL.D.—continued.

Canon of the Bible : Its Formation, History, and Fluctuations. Third Edition, revised and enlarged. Small crown 8vo. Cloth, price 5s.

DAVIES (G. Christopher).

Rambles and Adventures of Our School Field Club. With Four Illustrations. Crown 8vo. Cloth, price 5s.

DAVIES (Rev. J. L.), M.A.

Theology and Morality. Essays on Questions of Belief and Practice. Crown 8vo. Cloth, price 7s. 6d.

DAVIES (T. Hart.).

Catullus. Translated into English Verse. Crown 8vo. Cloth, price 6s.

DAWSON (George), M.A.

Prayers, with a Discourse on Prayer. Edited by his Wife. Fifth Edition. Crown 8vo. Price 6s.

Sermons on Disputed Points and Special Occasions. Edited by his Wife. Third Edition. Crown 8vo. Cloth, price 6s.

Sermons on Daily Life and Duty. Edited by his Wife. Second Edition. Crown 8vo. Cloth, price 6s.

DE L'HOSTE (Col. E. P.).

The Desert Pastor, Jean Jarousseau. Translated from the French of Eugène Pelletan. With a Frontispiece. New Edition. Fcap. 8vo. Cloth, price 3s. 6d.

DENNIS (J.).

English Sonnets. Collected and Arranged. Elegantly bound. Fcap. 8vo. Cloth, price 3s. 6d.

DE REDCLIFFE (Viscount Stratford), P.C., K.G., G.C.B.

Why am I a Christian? Fifth Edition. Crown 8vo. Cloth, price 3s.

DESPREZ (Philip S.).

Daniel and John ; or, the Apocalypse of the Old and that of the New Testament. Demy 8vo. Cloth, price 12s.

DE TOCQUEVILLE (A.).

Correspondence and Conversations of, with Nassau William Senior, from 1834 to 1859. Edited by M. C. M. Simpson. 2 vols. Post 8vo. Cloth, price 21s.

DE VERE (Aubrey).

Legends of the Saxon Saints. Small crown 8vo. Cloth, price 6s.

Alexander the Great. A Dramatic Poem. Small crown 8vo. Cloth, price 5s.

The Infant Bridal, and other Poems. A New and Enlarged Edition. Fcap. 8vo. Cloth, price 7s. 6d.

The Legends of St. Patrick, and other Poems. Small crown 8vo. Cloth, price 5s.

St. Thomas of Canterbury. A Dramatic Poem. Large fcap. 8vo. Cloth, price 5s.

Antar and Zara: an Eastern Romance. INISFAIL, and other Poems, Meditative and Lyrical. Fcap. 8vo. Price 6s.

The Fall of Rora, the Search after Proserpine, and other Poems, Meditative and Lyrical. Fcap. 8vo. Price 6s.

DOBSON (Austin).

Vignettes in Rhyme and Vers de Société. Third Edition. Fcap. 8vo. Cloth, price 5s.

Proverbs in Porcelain. By the Author of "Vignettes in Rhyme." Second Edition. Crown 8vo. 6s.

DOWDEN (Edward), LL.D.

Shakspeare: a Critical Study of his Mind and Art. Fifth Edition. Large post 8vo. Cloth, price 12s.

Studies in Literature, 1789-1877. Large post 8vo. Cloth, price 12s.

Poems. Second Edition. Fcap. 8vo. Cloth, price 5s.

DOWNTON (Rev. H.), M.A.

Hymns and Verses. Original and Translated. Small crown 8vo. Cloth, price 3s. 6d.

DRAPER (J. W.), M.D., LL.D.

History of the Conflict between Religion and Science. Fourteenth Edition. Crown 8vo. Cloth, price 5s.

Volume XIII. of The International Scientific Series.

DREW (Rev. G. S.), M.A.

Scripture Lands in connection with their History. Second Edition. 8vo. Cloth, price 10s. 6d.

Nazareth: Its Life and Lessons. Third Edition. Crown 8vo. Cloth, price 5s.

The Divine Kingdom on Earth as it is in Heaven. 8vo. Cloth, price 10s. 6d.

The Son of Man: His Life and Ministry. Crown 8vo. Cloth price 7s. 6d.

DREWRY (G. O.), M.D.

The Common-Sense Management of the Stomach. Fifth Edition. Fcap. 8vo. Cloth, price 2s. 6d.

DREWRY (G. O.), M.D., and BARTLETT (H. C.), Ph.D., F.C.S.

Cup and Platter: or, Notes on Food and its Effects. New and cheaper Edition. Small 8vo. Cloth, price 1s. 6d.

DRUMMOND (Miss).

Tripps Buildings. A Study from Life, with Frontispiece. Small crown 8vo. Cloth, price 3s. 6d.

DU MONCEL (Count).

The Telephone, the Microphone, and the Phonograph. With 74 Illustrations. Small crown 8vo. Cloth, price 5s.

DU VERNOIS (Col. von Verdy).

Studies in leading Troops. An authorized and accurate Translation by Lieutenant H. J. T. Hildyard, 71st Foot. Parts I. and II. Demy 8vo. Cloth, price 7s.

EDEN (Frederick).

The Nile without a Dragoman. Second Edition. Crown 8vo. Cloth, price 7s. 6d.

EDMONDS (Herbert).

Well Spent Lives : a Series of Modern Biographies. Crown 8vo. Price 5s.

Educational Code of the Prussian Nation, in its Present Form. In accordance with the Decisions of the Common Provincial Law, and with those of Recent Legislation. Crown 8vo. Cloth, price 2s. 6d.

EDWARDS (Rev. Basil).

Minor Chords ; or, Songs for the Suffering : a Volume of Verse. Fcap. 8vo. Cloth, price 3s. 6d. ; paper, price 2s. 6d.

ELLIOT (Lady Charlotte).

Medusa and other Poems. Crown 8vo. Cloth, price 6s.

ELLIOTT (Ebenezer), The Corn-Law Rhymers.

Poems. Edited by his Son, the Rev. Edwin Elliott, of St. John's, Antigua. 2 vols. Crown 8vo. Cloth, price 18s.

ELSDALE (Henry).

Studies in Tennyson's Idylls. Crown 8vo. Cloth, price 5s.

Epic of Hades (The).

By the author of "Songs of Two Worlds." Tenth and finally revised Edition. Fcap. 8vo. Cloth, price 7s. 6d. * * * Also an Illustrated Edition with seventeen full-page designs in photo-mezzotint by GEORGE R. CHAPMAN. 4to. Cloth, extra gilt leaves, price 25s.

EVANS (Mark).

The Gospel of Home Life. Crown 8vo. Cloth, price 4s. 6d.

The Story of our Father's Love, told to Children. Fourth and Cheaper Edition. With Four Illustrations. Fcap. 8vo. Cloth, price 1s. 6d.

A Book of Common Prayer and Worship for Household Use, compiled exclusively from the Holy Scriptures. New and Cheaper Edition. Fcap. 8vo. Cloth, price 1s.

EVANS (Mark)—continued.

The King's Story Book. In three parts. Fcap. 8vo. Cloth, price 1s. 6d. each. * * Part I., with four illustrations and Picture Map, now ready.

EX-CIVILIAN.

Life in the Mofussil ; or, Civilian Life in Lower Bengal. 2 vols. Large post 8vo. Price 14s.

FARQUHARSON (M.).

I. Elsie Dinsmore. Crown 8vo. Cloth, price 3s. 6d.

II. Elsie's Girlhood. Crown 8vo. Cloth, price 3s. 6d.

III. Elsie's Holidays at Roselands. Crown 8vo. Cloth, price 3s. 6d.

FIELD (Horace), B.A. Lond.

The Ultimate Triumph of Christianity. Small crown 8vo. Cloth, price 3s. 6d.

FINN (the late James), M.R.A.S.

Stirring Times ; or, Records from Jerusalem Consular Chronicles of 1853 to 1856. Edited and Compiled by his Widow. With a Preface by the Viscountess STRANGFORD. 2 vols. Demy 8vo. Price 30s.

Folkestone Ritual Case (The). The Argument, Proceedings, Judgment, and Report, revised by the several Counsel engaged. Demy 8vo. Cloth, price 25s.

FORMBY (Rev. Henry).

Ancient Rome and its Connection with the Christian Religion : an Outline of the History of the City from its First Foundation down to the Erection of the Chair of St. Peter, A.D. 42-47. With numerous Illustrations of Ancient Monuments, Sculpture, and Coinage, and of the Antiquities of the Christian Catacombs. Royal 4to. Cloth extra, price 50s. Roxburgh, half-morocco, price 52s. 6d.

FOWLE (Rev. Edmund).

Latin Primer Rules made Easy. Crown 8vo. Cloth, price 3s.

FOWLE (Rev. T. W.), M.A.

The Reconciliation of Religion and Science. Being Essays on Immortality, Inspiration, Miracles, and the Being of Christ. Demy 8vo. Cloth, price 10s. 6d.

The Divine Legation of Christ. Crown 8vo. Cloth, price 7s.

FRASER (Donald).

Exchange Tables of Sterling and Indian Rupee Currency, upon a new and extended system, embracing Values from One Farthing to One Hundred Thousand Pounds, and at Rates progressing, in Sixteenths of a Penny, from 1s. 9d. to 2s. 3d. per Rupee. Royal 8vo. Cloth, price 10s. 6d.

FRISWELL (J. Hain).

The Better Self. Essays for Home Life. Crown 8vo. Cloth, price 6s.

One of Two; or, A Left-Handed Bride. With a Frontispiece. Crown 8vo. Cloth, price 3s. 6d.

GARDNER (J.), M.D.

Longevity: The Means of Prolonging Life after Middle Age. Fourth Edition, Revised and Enlarged. Small crown 8vo. Cloth, price 4s.

GARRETT (E.).

By Still Waters. A Story for Quiet Hours. With Seven Illustrations. Crown 8vo. Cloth, price 6s.

GBLER (Karl Von).

Galileo Galilei and the Roman Curia, from Authentic Sources. Translated with the sanction of the Author, by Mrs. GEORGE STURGE. Demy 8vo. Cloth, price 12s.

GEDDES (James).

History of the Administration of John de Witt, Grand Pensionary of Holland. Vol. I. 1623-1654. Demy 8vo., with Portrait. Cloth, price 15s.

G. H. T.

Verses, mostly written in India. Crown 8vo. Cloth, price 6s.

GILBERT (Mrs.).

Autobiography and other Memorials. Edited by Josiah Gilbert. Third Edition. With Portrait and several Wood Engravings. Crown 8vo. Cloth, price 7s. 6d.

GILL (Rev. W. W.), B.A.

Myths and Songs from the South Pacific. With a Preface by F. Max Müller, M.A., Professor of Comparative Philology at Oxford. Post 8vo. Cloth, price 9s.

Ginevra and The Duke of

Guise. Two Tragedies. Crown 8vo. Cloth, price 6s.

GLOVER (F.), M.A.

Exempla Latina. A First Construing Book with Short Notes, Lexicon, and an Introduction to the Analysis of Sentences. Fcap. 8vo. Cloth, price 2s.

GODWIN (William).

William Godwin: His Friends and Contemporaries. With Portraits and Facsimiles of the handwriting of Godwin and his Wife. By C. Kegan Paul. 2 vols. Demy 8vo. Cloth, price 28s.

The Genius of Christianity

Unveiled. Being Essays never before published. Edited, with a Preface, by C. Kegan Paul. Crown 8vo. Cloth, price 7s. 6d.

GOETZE (Capt. A. von).

Operations of the German Engineers during the War of 1870-1871. Published by Authority, and in accordance with Official Documents. Translated from the German by Colonel G. Graham, V.C., C.B., R.E. With 6 large Maps. Demy 8vo. Cloth, price 21s.

GOLDSMID (Sir Francis Henry).

Memoir of. With Portrait. Crown 8vo. Cloth, price 5s.

GOODENOUGH (Commodore J. G.), R.N., C.B., C.M.G.

Memoir of, with Extracts from his Letters and Journals. Edited by his Widow. With Steel Engraved Portrait. Square 8vo. Cloth, 5s.

* * * Also a Library Edition with Maps, Woodcuts, and Steel Engraved Portrait. Square post 8vo. Cloth, price 14s.

GOSSE (Edmund W.).

Studies in the Literature of Northern Europe. With a Frontispiece designed and etched by Alma Tadema. Large post 8vo. Cloth, price 12s.

New Poems. Crown 8vo. Cloth, price 7s. 6d.

GOULD (Rev. S. Baring), M.A.
Germany, Present and Past. 2 Vols. Demy 8vo. Cloth, price 21s.

The Vicar of Morwenstow: a Memoir of the Rev. R. S. Hawker. With Portrait. Third Edition, revised. Square post 8vo. Cloth, 10s. 6d.

GREY (John), of Dilston.
John Grey (of Dilston): Memoirs. By Josephine E. Butler. New and Revised Edition. Crown 8vo. Cloth, price 3s. 6d.

GRIMLEY (Rev. H. N.), M.A.
Tremadoc Sermons, chiefly on the SPIRITUAL BODY, the UNSEEN WORLD, and the DIVINE HUMANITY. Second Edition. Crown 8vo. Cloth, price 6s.

GRÜNER (M. L.).
Studies of Blast Furnace Phenomena. Translated by L. D. B. Gordon, F.R.S.E., F.G.S. Demy 8vo. Cloth, price 7s. 6d.

GURNEY (Rev. Archer).
Words of Faith and Cheer. A Mission of Instruction and Suggestion. Crown 8vo. Cloth, price 6s.

Gwen: A Drama in Monologue. By the Author of the "Epic of Hades." Second Edition. Fcap. 8vo. Cloth, price 5s.

HAECKEL (Prof. Ernst).
The History of Creation. Translation revised by Professor E. Ray Lankester, M.A., F.R.S. With Coloured Plates and Genealogical Trees of the various groups of both plants and animals. 2 vols. Second Edition. Post 8vo. Cloth, price 32s.
The History of the Evolution of Man. With numerous Illustrations. 2 vols. Large post 8vo. Cloth, price 32s.

HAECKEL (Prof. Ernst.)—*continued.*

Freedom in Science and Teaching. From the German of Ernst Haeckel, with a Prefatory Note by T. H. Huxley, F.R.S. Crown 8vo. Cloth, price 5s.

HAKE (A. Egmont).
Paris Originals, with twenty etchings, by Léon Richeton. Large post 8vo. Cloth, price 14s.

Halleck's International Law; or, Rules Regulating the Intercourse of States in Peace and War. A New Edition, revised, with Notes and Cases. By Sir Sherston Baker, Bart. 2 vols. Demy 8vo. Cloth, price 38s.

HARDY (Thomas).
A Pair of Blue Eyes. New Edition. With Frontispiece. Crown 8vo. Cloth, price 6s.

The Return of the Native. New Edition. With Frontispiece. Crown 8vo. Cloth, price 6s.

HARRISON (Lieut.-Col. R.).
The Officer's Memorandum Book for Peace and War. Second Edition. Oblong 32mo. roan, elastic band and pencil, price 3s. 6d.; russia, 5s.

HARTINGTON (The Right Hon. the Marquis of), M.P.
Election Speeches in 1879 and 1880. With Address to the Electors of North-East Lancashire. Crown 8vo. Cloth, price 3s. 6d.

Haweis (Rev. H. R.), M.A.
Arrows in the Air. Crown 8vo. Second Edition. Cloth, price 6s.
Current Coin. Materialism—The Devil—Crime—Drunkennes—Pauperism—Emotion—Recreation—The Sabbath. Third Edition. Crown 8vo. Cloth, price 6s.

Speech in Season. Fourth Edition. Crown 8vo. Cloth, price 9s.
Thoughts for the Times. Eleventh Edition. Crown 8vo. Cloth, price 7s. 6d.

Unsectarian Family Prayers. New and Cheaper Edition. Fcap. 8vo. Cloth, price 1s. 6d.

HAWKER (Robert Stephen).

The Poetical Works of.

Now first collected and arranged with a prefatory notice by J. G. Godwin. With Portrait. Crown 8vo. Cloth, price 12s.

HAWTREY (Edward M.).

Corydalis. A Story of the Sicilian Expedition. Small crown 8vo. Cloth, price 3s. 6d.

HEIDENHAIN (Rudolf), M.D.

Animal Magnetism. Physiological Observations. Translated from the Fourth German Edition, by L. C. Wooldridge. With a Preface by G. R. Romanes, F.R.S. Crown 8vo. Cloth, price 2s. 6d.

HELLWALD (Baron F. von).

The Russians in Central Asia. A Critical Examination, down to the present time, of the Geography and History of Central Asia. Translated by Lieut.-Col. Theodore Wirgman, LL.B. Large post 8vo. With Map. Cloth, price 12s.

HELVIG (Major H.).

The Operations of the Bavarian Army Corps. Translated by Captain G. S. Schwabe. With Five large Maps. In 2 vols. Demy 8vo. Cloth, price 24s.

Tactical Examples: Vol. I. The Battalion, price 15s. **Vol. II.** The Regiment and Brigade, price 10s. 6d. Translated from the German by Col. Sir Lumley Graham. With numerous Diagrams. Demy 8vo. Cloth.

HERFORD (Brooke).

The Story of Religion in England. A Book for Young Folk. Crown 8vo. Cloth, price 5s.

HINTON (James).

Life and Letters of. Edited by Ellice Hopkins, with an Introduction by Sir W. W. Gull, Bart., and Portrait engraved on Steel by C. H. Jeens. Second Edition. Crown 8vo. Cloth, 8s. 6d.

Chapters on the Art of Thinking, and other Essays. With an Introduction by Shadworth Hodgson. Edited by C. H. Hinton. Crown 8vo. Cloth, price 8s. 6d.

HINTON (James)—*continued.*

The Place of the Physician.

To which is added **ESSAYS ON THE LAW OF HUMAN LIFE, AND ON THE RELATION BETWEEN ORGANIC AND INORGANIC WORLDS.** Second Edition. Crown 8vo. Cloth, price 3s. 6d.

Physiology for Practical Use. By various Writers. With 50 Illustrations. 2 vols. Second Edition. Crown 8vo. Cloth, price 12s. 6d.

An Atlas of Diseases of the Membrana Tympani. With Descriptive Text. Post 8vo. Price £6 6s.

The Questions of Aural Surgery. With Illustrations. 2 vols. Post 8vo. Cloth, price 12s. 6d.

The Mystery of Pain. New Edition. Fcap. 8vo. Cloth limp, 1s.

HOCKLEY (W. B.).

Tales of the Zenana; or, A Nuwab's Leisure Hours. By the Author of "Pandurang Hari." With a Preface by Lord Stanley of Alderley. 2 vols. Crown 8vo. Cloth, price 21s.

Pandurang Hari; or, Memoirs of a Hindoo. A Tale of Mahratta Life sixty years ago. With a Preface by Sir H. Bartle E. Frere, G.C.S.I., &c. New and Cheaper Edition. Crown 8vo. Cloth, price 6s.

HOFFBAUER (Capt.).

The German Artillery in the Battles near Metz. Based on the official reports of the German Artillery. Translated by Capt. E. O. Hollist. With Map and Plans. Demy 8vo. Cloth, price 21s.

HOLMES (E. G. A.).

Poems. First and Second Series. Fcap. 8vo. Cloth, price 5s. each.

HOLROYD (Major W. R. M.).

Tas-hil ul Kālām; or, Hindustani made Easy. Crown 8vo. Cloth, price 5s.

HOOPER (Mary).

Little Dinners: How to Serve them with Elegance and Economy. Thirteenth Edition. Crown 8vo. Cloth, price 5s.

HOOPER (Mary)—*continued.*

Cookery for Invalids, Persons of Delicate Digestion, and Children. Crown 8vo. Cloth, price 3s. 6d.

Every-Day Meals. Being Economical and Wholesome Recipes for Breakfast, Luncheon, and Supper. Second Edition. Crown 8vo. Cloth, price 5s.

HOOPER (Mrs. G.).

The House of Raby. With a Frontispiece. Crown 8vo. Cloth, price 3s. 6d.

HOPKINS (Ellice).

Life and Letters of James Hinton, with an Introduction by Sir W. W. Gull, Bart., and Portrait engraved on Steel by C. H. Jeens. Second Edition. Crown 8vo. Cloth price 8s. 6d.

HOPKINS (M.).

The Port of Refuge; or, Counsel and Aid to Shipmasters in Difficulty, Doubt, or Distress. Crown 8vo. Second and Revised Edition. Cloth, price 6s.

HORNER (The Misses).

Walks in Florence. A New and thoroughly Revised Edition. 2 vols. Crown 8vo. Cloth limp. With Illustrations.

Vol. I.—Churches, Streets, and Palaces. 10s. 6d. Vol. II.—Public Galleries and Museums. 5s.

HULL (Edmund C. P.).

The European in India. With a MEDICAL GUIDE FOR ANGLO-INDIANS. By R. R. S. Mair, M.D., F.R.C.S.E. Third Edition, Revised and Corrected. Post 8vo. Cloth, price 6s.

HUTCHISON (Lieut.-Col. F. J.), and Capt. G. H. MACGREGOR.

Military Sketching and Reconnaissance. With Fifteen Plates. Small 8vo. Cloth, price 6s.

The first Volume of Military Handbooks for Regimental Officers. Edited by Lieut.-Col. C. B. BRACKENBURY, R.A., A.A.G.

HUTTON (Arthur), M.A.

The Anglican Ministry. Its Nature and Value in relation to the Catholic Priesthood. With a Preface by his Eminence Cardinal Newman. Demy 8vo. Cloth, price 14s.

HUXLEY (Prof.)

The Crayfish: An Introduction to the Study of Zoology. With Eighty-two Illustrations. Crown 8vo. Cloth, price 5s.
Volume XXVIII. of the International Scientific Series.

INCHBOLD (J. W.).

Annus Amoris. Sonnets. Fcap. 8vo. Cloth, price 4s. 6d.

INGELOW (Jean).

Off the Skelligs. A Novel. With Frontispiece. Second Edition. Crown 8vo. Cloth, price 6s.

The Little Wonder-horn. A Second Series of "Stories Told to a Child." With Fifteen Illustrations. Small 8vo. Cloth, price 2s. 6d.

Indian Bishoprics. By an Indian Churchman. Demy 8vo. 6d.

International Scientific Series (The).

I. Forms of Water: A Familiar Exposition of the Origin and Phenomena of Glaciers. By J. Tyndall, LL.D., F.R.S. With 25 Illustrations. Seventh Edition. Crown 8vo. Cloth, price 5s.

II. Physics and Politics; or, Thoughts on the Application of the Principles of "Natural Selection" and "Inheritance" to Political Society. By Walter Bagehot. Fifth Edition. Crown 8vo. Cloth, price 4s.

III. Foods. By Edward Smith, M.D., &c. With numerous Illustrations. Sixth Edition. Crown 8vo. Cloth, price 5s.

IV. Mind and Body: The Theories of their Relation. By Alexander Bain, LL.D. With Four Illustrations. Seventh Edition. Crown 8vo. Cloth, price 4s.

V. The Study of Sociology. By Herbert Spencer. Eighth Edition. Crown 8vo. Cloth, price 5s.

International Scientific Series (The)—continued.

VI. On the Conservation of Energy. By Balfour Stewart, LL.D., &c. With 14 Illustrations. Fifth Edition. Crown 8vo. Cloth, price 5s.

VII. Animal Locomotion; or, Walking, Swimming, and Flying. By J. E. Pettigrew, M.D., &c. With 130 Illustrations. Second Edition. Crown 8vo. Cloth, price 5s.

VIII. Responsibility in Mental Disease. By Henry Maudsley, M.D. Third Edition. Crown 8vo. Cloth, price 5s.

IX. The New Chemistry. By Professor J. P. Cooke. With 31 Illustrations. Fifth Edition. Crown 8vo. Cloth, price 5s.

X. The Science of Law. By Prof. Sheldon Amos. Fourth Edition. Crown 8vo. Cloth, price 5s.

XI. Animal Mechanism. A Treatise on Terrestrial and Aerial Locomotion. By Prof. E. J. Marey. With 117 Illustrations. Second Edition. Crown 8vo. Cloth, price 5s.

XII. The Doctrine of Descent and Darwinism. By Prof. Osca Schmidt. With 26 Illustrations. Third Edition. Crown 8vo. Cloth, price 5s.

XIII. The History of the Conflict between Religion and Science. By J. W. Draper, M.D., LL.D. Fourteenth Edition. Crown 8vo. Cloth, price 5s.

XIV. Fungi; their Nature, Influences, Uses, &c. By M. C. Cooke, LL.D. Edited by the Rev. M. J. Berkeley, F.L.S. With numerous Illustrations. Second Edition. Crown 8vo. Cloth, price 5s.

XV. The Chemical Effects of Light and Photography. By Dr. Hermann Vogel. With 100 Illustrations. Third and Revised Edition. Crown 8vo. Cloth, price 5s.

XVI. The Life and Growth of Language. By Prof. William Dwight Whitney. Second Edition. Crown 8vo. Cloth, price 5s.

XVII. Money and the Mechanism of Exchange. By W. Stanley Jevons, F.R.S. Fourth Edition. Crown 8vo. Cloth, price 5s.

International Scientific Series (The)—continued.

XVIII. The Nature of Light: With a General Account of Physical Optics. By Dr. Eugene Lommel. With 188 Illustrations and a table of Spectra in Chromo-lithography. Third Edition. Crown 8vo. Cloth, price 5s.

XIX. Animal Parasites and Messmates. By M. Van Beneden. With 83 Illustrations. Second Edition. Crown 8vo. Cloth, price 5s.

XX. Fermentation. By Prof. Schützenberger. With 28 Illustrations. Second Edition. Crown 8vo. Cloth, price 5s.

XXI. The Five Senses of Man. By Prof. Bernstein. With 91 Illustrations. Second Edition. Crown 8vo. Cloth, price 5s.

XXII. The Theory of Sound in its Relation to Music. By Prof. Pietro Blaserna. With numerous Illustrations. Second Edition. Crown 8vo. Cloth, price 5s.

XXIII. Studies in Spectrum Analysis. By J. Norman Lockyer, F.R.S. With six photographic Illustrations of Spectra, and numerous engravings on wood. Crown 8vo. Second Edition. Cloth, price 6s. 6d.

XXIV. A History of the Growth of the Steam Engine. By Prof. R. H. Thurston. With numerous Illustrations. Second Edition. Crown 8vo. Cloth, price 6s. 6d.

XXV. Education as a Science. By Alexander Bain, LL.D. Third Edition. Crown 8vo. Cloth, price 5s.

XXVI. The Human Species. By Prof. A. de Quatrefages. Second Edition. Crown 8vo. Cloth, price 5s.

XXVII. Modern Chromatics. With Applications to Art and Industry, by Ogden N. Rood. With 130 original Illustrations. Crown 8vo. Cloth, price 5s.

XXVIII. The Crayfish: an Introduction to the Study of Zoology. By Prof. T. H. Huxley. With eighty-two Illustrations. Crown 8vo. Cloth, price 5s.

XXIX. The Brain as an Organ of Mind. By H. Charlton Bastian, M.D. With numerous Illustrations. Second Edition. Crown 8vo. Cloth, price 5s.

International Scientific Series (The)—*continued.*

Forthcoming Volumes.

Prof. W. KINGDON CLIFFORD, M.A.
The First Principles of the Exact Sciences explained to the Non-mathematical.

W. B. CARPENTER, LL.D., F.R.S.
The Physical Geography of the Sea.

Sir JOHN LUBBOCK, Bart., F.R.S.
On Ants and Bees.

Prof. W. T. THISELTON DYER, B.A., B.Sc.
Form and Habit in Flowering Plants.

Prof. MICHAEL FOSTER, M.D.
Protoplasm and the Cell Theory.

Prof. A. C. RAMSAY, LL.D., F.R.S.
Earth Sculpture: Hills, Valleys, Mountains, Plains, Rivers, Lakes; how they were Produced, and how they have been Destroyed.

P. BERT (Professor of Physiology, Paris).
Forms of Life and other Cosmical Conditions.

The Rev. A SECCHI, D.J., late Director of the Observatory at Rome.
The Stars.

Prof. J. ROSENTHAL, of the University of Erlangen.
General Physiology of Muscles and Nerves.

FRANCIS GALTON, F.R.S.
Psychometry.

J. W. JUDD, F.R.S.
The Laws of Volcanic Action.

Prof. F. N. BALFOUR.
The Embryonic Phases of Animal Life.

J. LUVS, Physician to the Hospice de la Salpêtrière.
The Brain and its Functions. With Illustrations.

Dr. CARL SEMPER.
Animals and their Conditions of Existence.

Prof. WURTZ.
Atoms and the Atomic Theory.

GEORGE J. ROMANES, F.L.S.
Animal Intelligence.

ALFRED W. BENNETT.
A Handbook of Cryptogamic Botany.

JENKINS (Rev. Canon).

The Girdle Legend of Prato.
Small crown 8vo. Cloth, price 2s.

JENKINS (E.) and RAYMOND (J.), Esqs.

A Legal Handbook for Architects, Builders, and Building Owners. Second Edition Revised. Crown 8vo. Cloth, price 6s.

JENKINS (Rev. R. C.), M.A.

The Privilege of Peter and the Claims of the Roman Church confronted with the Scriptures, the Councils, and the Testimony of the Popes themselves. Fcap. 8vo. Cloth, price 3s. 6d.

JENNINGS (Mrs. Vaughan).

Rahel: Her Life and Letters. With a Portrait from the Painting by Daffinger. Square post 8vo. Cloth, price 7s. 6d.

Jeroveam's Wife and other Poems. Fcap. 8vo. Cloth, price 3s. 6d.

JEVONS (W. Stanley), M.A., F.R.S.

Money and the Mechanism of Exchange. Fourth Edition. Crown 8vo. Cloth, price 5s.

Volume XVII. of The International Scientific Series.

JOEL (L.).

A Consul's Manual and Shipowner's and Shipmaster's Practical Guide in their Transactions Abroad. With Definitions of Nautical, Mercantile, and Legal Terms; a Glossary of Mercantile Terms in English, French, German, Italian, and Spanish. Tables of the Money, Weights, and Measures of the Principal Commercial Nations and their Equivalents in British Standards; and Forms of Consular and Notarial Acts. Demy 8vo. Cloth, price 12s.

JOHNSTONE (C. F.), M.A.

Historical Abstracts. Being Outlines of the History of some of the less-known States of Europe. Crown 8vo. Cloth, price 7s. 6d.

JONES (Lucy).

Puddings and Sweets. Being Three Hundred and Sixty-Five Receipts approved by Experience. Crown 8vo., price 2s. 6d.

JOYCE (P. W.), LL.D., &c.
Old Celtic Romances.
 Translated from the Gaelic by.
 Crown 8vo. Cloth, price 7s. 6d.

KAUFMANN (Rev. M.), B.A.
Utopias; or, Schemes of Social Improvement, from Sir Thomas More to Karl Marx. Crown 8vo. Cloth, price 5s.

Socialism: Its Nature, its Dangers, and its Remedies considered. Crown 8vo. Cloth, price 7s. 6d.

KAY (Joseph), M.A., Q.C.
Free Trade in Land.
 Edited by his Widow. With Preface by the Right Hon. John Bright, M. P. Third Edition. Crown 8vo. Cloth, price 5s.

KENT (Carolo).
Carona Catholica ad Petri successoris Pedes Oblata. De Summi Pontificis Leonis XIII. Assumptione Epigramma. In Quinquaginta Linguis. Fcap. 4to. Cloth, price 15s.

KER (David).
The Boy Slave in Bokhara.
 A Tale of Central Asia. With Illustrations. Crown 8vo. Cloth, price 3s. 6d.

The Wild Horseman of the Pampas. Illustrated. Crown 8vo. Cloth, price 3s. 6d.

KERNER (Dr. A.), Professor of Botany in the University of Innsbruck.

Flowers and their Unbidden Guests. Translation edited by W. OGLE, M.A., M.D., and a prefatory letter by C. Darwin, F.R.S. With Illustrations. Sq. 8vo. Cloth, price 9s.

KIDD (Joseph), M.D.
The Laws of Therapeutics, or, the Science and Art of Medicine. Crown 8vo. Cloth, price 6s.

KINAHAN (G. Henry), M.R.I.A., &c., of her Majesty's Geological Survey.

Manual of the Geology of Ireland. With 8 Plates, 26 Woodcuts, and a Map of Ireland, geologically coloured. Square 8vo. Cloth, price 15s.

KING (Mrs. Hamilton).
The Disciples. A Poem. Third Edition, with some Notes. Crown 8vo. Cloth, price 7s. 6d.
Aspromonte, and other Poems. Second Edition. Fcap. 8vo. Cloth, price 4s. 6d.

KING (Edward).
Echoes from the Orient.
 With Miscellaneous Poems. Small crown 8vo. Cloth, price 3s. 6d.

KINGSLEY (Charles), M.A.
Letters and Memories of his Life. Edited by his Wife. With 2 Steel engraved Portraits and numerous Illustrations on Wood, and a Facsimile of his Handwriting. Thirteenth Edition. 2 vols. Demy 8vo. Cloth, price 36s.

* * * Also a Cabinet Edition in 2 vols. Crown 8vo. Cloth, price 12s.
All Saints' Day and other Sermons. Second Edition. Crown 8vo. Cloth, 7s. 6d.

True Words for Brave Men: a Book for Soldiers' and Sailors' Libraries. Fifth Edition. Crown 8vo. Cloth, price 2s. 6d.

KNIGHT (Professor W.).
Studies in Philosophy and Literature. Large post 8vo. Cloth, price 7s. 6d.

LACORDAIRE (Rev. Père).
Life: Conferences delivered at Toulouse. A New and Cheaper Edition. Crown 8vo. Cloth, price 3s. 6d.

LAIRD-CLOWES (W.).
Love's Rebellion: a Poem. Fcap. 8vo. Cloth, price 3s. 6d.

LAMONT (Martha MacDonald).
The Gladiator: A Life under the Roman Empire in the beginning of the Third Century. With four Illustrations by H. M. Paget. Extra fcap. 8vo. Cloth, price 3s. 6d.

LANG (A.).
XXII Ballades in Blue China. Elzevir. 8vo. Parchment, price 3s. 6d.

LAYMANN (Capt.).
The Frontal Attack of Infantry. Translated by Colonel Edward Newdigate. Crown 8vo. Cloth, price 2s. 6d.

LEANDER (Richard).

Fantastic Stories. Translated from the German by Paulina B. Granville. With Eight full-page Illustrations by M. E. Fraser-Tytler. Crown 8vo. Cloth, price 5s.

LEE (Rev. F. G.), D.C.L.

The Other World; or, Glimpses of the Supernatural. 2 vols. A New Edition. Crown 8vo. Cloth, price 15s.

LEE (Holme).

Her Title of Honour. A Book for Girls. New Edition. With a Frontispiece. Crown 8vo. Cloth, price 5s.

LEWIS (Edward Dillon).

A Draft Code of Criminal Law and Procedure. Demy 8vo. Cloth, price 21s.

LEWIS (Mary A.).

A Rat with Three Tales. With Four Illustrations by Catherine F. Frere. Crown 8vo. Cloth, price 5s.

LINDSAY (W. Lauder), M.D., &c.

Mind in the Lower Animals in Health and Disease. 2 vols. Demy 8vo. Cloth, price 32s.

LLOYD (Francis) and Charles Tebbitt.

Extension of Empire Weakness? Deficits Ruin? With a Practical Scheme for the Reconstruction of Asiatic Turkey. Small crown 8vo. Cloth, price 3s. 6d.

LOCKER (F.).

London Lyrics. A New and Revised Edition, with Additions and a Portrait of the Author. Crown 8vo. Cloth, elegant, price 6s.

Also, a Cheaper Edition. Fcap 8vo. Cloth, price 2s. 6d.

LOCKYER (J. Norman), F.R.S.

Studies in Spectrum Analysis; with six photographic illustrations of Spectra, and numerous engravings on wood. Second Edition. Crown 8vo. Cloth, price 6s. 6d.

Vol. XXIII. of The International Scientific Series.

LOMMEL (Dr. E.).

The Nature of Light: With a General Account of Physical Optics. Second Edition. With 188 Illustrations and a Table of Spectra in Chromo-lithography. Third Edition. Crown 8vo. Cloth, price 5s.

Volume XVIII. of The International Scientific Series.

LONSDALE (Margaret).

Sister Dora. A Biography, with Portrait engraved on steel by C. H. Jeens, and one illustration. Twelfth edition. Crown 8vo. Cloth, price 6s.

LORIMER (Peter), D.D.

John Knox and the Church of England: His Work in her Pulpit, and his Influence upon her Liturgy, Articles, and Parties. Demy 8vo. Cloth, price 12s.

John Wiclif and his English Precursors, by Gerhard Victor Lechler. Translated from the German, with additional Notes. 2 vols. Demy 8vo. Cloth, price 21s.

Love's Gamut and other Poems. Small crown 8vo. Cloth, price 3s. 6d.

LOWNDES (Henry).

Poems and Translations. Crown 8vo. Cloth, price 6s.

MAC CLINTOCK (L.).

Sir Spangle and the Dingy Hen. Illustrated. Square crown 8vo., price 2s. 6d.

MACDONALD (G.).

Malcolm. With Portrait of the Author engraved on Steel. Fourth Edition. Crown 8vo. Price 6s.

The Marquis of Lossie. Second Edition. Crown 8vo. Cloth, price 6s.

St. George and St. Michael. Second Edition. Crown 8vo. Cloth, 6s.

MACKENNA (S. J.).

Plucky Fellows. A Book for Boys. With Six Illustrations. Fourth Edition. Crown 8vo. Cloth, price 3s. 6d.

At School with an Old Dragoon. With Six Illustrations. Second Edition. Crown 8vo. Cloth, price 5s.

MACLACHLAN (Mrs.).

Notes and Extracts on Everlasting Punishment and Eternal Life, according to Literal Interpretation. Small crown 8vo. Cloth, price 3s. 6d.

MACNAUGHT (Rev. John).

Cœna Domini: An Essay on the Lord's Supper, its Primitive Institution, Apostolic Uses, and Subsequent History. Demy 8vo. Cloth, price 14s.

MAGNUSSON (Eirikr), M.A., and PALMER (E.H.), M.A.

Johan Ludvig Runeberg's Lyrical Songs, Idylls and Epigrams. Fcap. 8vo. Cloth, price 5s.

MAIR (R. S.), M.D., F.R.C.S.E.

The Medical Guide for Anglo-Indians. Being a Compendium of Advice to Europeans in India, relating to the Preservation and Regulation of Health. With a Supplement on the Management of Children in India. Second Edition. Crown 8vo. Limp cloth, price 3s. 6d.

MALDEN (H. E. and E. E.)

Princes and Princesses. Illustrated. Small crown 8vo. Cloth, price 2s. 6d.

MANNING (His Eminence Cardinal).

Essays on Religion and Literature. By various Writers. Third Series. Demy 8vo. Cloth, price 10s. 6d.

The Independence of the Holy See, with an Appendix containing the Papal Allocution and a translation. Cr. 8vo. Cloth, price 5s.

The True Story of the Vatican Council. Crown 8vo. Cloth, price 5s.

MAREY (E. J.).

Animal Mechanics. A Treatise on Terrestrial and Aerial Locomotion. With 117 Illustrations. Second Edition. Crown 8vo. Cloth, price 5s.

Volume XI. of The International Scientific Series.

MARKHAM (Capt. Albert Hastings), R.N.

The Great Frozen Sea. A Personal Narrative of the Voyage of the "Alert" during the Arctic Expedition of 1875-6. With six full-page Illustrations, two Maps, and twenty-seven Woodcuts. Fourth and cheaper edition. Crown 8vo. Cloth, price 6s.

Master Bobby: a Tale. By the Author of "Christina North." With Illustrations by E. H. BELL. Extra fcap. 8vo. Cloth, price 3s. 6d.

MASTERMAN (J.).

Half-a-dozen Daughters. With a Frontispiece. Crown 8vo. Cloth, price 3s. 6d.

MAUDSLEY (Dr. H.).

Responsibility in Mental Disease. Third Edition. Crown 8vo. Cloth, price 5s.

Volume VIII. of The International Scientific Series.

MEREDITH (George).

The Egoist. A Comedy in Narrative. 3 vols. Crown 8vo. Cloth.

* * * Also a Cheaper Edition, with Frontispiece. Crown 8vo. Cloth, price 6s.

The Ordeal of Richard Feverel. A History of Father and Son. In one vol. with Frontispiece. Crown 8vo. Cloth, price 6s.

MERRITT (Henry).

Art - Criticism and Romance. With Recollections, and Twenty-three Illustrations in *eau-forte*, by Anna Lea Merritt. Two vols. Large post 8vo. Cloth, 25s.

MIDDLETON (The Lady).

Ballads. Square 16mo. Cloth, price 3s. 6d.

MILLER (Edward).

The History and Doctrines of Irvingism; or, the so-called Catholic and Apostolic Church. 2 vols. Large post 8vo. Cloth, price 25s.

The Church in Relation to the State. Crown 8vo. Cloth, price 7s. 6d.

MILNE (James).

Tables of Exchange for the
Conversion of Sterling Money into
Indian and Ceylon Currency, at
Rates from 1s. 8d. to 2s. 3d. per
Rupee. Second Edition. Demy
8vo. Cloth, price £2 2s.

MINCHIN (J. G.).

Bulgaria since the War.
Notes of a Tour in the Autumn of
1879. Small crown 8vo. Cloth,
price 3s. 6d.

MIVART (St. George), F.R.S.

Contemporary Evolution :
An Essay on some recent Social
Changes. Post 8vo. Cloth, price
7s. 6d.

MOCKLER (E.).

**A Grammar of the Baloo-
chee Language,** as it is spoken in
Makran (Ancient Gedrosia), in the
Persia-Arabic and Roman characters.
Fcap. 8vo. Cloth, price 5s.

MOFFAT (Robert Scott).

**The Economy of Consump-
tion;** an Omitted Chapter in Political
Economy, with special reference to
the Questions of Commercial Crises
and the Policy of Trades Unions; and
with Reviews of the Theories of Adam
Smith, Ricardo, J. S. Mill, Fawcett,
&c. Demy 8vo. Cloth, price 18s.

**The Principles of a Time
Policy :** being an Exposition of a
Method of Settling Disputes between
Employers and Employed in regard
to Time and Wages, by a simple Pro-
cess of Mercantile Barter, without
recourse to Strikes or Locks-out.
Reprinted from "The Economy of
Consumption," with a Preface and
Appendix containing Observations on
some Reviews of that book, and a Re-
criticism of the Theories of Ricardo
and J. S. Mill on Rent, Value, and
Cost of Production. Demy 8vo.
Cloth, price 3s. 6d.

MOLTKE (Field-Marshal Von).

Letters from Russia.
Translated by Robina Napier.
Crown 8vo. Cloth, price 6s.

Notes of Travel. Being Ex-
tracts from the Journals of. Crown
8vo. Cloth, price 6s.

Monmouth: A Drama, of which
the Outline is Historical. Dedicated
by permission to Mr. Henry Irving.
Small crown 8vo. Cloth, price 5s.

MORELL (J. R.).

**Euclid Simplified in Me-
thod and Language.** Being a
Manual of Geometry. Compiled from
the most important French Works,
approved by the University of Paris
and the Minister of Public Instruc-
tion. Fcap. 8vo. Cloth, price 2s. 6d.

MORICE (Rev. F. D.), M.A.

**The Olympian and Pythian
Odes of Pindar.** A New Transla-
tion in English Verse. Crown 8vo.
Cloth, price 7s. 6d.

MORSE (E. S.), Ph.D.

First Book of Zoology.
With numerous Illustrations. Crown
8vo. Cloth, price 5s.

MORSHEAD (E. D. A.)

**The Agamemnon of Æs-
chylus.** Translated into English
verse. With an Introductory Essay.
Crown 8vo. Cloth, price 5s.

MORTERRA (Felix).

The Legend of Allandale,
and other Poems. Small crown 8vo.
Cloth, price 6s.

NAAKE (J. T.).

Slavonic Fairy Tales.
From Russian, Servian, Polish, and
Bohemian Sources. With Four Illus-
trations. Crown 8vo. Cloth, price 5s.

NEWMAN (J. H.), D.D.

**Characteristics from the
Writings of.** Being Selections
from his various Works. Arranged
with the Author's personal approval.
Third Edition. With Portrait.
Crown 8vo. Cloth, price 6s.

* * A Portrait of the Rev. Dr. J. H.
Newman, mounted for framing, can
be had, price 2s. 6d.

**NICHOLAS (Thomas), Ph.D.,
F.G.S.**

**The Pedigree of the English
People:** an Argument, Historical
and Scientific, on the Formation and
Growth of the Nation, tracing Race-
admixture in Britain from the earliest
times, with especial reference to the
incorporation of the Celtic Aborig-
ines. Fifth Edition. Demy 8vo.
Cloth, price 16s.

NICHOLSON (Edward Byron).

The Christ Child, and other Poems. Crown 8vo. Cloth, price 4s. 6d.

The Rights of an Animal. Crown 8vo. Cloth, price 3s. 6d.

The Gospel according to the Hebrews. Its Fragments translated and annotated, with a critical Analysis of the External and Internal Evidence relating to it. Demy 8vo. Cloth, price 9s. 6d.

NICOLS (Arthur), F.G.S., F.R.G.S.

Chapters from the Physical History of the Earth. An Introduction to Geology and Palæontology, with numerous illustrations. Crown 8vo. Cloth, price 5s.

NOAKE (Major R. Crompton).

The Bivouac; or, Martial Lyrist, with an Appendix—Advice to the Soldier. Fcap. 8vo. Price 5s. 6d.

NORMAN PEOPLE (The).

The Norman People, and their Existing Descendants in the British Dominions and the United States of America. Demy 8vo. Cloth, price 21s.

NORRIS (Rev. Alfred).

The Inner and Outer Life Poems. Fcap. 8vo. Cloth, price 6s.

Notes on Cavalry Tactics, Organization, &c. By a Cavalry Officer. With Diagrams. Demy 8vo. Cloth, price 12s.

Nuces: Exercises on the Syntax of the Public School Latin Primer. New Edition in Three Parts. Crown 8vo. Each 1s. * * The Three Parts can also be had bound together in cloth, price 3s.

O'BRIEN (Charlotte G.).

Light and Shade. 2 vols. Crown 8vo. Cloth, gilt tops, price 12s.

Ode of Life (The).

Third Edition. Fcap. 8vo. Cloth, price 5s.

O'HAGAN (John).

The Song of Roland. Translated into English Verse. Large post 8vo. Parchment antique, price 10s. 6d.

O'MEARA (Kathleen).

Frederic Ozanam, Professor of the Sorbonne; His Life and Works. Second Edition. Crown 8vo. Cloth, price 7s. 6d.

Oriental Sporting Magazine (The).

A Reprint of the first 5 Volumes, in 2 Volumes. Demy 8vo. Cloth, price 28s.

OWEN (F. M.).

John Keats. A Study. Crown 8vo. Cloth, price 6s.

OWEN (Rev. Robert), B.D.

Sanctorale Catholicum; or Book of Saints. With Notes, Critical, Exegetical, and Historical. Demy 8vo. Cloth, price 18s.

Palace and Prison and Fair Geraldine. Two Tragedies, by the Author of "Ginevra" and the "Duke of Guise." Crown 8vo. Cloth, 6s.

PALGRAVE (W. Gifford).

Hermann Agha; An Eastern Narrative. Third and Cheaper Edition. Crown 8vo. Cloth, price 6s.

PALMER (Charles Walter).

The Weed: a Poem. Small crown 8vo. Cloth, price 3s.

PANDURANG HARI;

Or, Memoirs of a Hindoo. With an Introductory Preface by Sir H. Bartle E. Frere, G.C.S.I., C.B. Crown 8vo. Price 6s.

PARKER (Joseph), D.D.

The Paraclete: An Essay on the Personality and Ministry of the Holy Ghost, with some reference to current discussions. Second Edition. Demy 8vo. Cloth, price 12s.

PARR (Capt. H. Hallam).

A Sketch of the Kafir and Zulu Wars: Guadana to Isandhlwana, with Maps. Small crown 8vo. Cloth, price 5s.

PARSLOE (Joseph).

Our Railways : Sketches, Historical and Descriptive. With Practical Information as to Fares, Rates, &c., and a Chapter on Railway Reform. Crown 8vo. Cloth, price 6s.

PATTISON (Mrs. Mark).

The Renaissance of Art in France. With Nineteen Steel Engravings. 2 vols. Demy 8vo. Cloth, price 32s.

PAUL (C. Kegan).

Mary Wollstonecraft. Letters to Imlay. With Prefatory Memoir by, and Two Portraits in *eau forte*, by Anna Lea Merritt. Crown 8vo. Cloth, price 6s.

Goethe's Faust. A New Translation in Rime. Crown 8vo. Cloth, price 6s.

William Godwin: His Friends and Contemporaries. With Portraits and Facsimiles of the Handwriting of Godwin and his Wife. 2 vols. Square post 8vo. Cloth, price 28s.

The Genius of Christianity Unveiled. Being Essays by William Godwin never before published. Edited, with a Preface, by C. Kegan Paul. Crown 8vo. Cloth, price 7s. 6d.

PAUL (Margaret Agnes).

Gentle and Simple: A Story. 2 vols. Crown 8vo. Cloth, gilt tops, price 12s.

** Also a Cheaper Edition in one vol. with Frontispiece. Crown 8vo. Cloth, price 6s.

PAYNE (John).

Songs of Life and Death. Crown 8vo. Cloth, price 5s.

PAYNE (Prof. J. F.).

Lectures on Education. Price 6d.

II. Fröbel and the Kindergarten system. Second Edition.

PAYNE (Prof. J. F.)—continued.

A Visit to German Schools: Elementary Schools in Germany. Notes of a Professional Tour to inspect some of the Kindergartens, Primary Schools, Public Girls' Schools, and Schools for Technical Instruction in Hamburg, Berlin, Dresden, Weimar, Gotha, Eisenach, in the autumn of 1874. With Critical Discussions of the General Principles and Practice of Kindergartens and other Schemes of Elementary Education. Crown 8vo. Cloth, price 4s. 6d.

PELLETAN (E.).

The Desert Pastor, Jean Jarousseau. Translated from the French. By Colonel E. P. De L'Hoste. With a Frontispiece. New Edition. Fcap. 8vo. Cloth, price 3s. 6d.

PENNELL (H. Cholmondeley).

Pegasus Resaddled. By the Author of "Puck on Pegasus," &c. &c. With Ten Full-page Illustrations by George Du Maurier. Second Edition. Fcap. 4to. Cloth elegant, price 12s. 6d.

PENRICE (Maj. J.), B.A.

A Dictionary and Glossary of the Ko-ran. With copious Grammatical References and Explanations of the Text. 4to. Cloth, price 21s.

PESCHEL (Dr. Oscar).

The Races of Man and their Geographical Distribution. Large crown 8vo. Cloth, price 9s.

PETTIGREW (J. Bell), M.D., F.R.S.

Animal Locomotion; or, Walking, Swimming, and Flying. With 130 Illustrations. Second Edition. Crown 8vo. Cloth, price 5s.

Volume VII. of The International Scientific Series.

PFEIFFER (Emily).

Quarterman's Grace, and other Poems. Crown 8vo. Cloth, price 5s.

Glan Alarch: His Silence and Song. A Poem. Second Edition. Crown 8vo. price 6s.

PFEIFFER (Emily)—*continued.*

Gerard's Monument, and other Poems. Second Edition. Crown 8vo. Cloth, price 6s.

Poems. Second Edition. Crown 8vo. Cloth, price 6s.

Sonnets and Songs. New Edition. 15mo, handsomely printed and bound in cloth, gilt edges, price 5s.

PINCHES (Thomas), M.A.

Samuel Wilberforce: Faith—Service—Recompense. Three Sermons. With a Portrait of Bishop Wilberforce (after a Photograph by Charles Watkins). Crown 8vo. Cloth, price 4s. 6d.

PLAYFAIR (Lieut.-Col.), Her Britannic Majesty's Consul-General in Algiers.

Travels in the Footsteps of Bruce in Algeria and Tunis. Illustrated by facsimiles of Bruce's original Drawings, Photographs, Maps, &c. Royal 4to. Cloth, bevelled boards, gilt leaves, price £3 3s.

POLLOCK (W. H.).

Lectures on French Poets. Delivered at the Royal Institution. Small crown 8vo. Cloth, price 5s.

POUSHKIN (A. S.).

Russian Romance. Translated from the Tales of Belkin, &c. By Mrs. J. Buchan Telfer (*née* Mouravieff). Crown 8vo. Cloth, price 3s. 6d.

PRESBYTER.

Unfoldings of Christian Hope. An Essay showing that the Doctrine contained in the Damnable Clauses of the Creed commonly called Athanasian is unscriptural. Small crown 8vo. Cloth, price 4s. 6d.

PRICE (Prof. Bonamy).

Currency and Banking. Crown 8vo. Cloth, price 6s.

Chapters on Practical Political Economy. Being the Substance of Lectures delivered before the University of Oxford. Large post 8vo. Cloth, price 12s.

Proteus and Amadeus. A

Correspondence. Edited by Aubrey De Vere. Crown 8vo. Cloth, price 5s.

PUBLIC SCHOOLBOY.

The Volunteer, the Militiaman, and the Regular Soldier. Crown 8vo. Cloth, price 5s.

PULPIT COMMENTARY (The).

Edited by the Rev. J. S. EXELL and the Rev. Canon H. D. M. SPENCE.

Ezra, Nehemiah, and Esther. By Rev. Canon G. Rawlinson, M.A.; with Homilies by Rev. Prof. J. R. Thomson, M.A., Rev. Prof. R. A. Redford, LL.B., M.A., Rev. W. S. Lewis, M.A., Rev. J. A. Macdonald, Rev. A. Mackennal, B.A., Rev. W. Clarkson, B.A., Rev. F. Hastings, Rev. W. Dinwiddie, LL.B., Rev. Prof. Rowlands, B.A., Rev. G. Wood, B.A., Rev. Prof. P. C. Barker, LL.B., M.A., and Rev. J. S. Exell. Second Edition. One Vol., price 12s. 6d.

Punjaub (The) and North

Western Frontier of India. By an old Punjaabee. Crown 8vo. Cloth, price 5s.

QUATREFAGES (Prof. A. de).

The Human Species. Second Edition. Crown 8vo. Cloth, price 5s.

Vol. XXVI. of The International Scientific Series.

RAVENSHAW (John Henry), B.C.S.

Gaur: Its Ruins and Inscriptions. Edited with considerable additions and alterations by his Widow. With forty-four photographic illustrations and twenty-five fac-similes of Inscriptions. Super royal 4to. Cloth, 3l. 13s. 6d.

READ (Carveth).

On the Theory of Logic: An Essay. Crown 8vo. Cloth, price 6s.

Realities of the Future Life.

Small crown 8vo. Cloth, price 1s. 6d.

REANEY (Mrs. G. S.).

Blessing and Blessed; a Sketch of Girl Life. With a frontispiece. Crown 8vo. Cloth, price 5s.

Waking and Working; or, from Girlhood to Womanhood. With a Frontispiece. Crown 8vo. Cloth, price 5s.

English Girls: their Place and Power. With a Preface by R. W. Dale, M.A., of Birmingham. Second Edition. Fcap. 8vo. Cloth, price 2s. 6d.

Just Anyone, and other Stories. Three Illustrations. Royal 16mo. Cloth, price 1s. 6d.

Sunshine Jenny and other Stories. Three Illustrations. Royal 16mo. Cloth, price 1s. 6d.

Sunbeam Willie, and other Stories. Three Illustrations. Royal 16mo. Cloth, price 1s. 6d.

REYNOLDS (Rev. J. W.).

The Supernatural in Nature. A Verification by Free Use of Science. Second Edition, revised and enlarged. Demy 8vo. Cloth, price 14s.

Mystery of Miracles, The. By the Author of "The Supernatural in Nature." Crown 8vo. Cloth, price 6s.

RIBOT (Prof. Th.).

English Psychology. Second Edition. A Revised and Corrected Translation from the latest French Edition. Large post 8vo. Cloth, price 9s.

Heredity: A Psychological Study on its Phenomena, its Laws, its Causes, and its Consequences. Large crown 8vo. Cloth, price 9s.

RINK (Chevalier Dr. Henry).

Greenland: Its People and its Products. By the Chevalier Dr. HENRY RINK, President of the Greenland Board of Trade. With sixteen Illustrations, drawn by the Eskimo, and a Map. Edited by Dr. ROBERT BROWN. Crown 8vo. Price 10s. 6d.

ROBERTSON (The Late Rev. F. W.), M.A., of Brighton.

Notes on Genesis. New and cheaper Edition. Crown 8vo., price 3s. 6d.

Sermons. Four Series. Small crown 8vo. Cloth, price 3s. 6d. each.

Expository Lectures on St. Paul's Epistles to the Corinthians. A New Edition. Small crown 8vo. Cloth, price 5s.

Lectures and Addresses, with other literary remains. A New Edition. Crown 8vo. Cloth, price 5s.

An Analysis of Mr. Tennyson's "In Memoriam." (Dedicated by Permission to the Poet-Laureate.) Fcap. 8vo. Cloth, price 2s.

The Education of the Human Race. Translated from the German of Gotthold Ephraim Lessing. Fcap. 8vo. Cloth, price 2s. 6d.

Life and Letters. Edited by the Rev. Stopford Brooke, M.A., Chaplain in Ordinary to the Queen.

I. 2 vols., uniform with the Sermons. With Steel Portrait. Crown 8vo. Cloth, price 7s. 6d.

II. Library Edition, in Demy 8vo., with Two Steel Portraits. Cloth, price 12s.

III. A Popular Edition, in one vol. Crown 8vo. Cloth, price 6s.

The above Works can also be had half-bound in morocco.

** A Portrait of the late Rev. F. W. Robertson, mounted for framing, can be had, price 2s. 6d.

ROBINSON (A. Mary F.).

A Handful of Honey-suckle. Fcap. 8vo. Cloth, price 3s. 6d.

RODWELL (G. F.), F.R.A.S., F.C.S.

Etna: a History of the Mountain and its Eruptions. With Maps and Illustrations. Square 8vo. Cloth, price 9s.

ROOD (Ogden N.).

Modern Chromatics, with Applications to Art and Industry. With 130 Original Illustrations. Crown 8vo. Cloth, price 5s.

Vol. XXVII. of The International Scientific Series.

ROSS (Mrs. E.), ("Nelsie Brook").

Daddy's Pet. A Sketch from Humble Life. With Six Illustrations. Royal 16mo. Cloth, price 1s.

ROSS (Alexander), D.D.

Memoir of Alexander Ewing, Bishop of Argyll and the Isles. Second and Cheaper Edition. Demy 8vo. Cloth, price 10s. 6d.

SADLER (S. W.), R.N.

The African Cruiser. A Midshipman's Adventures on the West Coast. With Three Illustrations. Second Edition. Crown 8vo. Cloth, price 3s. 6d.

SALTS (Rev. Alfred), LL.D.

Godparents at Confirmation. With a Preface by the Bishop of Manchester. Small crown 8vo. Cloth, limp, price 2s.

SAUNDERS (Katherine).

Gideon's Rock, and other Stories. Crown 8vo. Cloth, price 6s.

Joan Merryweather, and other Stories. Crown 8vo. Cloth, price 6s.

Margaret and Elizabeth. A Story of the Sea. Crown 8vo. Cloth, price 6s.

SAUNDERS (John).

Israel Mort, Overman: A Story of the Mine. Cr. 8vo. Price 6s.

Hirell. With Frontispiece. Crown 8vo. Cloth, price 3s. 6d.

Abel Drake's Wife. With Frontispiece. Crown 8vo. Cloth, price 3s. 6d.

SAYCE (Rev. Archibald Henry).

Introduction to the Science of Language. Two vols., large post 8vo. Cloth, price 25s.

SHELL (Maj. von).

The Operations of the First Army under Gen. von Goeben. Translated by Col. C. H. von Wright. Four Maps. Demy 8vo. Cloth, price 9s.

SHELL (Maj. von)—*continued.*

The Operations of the First Army under Gen. von Steinmetz. Translated by Captain E. O. Hollist. Demy 8vo. Cloth, price 10s. 6d.

SHELLENDORF (Maj.-Gen. B. von).

The Duties of the General Staff. Translated from the German by Lieutenant Hare. Vol. I. Demy 8vo. Cloth, 10s. 6d.

SCHERFF (Maj. W. von).

Studies in the New Infantry Tactics. Parts I. and II. Translated from the German by Colonel Lumley Graham. Demy 8vo. Cloth, price 7s. 6d.

SCHMIDT (Prof. Oscar).

The Doctrine of Descent and Darwinism. With 26 Illustrations. Third Edition. Crown 8vo. Cloth, price 5s.

Volume XII. of The International Scientific Series.

SCHÜTZENBERGER (Prof. F.).

Fermentation. With Numerous Illustrations. Second Edition. Crown 8vo. Cloth, price 5s.

Volume XX. of The International Scientific Series.

SCOONES (W. Baptiste).

Four Centuries of English Letters. A Selection of 350 Letters by 150 Writers from the period of the Paston Letters to the Present Time. Edited and arranged by. Large crown 8vo. Cloth, price 9s.

SCOTT (Leader).

A Nook in the Apennines: A Summer beneath the Chestnuts. With Frontispiece, and 27 Illustrations in the Text, chiefly from Original Sketches. Crown 8vo. Cloth, price 7s. 6d.

SCOTT (Robert H.).

Weather Charts and Storm Warnings. Illustrated. Second Edition. Crown 8vo. Cloth, price 3s. 6d.

Seeking his Fortune, and other Stories. With Four Illustrations. Crown 8vo. Cloth, price 3s. 6d.

SENIOR (N. W.).**Alexis De Tocqueville.**

Correspondence and Conversations with Nassau W. Senior, from 1833 to 1859. Edited by M. C. M. Simpson. 2 vols. Large post 8vo. Cloth, price 21s.

Sermons to Naval Cadets.

Preached on board H.M.S. "Britannia." Small crown 8vo. Cloth, price 3s. 6d.

Seven Autumn Leaves from

Fairyland. Illustrated with Nine Etchings. Square crown 8vo. Cloth, price 3s. 6d.

SHADWELL (Maj.-Gen.), C.B.

Mountain Warfare. Illustrated by the Campaign of 1799 in Switzerland. Being a Translation of the Swiss Narrative compiled from the Works of the Archduke Charles, Jomini, and others. Also of Notes by General H. Dufour on the Campaign of the Valtelline in 1635. With Appendix, Maps, and Introductory Remarks. Demy 8vo. Cloth, price 16s.

SHAKSPEARE (Charles).

Saint Paul at Athens : Spiritual Christianity in Relation to some Aspects of Modern Thought. Nine Sermons preached at St. Stephen's Church, Westbourne Park. With Preface by the Rev. Canon FARRAR. Crown 8vo. Cloth, price 5s.

SHAW (Major Wilkinson).

The Elements of Modern Tactics. Practically applied to English Formations. With Twenty-five Plates and Maps. Small crown 8vo. Cloth, price 12s.

* * * The Second Volume of "Military Handbooks for Officers and Non-commissioned Officers." Edited by Lieut.-Col. C. B. Brackenbury, R.A., A.A.G.

SHAW (Flora L.).

Castle Blair: a Story of Youthful Lives. 2 vols. Crown 8vo. Cloth, gilt tops, price 12s. Also, an edition in one vol. Crown 8vo. 6s.

SHELLEY (Lady).

Shelley Memorials from Authentic Sources. With (now first printed) an Essay on Christianity by Percy Bysshe Shelley. With Portrait. Third Edition. Crown 8vo. Cloth, price 5s.

SHELLEY (Percy Bysshe).

Poems selected from. Dedicated to Lady Shelley. With Preface by Richard Garnett. Printed on hand-made paper. With miniature frontispiece. Elzevir. 8vo., limp parchment antique. Price 6s., vellum 7s. 6d.

SHERMAN (Gen. W. T.).

Memoirs of General W. T. Sherman, Commander of the Federal Forces in the American Civil War. By Himself. 2 vols. With Map. Demy 8vo. Cloth, price 24s. *Copyright English Edition.*

SHILLITO (Rev. Joseph).

Womanhood: its Duties, Temptations, and Privileges. A Book for Young Women. Second Edition. Crown 8vo. Price 3s. 6d.

SHIPLEY (Rev. Orby), M.A.

Principles of the Faith in Relation to Sin. Topics for Thought in Times of Retreat. Eleven Addresses. With an Introduction on the neglect of Dogmatic Theology in the Church of England, and a Postscript on his leaving the Church of England. Demy 8vo. Cloth, price 12s.

Church Tracts, or Studies in Modern Problems. By various Writers. 2 vols. Crown 8vo. Cloth, price 5s. each.

SMITH (Edward), M.D., LL.B., F.R.S.

Health and Disease, as Influenced by the Daily, Seasonal, and other Cyclical Changes in the Human System. A New Edition. Post 8vo. Cloth, price 7s. 6d.

Foods. Profusely Illustrated. Sixth Edition. Crown 8vo. Cloth, price 5s.

Volume III. of The International Scientific Series.

SMITH (Edward), M.D., LL.B., F.R.S.—*continued.*

Practical Dietary for Families, Schools, and the Labouring Classes. A New Edition. Post 8vo. Cloth, price 3s. 6d.

Tubercular Consumption in its Early and Remediabale Stages. Second Edition. Crown 8vo. Cloth, price 6s.

Songs of Two Worlds. By the Author of "The Epic of Hades." Fifth Edition. Complete in one Volume, with Portrait. Fcap. 8vo. Cloth, price 7s. 6d.

Songs for Music.

By Four Friends. Square crown 8vo. Cloth, price 5s.
Containing songs by Reginald A. Gatty, Stephen H. Gatty, Greville J. Chester, and Juliana Ewing.

SPEDDING (James).

Reviews and Discussions, Literary, Political, and Historical, not relating to Bacon. Demy 8vo. Cloth, price 12s. 6d.

SPENCER (Herbert).

The Study of Sociology. Eighth Edition. Crown 8vo. Cloth, price 5s.

Volume V. of The International Scientific Series.

STEDMAN (Edmund Clarence).

Lyrics and Idylls. With other Poems. Crown 8vo. Cloth, price 7s. 6d.

STEPHENS (Archibald John), LL.D.

The Folkestone Ritual Case. The Substance of the Argument delivered before the Judicial Committee of the Privy Council. On behalf of the Respondents. Demy 8vo. Cloth, price 6s.

STEVENS (William).

The Truce of God, and other Poems. Small crown 8vo. Cloth, price 3s. 6d.

STEVENSON (Robert Louis).

An Inland Voyage. With Frontispiece by Walter Crane. Crown 8vo. Cloth, price 7s. 6d.

STEVENSON (Robert Louis)—*continued.*

Travels with a Donkey in the Cevennes. With Frontispiece by Walter Crane. Crown 8vo. Cloth, price 7s. 6d.

STEVENSON (Rev. W. F.).

Hymns for the Church and Home. Selected and Edited by the Rev. W. Fleming Stevenson.

The most complete Hymn Book published.

The Hymn Book consists of Three Parts :—I. For Public Worship.—II. For Family and Private Worship.—III. For Children.

*** Published in various forms and prices, the latter ranging from 8d. to 6s. Lists and full particulars will be furnished on application to the Publishers.*

STEWART (Prof. Balfour), M.A., LL.D., F.R.S.

On the Conservation of Energy. Fifth Edition. With Fourteen Engravings. Crown 8vo. Cloth, price 5s.

Volume VI. of The International Scientific Series.

STORR (Francis), and TURNER Hawes).

Canterbury Chimes; or, Chaucer Tales retold to Children. With Illustrations from the Ellesmere MS. Extra Fcap. 8vo. Cloth, price 3s. 6d.

STRETTON (Hesba).

David Lloyd's Last Will. With Four Illustrations. Royal 16mo., price 2s. 6d.

The Wonderful Life. Thirteenth Thousand. Fcap. 8vo. Cloth, price 2s. 6d.

Through a Needle's Eye: a Story. 2 vols. Crown 8vo. Cloth, gilt top, price 12s.

*** Also a Cheaper Edition in one volume, with Frontispiece. Crown 8vo. Cloth, price 6s.*

STUBBS (Lieut.-Colonel F. W.)

The Regiment of Bengal Artillery. The History of its Organization, Equipment, and War Services. Compiled from Published Works, Official Records, and various Private Sources. With numerous Maps and Illustrations. 2 vols. Demy 8vo. Cloth, price 32s.

STUMM (Lieut. Hugo), German Military Attaché to the Khivan Expedition.

Russia's advance Eastward. Based on the Official Reports of. Translated by Capt. C. E. H. VINCENT. With Map. Crown 8vo. Cloth, price 6s.

SULLY (James), M.A.
Sensation and Intuition. Demy 8vo. Cloth, price 10s. 6d.

Pessimism : a History and a Criticism. Demy 8vo. Price 14s.

Sunnyland Stories.
By the Author of "Aunt Mary's Bran Pie." Illustrated. Small 8vo. Cloth, price 3s. 6d.

Sweet Silvery Sayings of Shakespeare. Crown 8vo. Cloth gilt, price 7s. 6d.

SYME (David).
Outlines of an Industrial Science. Second Edition. Crown 8vo. Cloth, price 6s.

Tales from Ariosto. Retold for Children, by a Lady. With three illustrations. Crown 8vo. Cloth, price 4s. 6d.

TAYLOR (Algernon).
Guienne. Notes of an Autumn Tour. Crown 8vo. Cloth, price 4s. 6d.

TAYLOR (Sir H.).
Works Complete. Author's Edition, in 5 vols. Crown 8vo. Cloth, price 6s. each.

Vols. I. to III. containing the Poetical Works, Vols. IV. and V. the Prose Works.

TAYLOR (Col. Meadows), C.S.I., M.R.I.A.
A Noble Queen : a Romance of Indian History. Crown 8vo. Cloth. Price 6s.

Seeta. 3 vols. Crown 8vo. Cloth.

Tippoo Sultaun : a Tale of the Mysore War. New Edition with Frontispiece. Crown 8vo. Cloth, price 6s.

TAYLOR (Col. Meadows), C.S.I., M.R.I.A.—*continued.*

Ralph Darnell. New and Cheaper Edition. With Frontispiece. Crown 8vo. Cloth, price 6s.

The Confessions of a Thug. New Edition. Crown 8vo. Cloth, price 6s.

Tara : a Mahratta Tale. New Edition. Crown 8vo. Cloth, price 6s.

TEBBITT (Charles) and Francis Lloyd.

Extension of Empire Weakness? Deficits Ruin? With a Practical Scheme for the Reconstruction of Asiatic Turkey. Small crown 8vo. Cloth, price 3s. 6d.

TENNYSON (Alfred).
The Imperial Library Edition. Complete in 7 vols. Demy 8vo. Cloth, price £3 13s. 6d.; in Roxburgh binding, £4 7s. 6d.

Author's Edition. Complete in 6 Volumes. Post 8vo. Cloth gilt; or half-morocco, Roxburgh style :—

VOL. I. Early Poems, and English Idylls. Price 6s.; Roxburgh, 7s. 6d.

VOL. II. Locksley Hall, Lucretius, and other Poems. Price 6s.; Roxburgh, 7s. 6d.

VOL. III. The Idylls of the King (Complete). Price 7s. 6d.; Roxburgh, 9s.

VOL. IV. The Princess, and Maud. Price 6s.; Roxburgh, 7s. 6d.

VOL. V. Enoch Arden, and In Memoriam. Price 6s.; Roxburgh, 7s. 6d.

VOL. VI. Dramas. Price 7s.; Roxburgh, 8s. 6d.

Cabinet Edition. 12 vols. Each with Frontispiece. Fcap. 8vo. Cloth, price 2s. 6d. each.

CABINET EDITION. 12 vols. Complete in handsome Ornamental Case. 32s.

Pocket Volume Edition. 13 vols. In neat case, 36s. Ditto, ditto. Extra cloth gilt, in case, 42s.

TENNYSON (Alfred)—continued.

The Royal Edition. Complete in one vol. Cloth, 16s. Cloth extra, 18s. Roxburgh, half morocco, price 20s.

The Guinea Edition. Complete in 12 vols., neatly bound and enclosed in box. Cloth, price 21s. French morocco, price 31s. 6d.

The Shilling Edition of the Poetical and Dramatic Works, in 12 vols., pocket size. Price 1s. each.

The Crown Edition. Complete in one vol., strongly bound in cloth, price 6s. Cloth, extra gilt leaves, price 7s. 6d. Roxburgh, half morocco, price 8s. 6d.

** Can also be had in a variety of other bindings.

Original Editions :

The Lover's Tale. (Now for the first time published.) Fcap. 8vo. Cloth, 3s. 6d.

Poems. Small 8vo. Cloth, price 6s.

Maud, and other Poems. Small 8vo. Cloth, price 3s. 6d.

The Princess. Small 8vo. Cloth, price 3s. 6d.

Idylls of the King. Small 8vo. Cloth, price 5s.

Idylls of the King. Complete. Small 8vo. Cloth, price 6s.

The Holy Grail, and other Poems. Small 8vo. Cloth, price 4s. 6d.

Gareth and Lynette. Small 8vo. Cloth, price 3s.

Enoch Arden, &c. Small 8vo. Cloth, price 3s. 6d.

In Memoriam. Small 8vo. Cloth, price 4s.

Queen Mary. A Drama. New Edition. Crown 8vo. Cloth, price 6s.

Harold. A Drama. Crown 8vo. Cloth, price 6s.

Selections from Tennyson's Works. Super royal 16mo. Cloth, price 3s. 6d. Cloth gilt extra, price 4s.

TENNYSON (Alfred)—continued.

Songs from Tennyson's Works. Super royal 16mo. Cloth extra, price 3s. 6d.

Also a cheap edition. 16mo. Cloth, price 2s. 6d.

Idylls of the King, and other Poems. Illustrated by Julia Margaret Cameron. 2 vols. Folio. Half-bound morocco, cloth sides, price £6 6s. each.

Tennyson for the Young and for Recitation. Specially arranged. Fcap. 8vo. Price 1s. 6d.

Tennyson Birthday Book.

Edited by Emily Shakespear. 32mo. Cloth limp, 2s.; cloth extra, 3s.

** A superior edition, printed in red and black, on antique paper, specially prepared. Small crown 8vo. Cloth extra, gilt leaves, price 5s.; and in various calf and morocco bindings.

In Memoriam. A new Edition, choicely printed on hand-made paper, with a Miniature Portrait in *eau forte* by Le Rat, after a photograph by the late Mrs. Cameron. Bound in limp parchment, antique, price 6s., vellum 7s. 6d.

The Princess. A Medley. Choicely printed on hand-made paper, with a miniature frontispiece by H. M. Paget and a tail-piece in outline by Gordon Browne. Limp parchment, antique, price 6s., vellum, price 7s.

Songs Set to Music, by various Composers. Edited by W. G. Cusins. Dedicated by express permission to Her Majesty the Queen. Royal 4to. Cloth extra, gilt leaves, price 21s., or in half-morocco, price 25s.

THOMAS (Moy).

A Fight for Life. With Frontispiece. Crown 8vo. Cloth, price 3s. 6d.

THOMPSON (Alice C.).

Preludes. A Volume of Poems. Illustrated by Elizabeth Thompson (Painter of "The Roll Call"). 8vo. Cloth, price 7s. 6d.

THOMSON (J. Turnbull).

Social Problems; or, an Inquiry into the Law of Influences. With Diagrams. Demy 8vo. Cloth, price 10s. 6d.

THRING (Rev. Godfrey), B.A.
Hymns and Sacred Lyrics.

Fcap. 8vo. Cloth, price 3s. 6d.

THURSTON (Prof. R. H.).

A History of the Growth of the Steam Engine. With numerous Illustrations. Second Edition. Crown 8vo. Cloth, price 6s. 6d.

TODHUNTER (Dr. J.)

A Study of Shelley. Crown 8vo. Cloth, price 7s.

Alcegis : A Dramatic Poem. Extra fcap. 8vo. Cloth, price 5s.

Laurella; and other Poems. Crown 8vo. Cloth, price 6s. 6d.

TOLINGSBY (Frere).

Elnora. An Indian Mythological Poem. Fcap. 8vo. Cloth, price 6s.

Translations from Dante, Petrarch, Michael Angelo, and Vittoria Colonna. Fcap. 8vo. Cloth, price 7s. 6d.

TURNER (Rev. C. Tennyson).

Sonnets, Lyrics, and Translations. Crown 8vo. Cloth, price 4s. 6d.

TWINING (Louisa).

Recollections of Work-house Visiting and Management during twenty-five years. Small crown 8vo. Cloth, price 3s. 6d.

TYNDALL (John), LL.D., F.R.S
Forms of Water. A Familiar Exposition of the Origin and Phenomena of Glaciers. With Twenty-five Illustrations. Seventh Edition. Crown 8vo. Cloth, price 5s.

Volume I. of The International Scientific Series.

VAN BENEDEN (Mons.).

Animal Parasites and Messmates. With 83 Illustrations. Second Edition. Cloth, price 5s.

Volume XIX. of The International Scientific Series.

VAUGHAN (H. Halford), sometime Regius Professor of Modern History in Oxford University.

New Readings and Renderings of Shakespeare's Tragedies. Vol. I. Demy 8vo. Cloth, price 15s.

VILLARI (Prof.).

Niccolo Machiavelli and His Times. Translated by Linda Villari. 2 vols. Large post 8vo. Cloth, price 24s.

VINCENT (Capt. C. E. H.).

Elementary Military Geography, Reconnoitring, and Sketching. Compiled for Non-Commissioned Officers and Soldiers of all Arms. Square crown 8vo. Cloth, price 2s. 6d.

VOGEL (Dr. Hermann).

The Chemical Effects of Light and Photography, in their application to Art, Science, and Industry. The translation thoroughly revised. With 100 Illustrations, including some beautiful specimens of Photography. Third Edition. Crown 8vo. Cloth, price 5s.

Volume XV. of The International Scientific Series.

VYNER (Lady Mary).

Every day a Portion. Adapted from the Bible and the Prayer Book, for the Private Devotions of those living in Widowhood. Collected and edited by Lady Mary Vyner. Square crown 8vo. Cloth extra, price 5s.

WALDSTEIN (Charles), Ph. D.

The Balance of Emotion and Intellect: An Essay Introductory to the Study of Philosophy. Crown 8vo. Cloth, price 6s.

WALLER (Rev. C. B.)

The Apocalypse, Reviewed under the Light of the Doctrine of the Unfolding Ages and the Restitution of all Things. Demy 8vo. Cloth, price 12s.

WALTERS (Sophia Lydia).

The Brook : A Poem. Small crown 8vo. Cloth, price 3s. 6d.

WALTERS (Sophia Lydia)—*continued.*

A Dreamer's Sketch Book.

With Twenty-one Illustrations by Percival Skelton, R. P. Leitch, W. H. J. Boot, and T. R. Pritchett. Engraved by J. D. Cooper. Fcap. 4to. Cloth, price 12s. 6d.

WARTENSLEBEN (Count H. von).

The Operations of the South Army in January and February, 1871. Compiled from the Official War Documents of the Head-quarters of the Southern Army. Translated by Colonel C. H. von Wright. With Maps. Demy 8vo. Cloth, price 6s.

The Operations of the First Army under Gen. von Manteuffel. Translated by Colonel C. H. von Wright. Uniform with the above. Demy 8vo. Cloth, price 9s.

WATERFIELD, W.

Hymns for Holy Days and Seasons. 32mo. Cloth, price 1s. 6d.

WATSON (William).

The Prince's Quest and other Poems. Crown 8vo. Cloth, price 5s.

WATSON (Sir Thomas), Bart., M.D.

The Abolition of Zymotic Diseases, and of other similar enemies of Mankind. Small crown 8vo. Cloth, price 3s. 6d.

WAY (A.), M.A.

The Odes of Horace Literally Translated in Metre. Fcap. 8vo. Cloth, price 2s.

WEBSTER (Augusta).

Disguises. A Drama. Small crown 8vo. Cloth, price 5s.

WEDMORE (Frederick).

The Masters of Genre Painting. With sixteen illustrations. Crown 8vo. Cloth, price 7s. 6d.

WELLS (Capt. John C.), R.N.

Spitzbergen—The Gateway to the Polynia; or, A Voyage to Spitzbergen. With numerous illustrations by Whymper and others, and Map. New and Cheaper Edition. Demy 8vo. Cloth, price 6s.

Wet Days, by a Farmer. Small crown 8vo. Cloth, price 6s.

WETMORE (W. S.).

Commercial Telegraphic Code. Second Edition. Post 4to. Boards, price 42s.

WHITAKER (Florence).

Christy's Inheritance. A London Story. Illustrated. Royal 16mo. Cloth, price 1s. 6d.

WHITE (A. D.), LL.D.

Warfare of Science. With Prefatory Note by Professor Tyndall. Second Edition. Crown 8vo. Cloth, price 3s. 6d.

WHITNEY (Prof. W. D.)

The Life and Growth of Language. Second Edition. Crown 8vo. Cloth, price 5s. *Copyright Edition.*

Volume XVI. of The International Scientific Series.

Essentials of English Grammar for the Use of Schools. Crown 8vo. Cloth, price 3s. 6a.

WICKHAM (Capt. E. H., R.A.)

Influence of Firearms upon Tactics: Historical and Critical Investigations. By an OFFICER OF SUPERIOR RANK (in the German Army). Translated by Captain E. H. Wickham, R.A. Demy 8vo. Cloth, price 7s. 6d.

WICKSTEED (P. H.).

Dante: Six Sermons. Crown 8vo. Cloth, price 5s.

WILLIAMS (Rowland), D.D.

Life and Letters of, with Extracts from his Note-Books. Edited by Mrs. Rowland Williams. With a Photographic Portrait. 2 vols. Large post 8vo. Cloth, price 24s.

Stray Thoughts from the Note-Books of the Late Rowland Williams, D.D. Edited by his Widow. Crown 8vo. Cloth, price 3s. 6d.

Psalms, Litanies, Counsels and Collects for Devout Persons. Edited by his Widow. New and Popular Edition. Crown 8vo. Cloth, price 3s. 6d.

WILLIS (R.), M.D.

Servetus and Calvin : a Study of an Important Epoch in the Early History of the Reformation. 8vo. Cloth, price 16s.

William Harvey. A History of the Discovery of the Circulation of the Blood. With a Portrait of Harvey, after Faithorne. Demy 8vo. Cloth, price 14s.

WILLOUGHBY (The Hon. Mrs.).

On the North Wind—Thistledown. A Volume of Poems. Elegantly bound. Small crown 8vo. Cloth, price 7s. 6d.

WILSON (H. Schütz).

The Tower and Scaffold. A Miniature Monograph. Large fcap. 8vo. Price 1s.

Within Sound of the Sea.

By the Author of "Blue Roses," "Vera," &c. Third Edition. 2 vols. Crown 8vo. Cloth, gilt tops, price 12s.

* * Also a cheaper edition in one Vol. with frontispiece. Crown 8vo. Cloth, price 6s.

WOINOVITS (Capt. I.).

Austrian Cavalry Exercise. Translated by Captain W. S. Cooke. Crown 8vo. Cloth, price 7s.

WOLLSTONECRAFT (Mary).

Letters to Imlay. With a Preparatory Memoir by C. Kegan Paul, and two Portraits in *eau forte* by Anna Lea Merritt. Crown 8vo. Cloth, price 6s.

WOOD (Major-General J. Creighton).

Doubling the Consonant. Small crown 8vo. Cloth, price 1s. 6d.

WOODS (James Chapman).

A Child of the People, and other poems. Small crown 8vo. Cloth, price 5s.

WRIGHT (Rev. David), M.A.

Waiting for the Light, and other Sermons. Crown 8vo. Cloth, price 6s.

YOUMANS (Eliza A.).

An Essay on the Culture of the Observing Powers of Children, especially in connection with the Study of Botany. Edited, with Notes and a Supplement, by Joseph Payne, F.C.P., Author of "Lectures on the Science and Art of Education," &c. Crown 8vo. Cloth, price 2s. 6d.

First Book of Botany.

Designed to Cultivate the Observing Powers of Children. With 300 Engravings. New and Cheaper Edition. Crown 8vo. Cloth, price 2s. 6d.

YOUMANS (Edward L.), M.D.

A Class Book of Chemistry, on the Basis of the New System. With 200 Illustrations. Crown 8vo. Cloth, price 5s.

YOUNG (William).

Gottlob, etcetera. Small crown 8vo. Cloth, price 3s. 6d.

ZIMMERN (H.).

Stories in Precious Stones. With Six Illustrations. Third Edition. Crown 8vo. Cloth, price 5s.



THE
INTERNATIONAL
SCIENTIFIC SERIES

